

Extreme optical pulses: origin, predictability and control

Cristina Masoller
Cristina.masoller@upc.edu
www.fisica.edu.uy/~cris



UNIVERSITAT POLITÈCNICA
DE CATALUNYA
BARCELONATECH

Campus d'Excel·lència Internacional

Dynamic Days Europe,
Bayreuth, Germany,
September 2014





- José A. Reinoso Sandro Perrone
- Jordi Zamora Munt Ramon Vilaseca

- B. Garbin, M. Feyereisen, S. Barland, M. Giudici (INLN, Nice, France)

- Jorge Tredicce (Universite de la Nouvelle Caledonie)

- Jose Rios Leite (Universidade Federal de Pernambuco, Recife, Brasil)

What is a rogue wave?

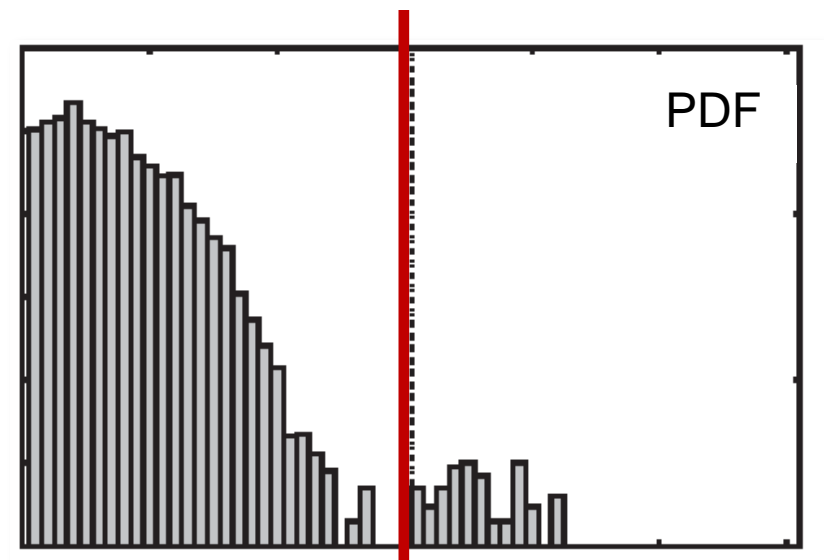
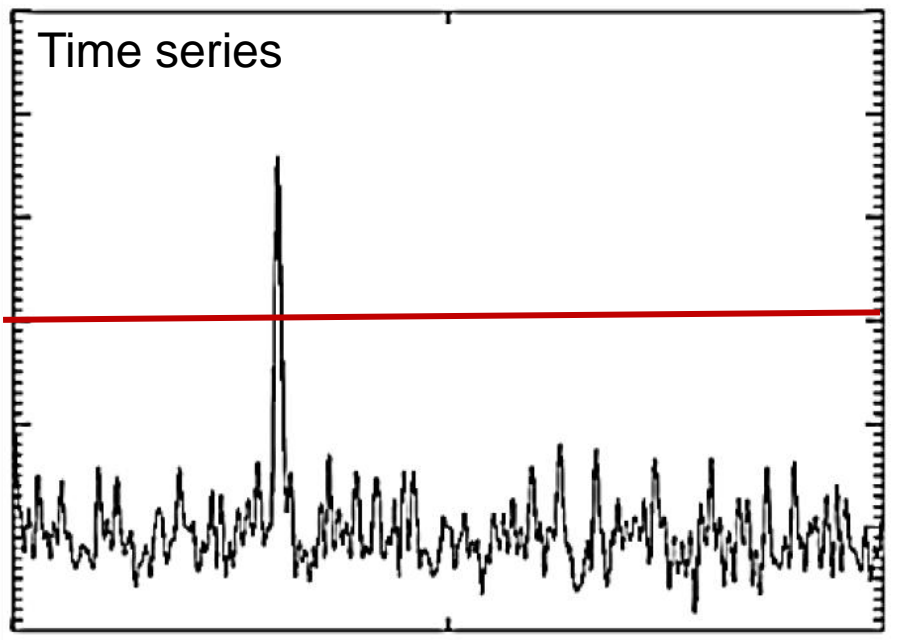
A “monster wave”, ultra-high wave that falls outside (and far from) the main part of a long-tailed probability distribution.



