

# Characterizing social information spreading by using event synchronization and causality measures

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# Data

- 28000 news articles published in Argentina in six main cities.
- 26/05/2022 - 26/09/2022
- Use an unsupervised non-negative matrix factorization algorithm to classify the articles in 20 non-orthogonal topics.



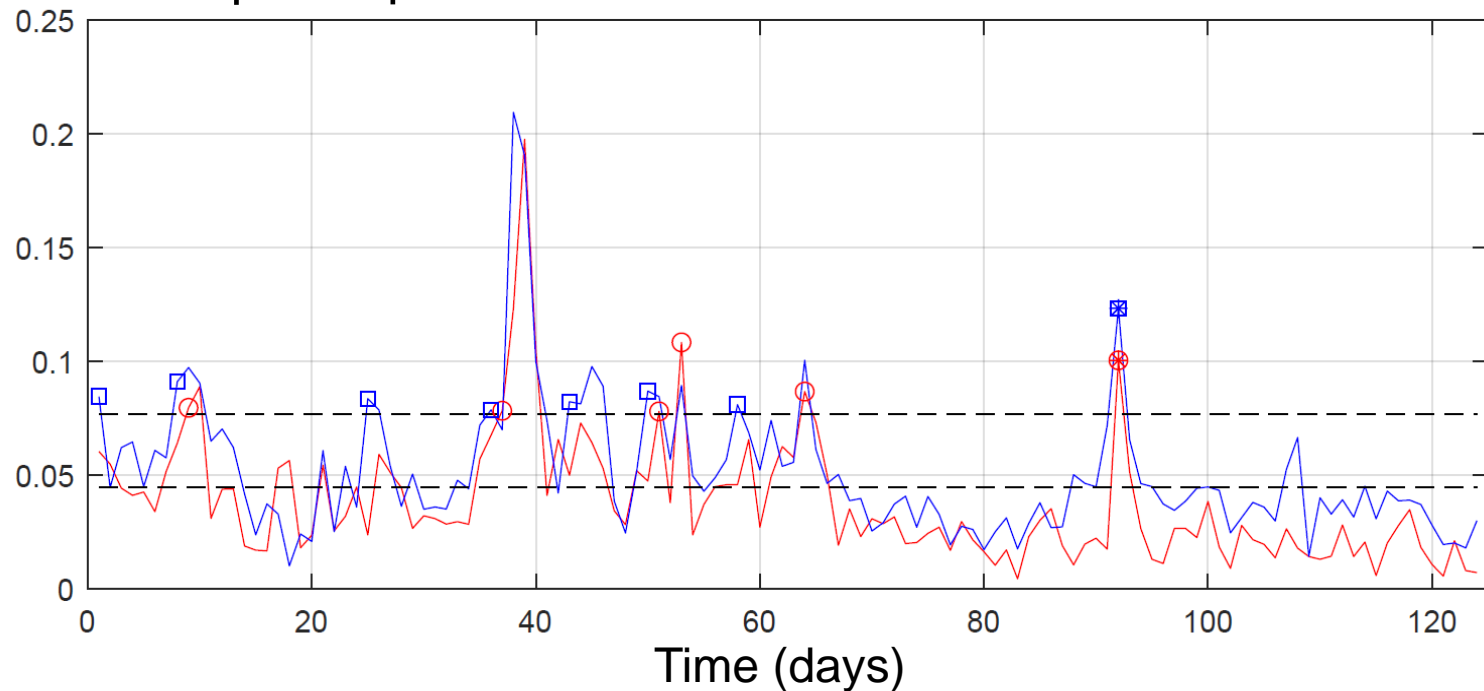
S. Pinto, F. Albanese, C. O. Dorso, and P. Balenzuela. *Quantifying time-dependent media agenda and public opinion by topic modeling*. Physica A, 524:614, 2019

# Data

We obtain a time series for each topic in each town, by adding the number of articles per day.

We define “events” using two thresholds.

Example: Topic “*Alberto Fernandez*” in **BsAs** and in **Mendoza**



# How to find “synchronized events” in two time series?

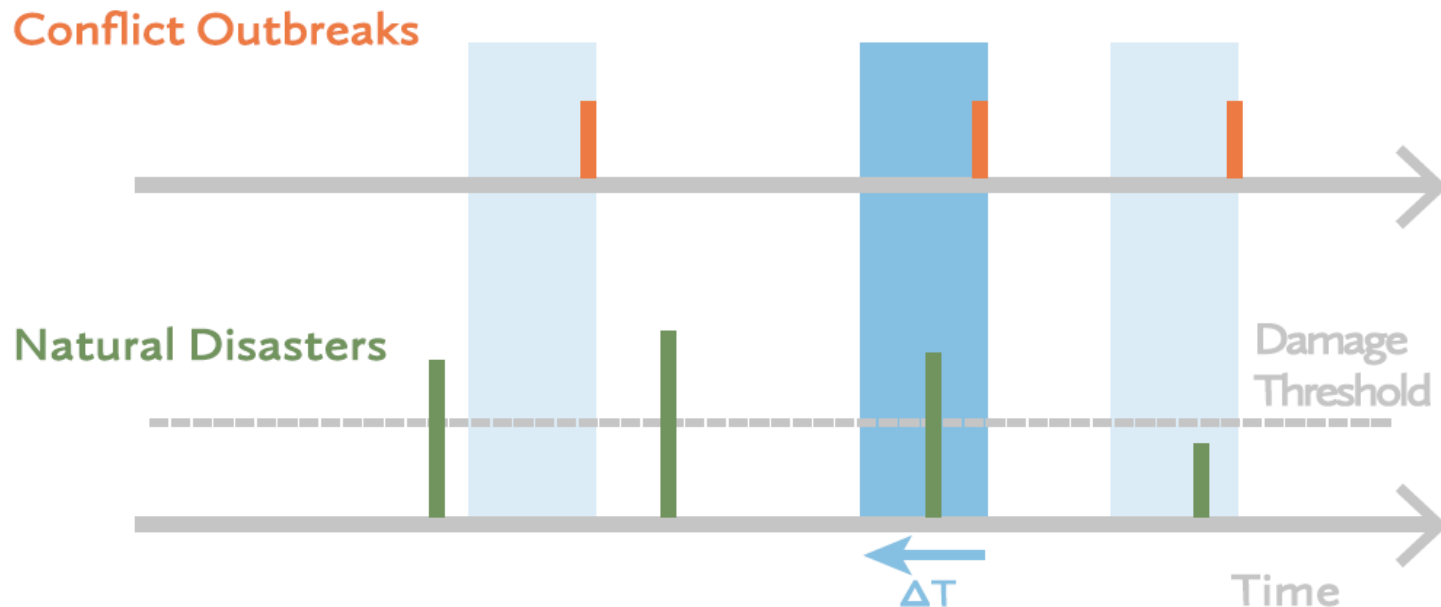
## Example

# Armed-conflict risks enhanced by climate-related disasters in ethnically fractionalized countries

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9216–9221 | PNAS | August 16, 2016 | vol. 113 | no. 33



# Event synchronization measures

- Define “events” in each time series.
- Count  $c^\tau(x|y)$  = number of times an event appears in  $x$  shortly after (within interval  $\tau$ ) an event appears in  $y$ . Idem for  $c^\tau(y|x)$ .
- Calculate:

$$Q_\tau = \frac{c^\tau(y|x) + c^\tau(x|y)}{\sqrt{m_x m_y}} \qquad q_\tau = \frac{c^\tau(y|x) - c^\tau(x|y)}{\sqrt{m_x m_y}}$$

$m_x, m_y$  are the number of events in each time series.

- $Q_\tau = 1$  : the events of the signals are fully synchronized.
- $q_\tau = 1$  : the events in  $x$  always occur before those in  $y$ .
- $q_\tau = -1$  : the events in  $x$  always occur after those in  $y$ .

No “causal” information

Quián Quiroga et al, *PRE* 66, 041904 (2002).

# Granger Causality

Hypothesis:  $X_1$  and  $X_2$  can be described by stationary autoregressive linear models.

$$X_1(t) = \sum_{j=1}^p \text{past of } X_1 A_{11,j} X_1(t-j) + \text{Residual error } E_1(t)$$

$$X_1(t) = \sum_{j=1}^p \text{past of } X_1 A_{11,j} X_1(t-j) + \sum_{j=1}^p \text{past of } X_2 A_{12,j} X_2(t-j) + \text{Residual error } E'_1(t)$$

$$\text{If } \langle E'_1(t) \rangle < \langle E_1(t) \rangle \quad \longrightarrow \quad X_2 \rightarrow X_1$$

C. W. J. Granger *Investigating causal relations by econometric models and cross-spectral methods*. *Econometrica* 37, 424–438 (1969) (> 10000 citations)

# Transfer Entropy (TE)

- TE: is the *Conditional* Mutual Information, given the “past” of one of the variables.