The Great Wave of Kanagawa, Katsushika Hokusai. Source: Wikipedia

Two more precise definitions

- A RW: above **twice** the significant wave height (SWH).
SWH = <highest 1/3 waves> that occur over a certain period of time.
- A RW: above a certain threshold ($\langle H \rangle + 4-8 \sigma$)

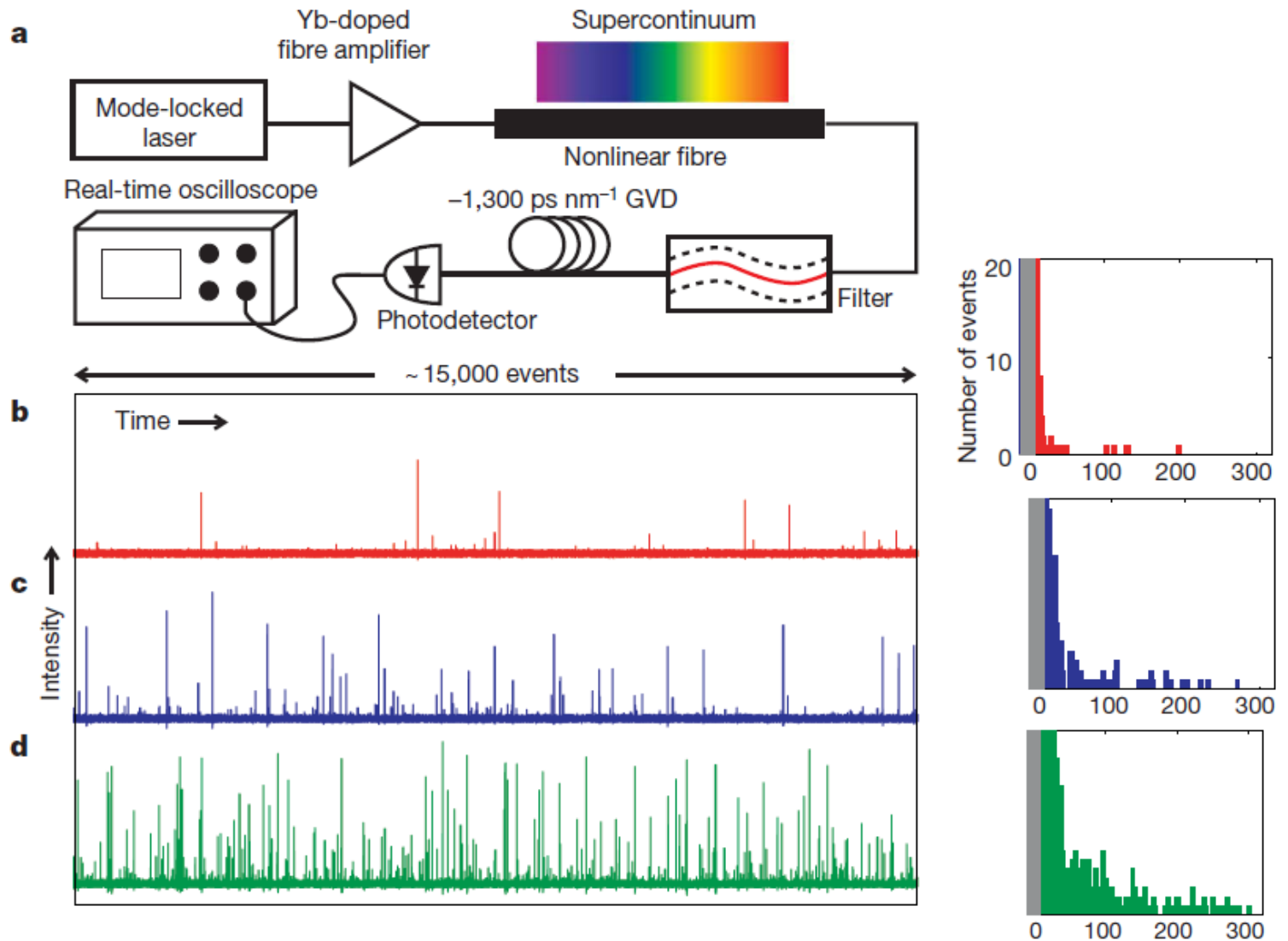


RWs appear suddenly



A challenge for the oil and gas industry, for the design of safe off-shore platforms.

Source: National Geographic



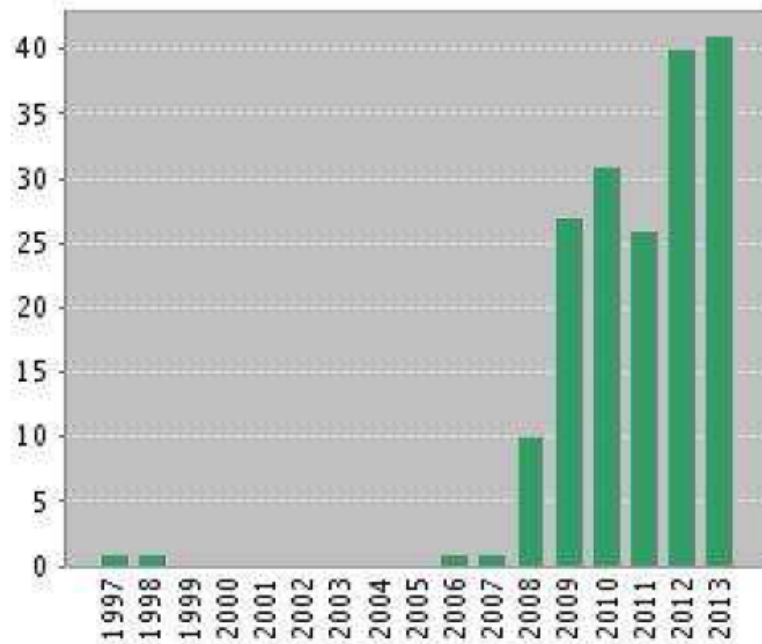
Since 2007: a lot of work

Citation Report Topic=(optical rogue wave)

Timespan=All years. Databases=SCI-EXPANDED, SSCI, A&HCI, CPCI-S, CPCI-SSH.