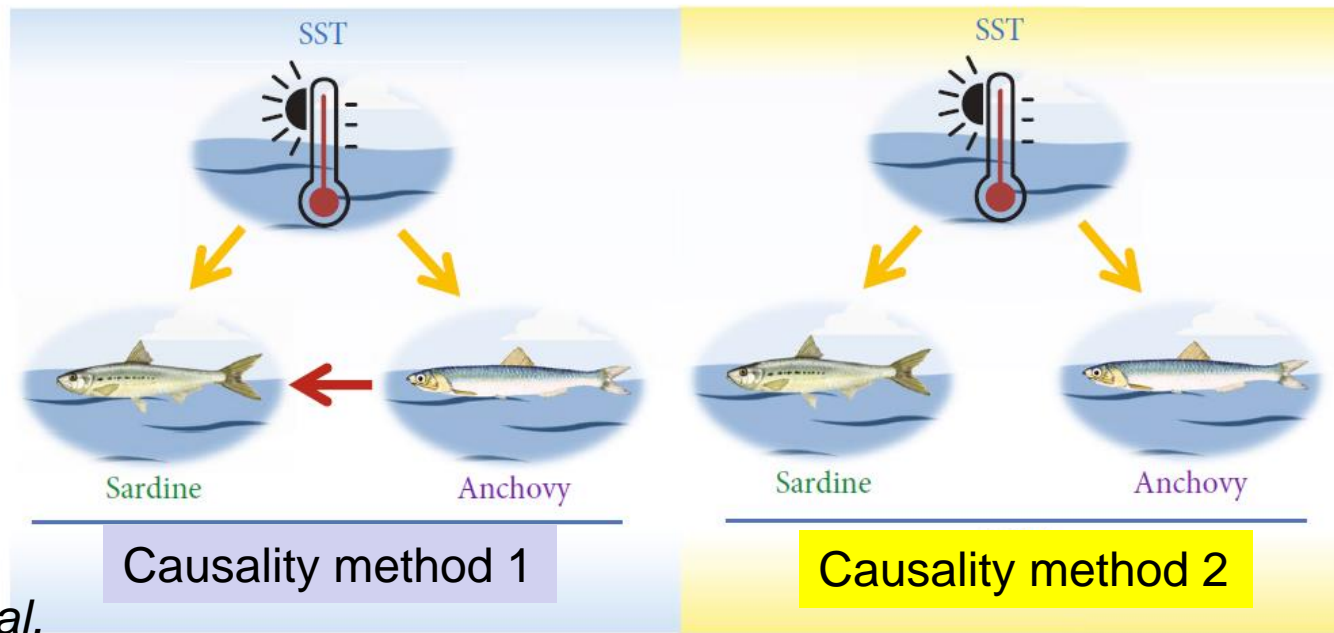
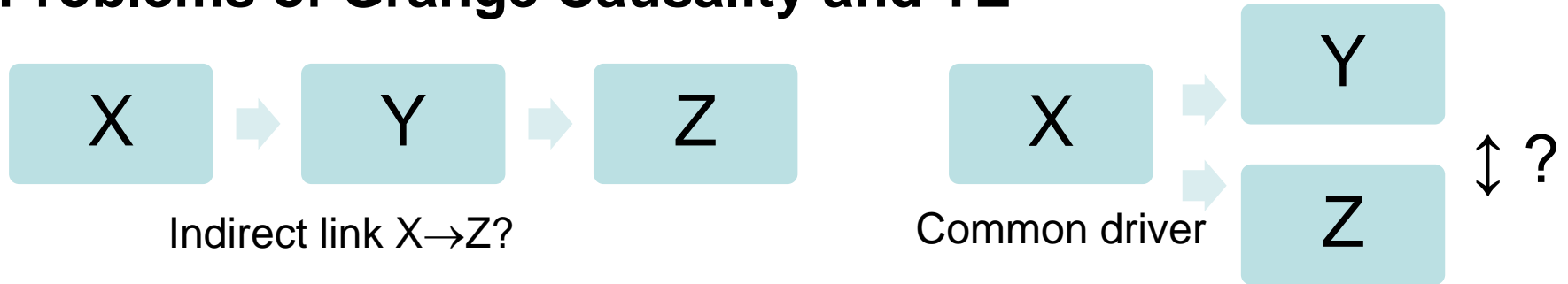
$$TE(x,y) = MI(x, y|x_{\tau})$$

$$TE(y,x) = MI(y, x|y_{\tau})$$

- $MI(x,y) = MI(y,x)$  but  $TE(x,y) \neq TE(y,x)$
- TE and GC are equivalent for Gaussian processes.

*T. Schreiber, Measuring information transfer, Phys. Rev. Lett. 85, 461 (2000).*

# Problems of Grange Causality and TE



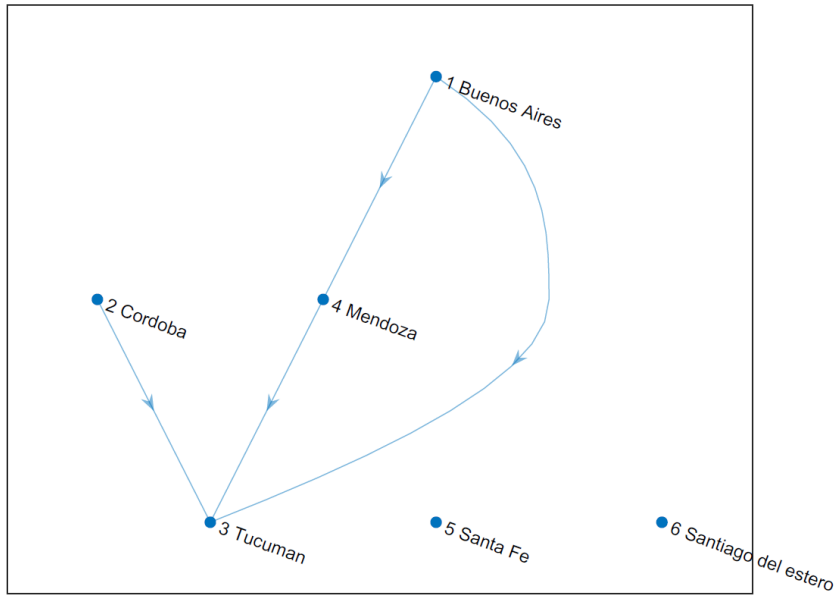
X. Ying et al.  
AAAS Research 2022

Many alternative approaches to try to “solve” these problems.

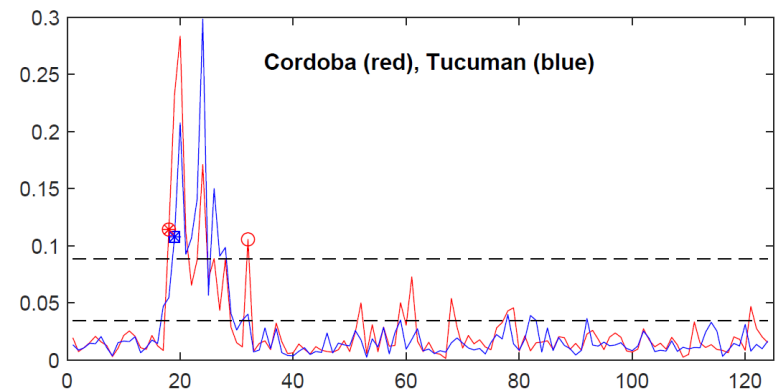
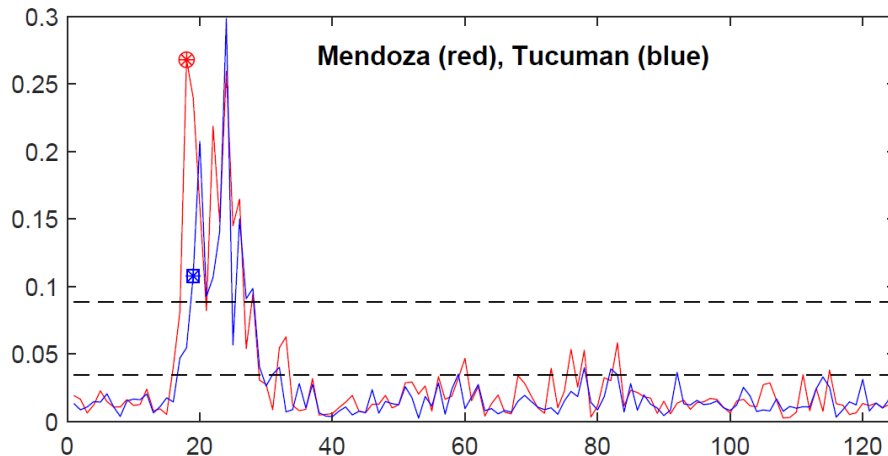
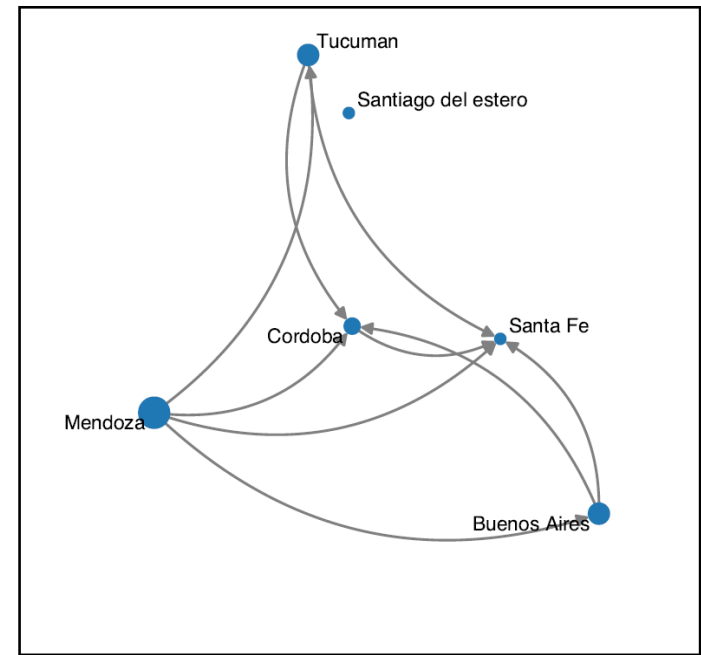


# Results. Example topic “Avion Iraní”

Qs **or** Qa significant

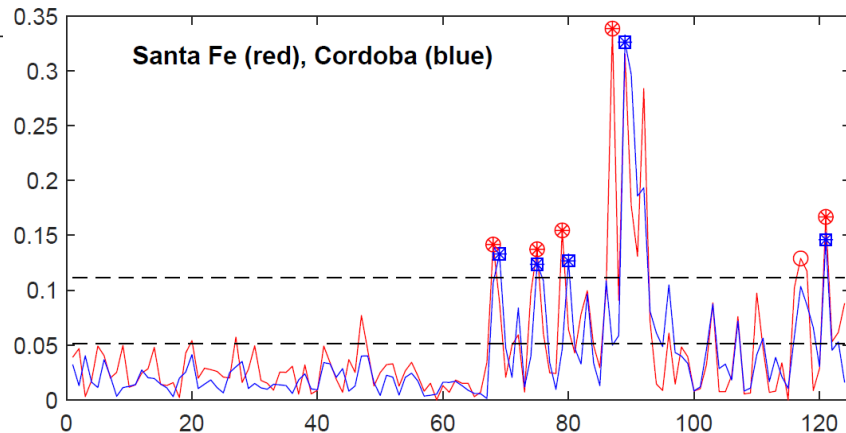
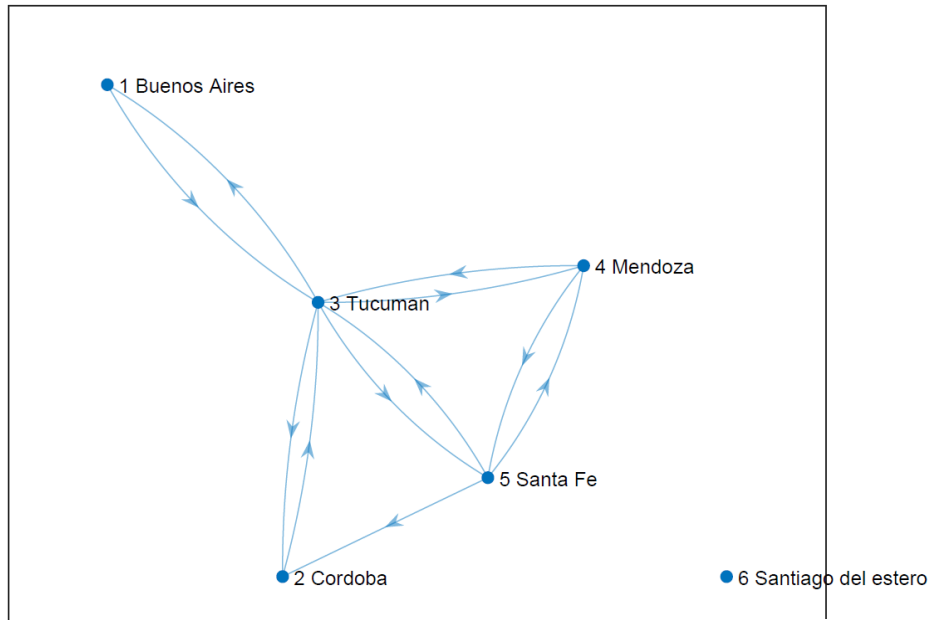


GC **and** TE significant

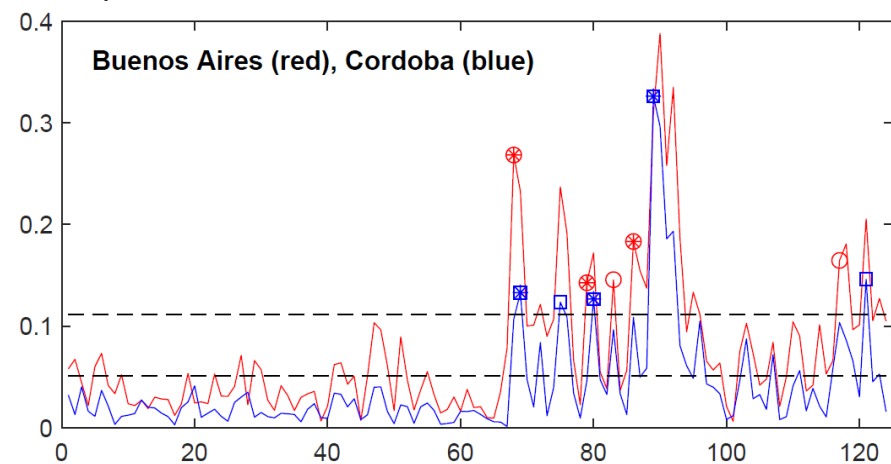
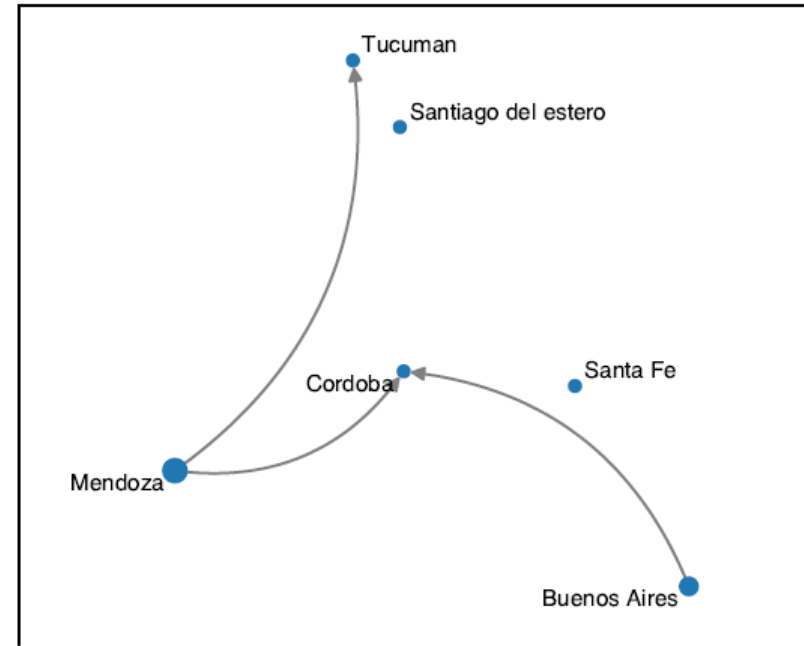


# Results. Example topic “Diego Luciani”

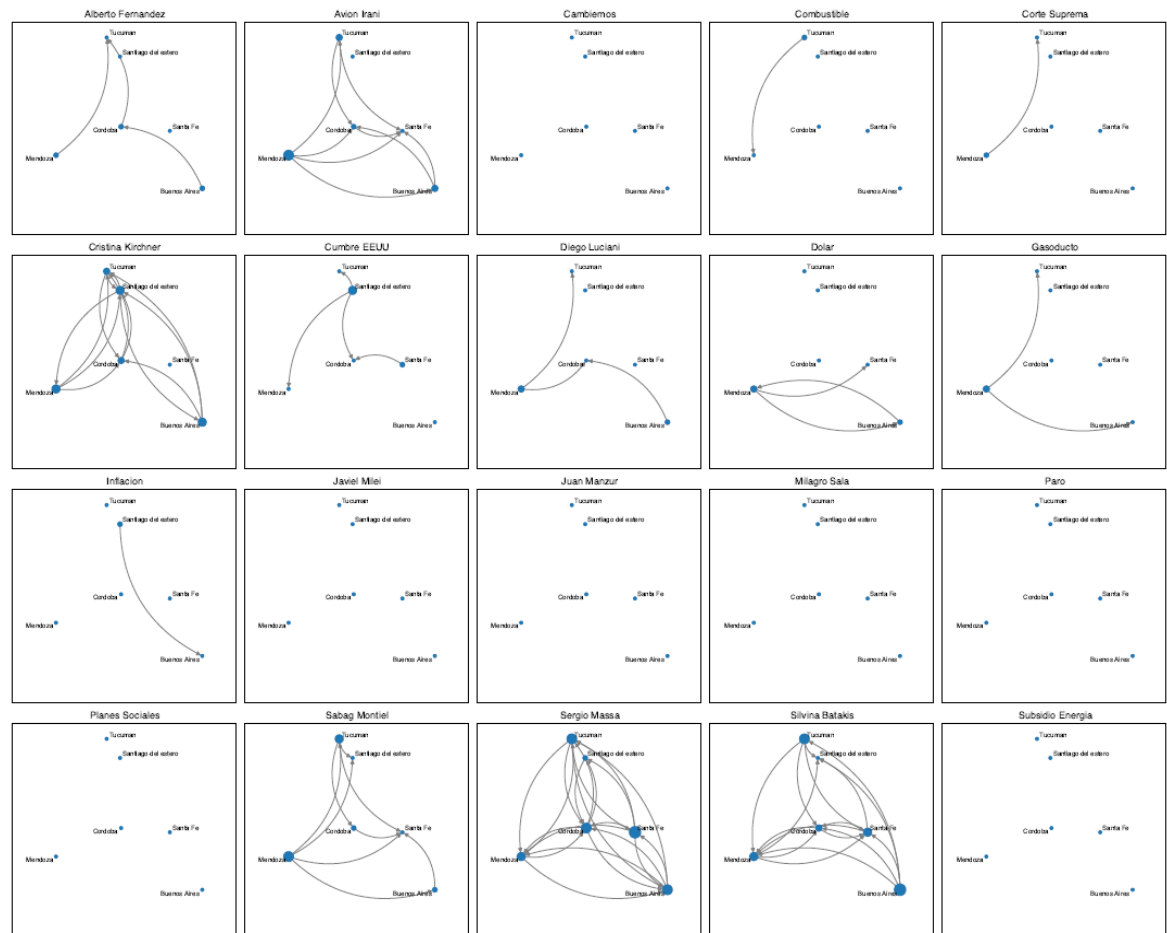
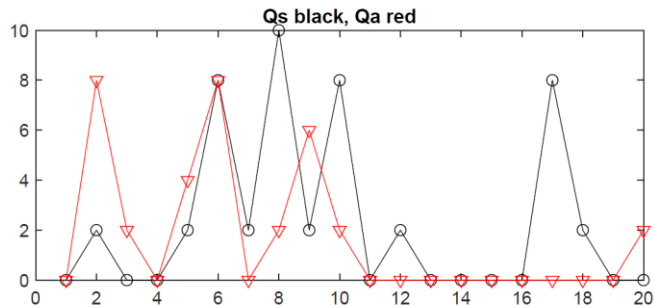
## Qs or Qa significant



## GC and TE significant



# Results



# Preliminary conclusions



- The networks obtained with event synchronization measures strongly depend on the criteria used to define the events and on the thresholds to obtain adjacency matrices.
- There are coincidences and differences with the networks obtained by combining GC and TE.
- It could be interesting to analyze networks obtained by counting only the number of synchronized events, without "penalizing" the occurrence of unsynchronized events.
- Temporal info can be obtained by counting events in time segments.

**Thanks to my collaborators and  
Thank you for your attention!**