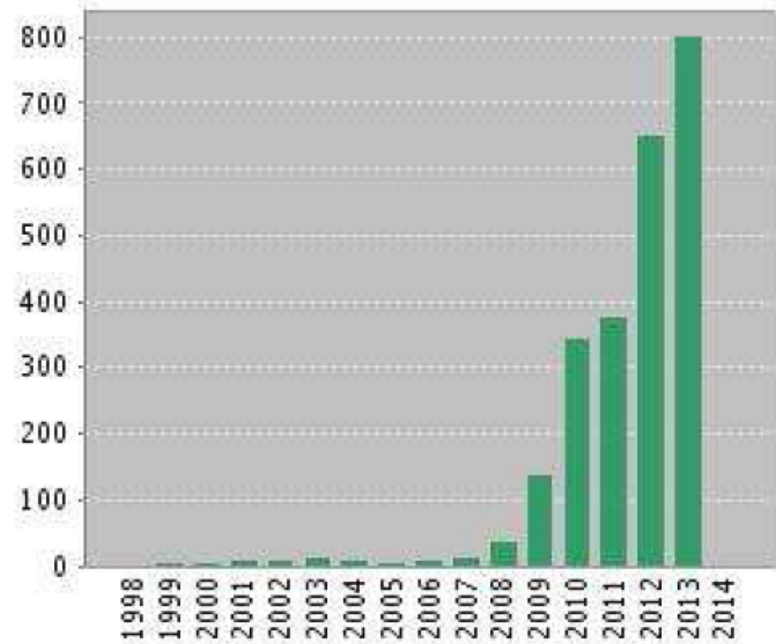
This report reflects citations to source items indexed within Web of Science. Perform a Cited Reference Search to include cita indexed within Web of Science.

Published Items in Each Year



The latest 20 years are displayed.

Citations in Each Year

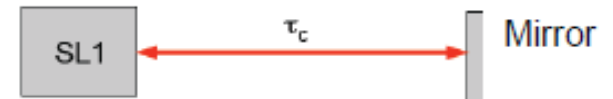
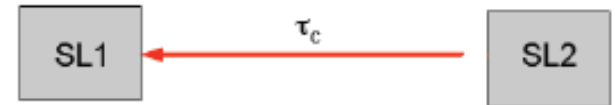


The latest 20 years are displayed.

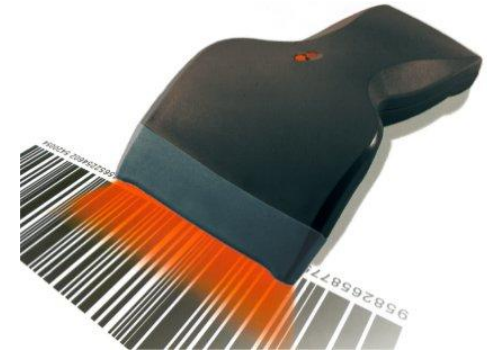
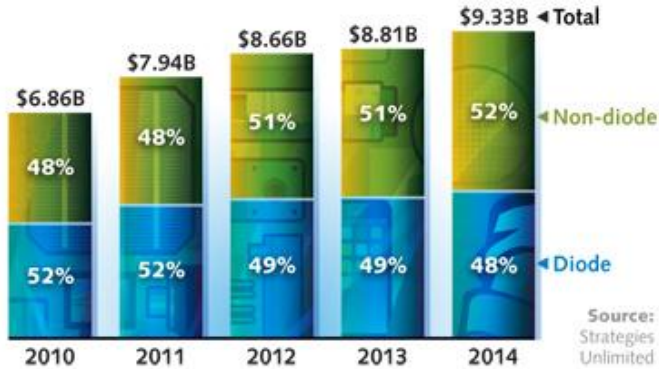
Optical RWs in semiconductor lasers

Two setups:

- With **optical injection**:
observations & numerical results.
- With **optical feedback**:
numerical results.



Why semiconductor lasers? (diode lasers)



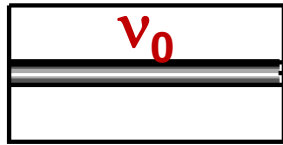
- Used in:
 - Telecommunications
 - Optical data storage (CDs, DVDs, Blu rays)
 - Barcode scanners, printers, mouse
 - Biomedical applications (imaging, sensing, etc)

Semiconductor lasers provide an inexpensive and controllable setup for the study of optical rogue waves

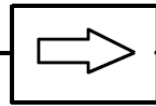
- RWs can be **deterministic**, generated by a crisis-like process.
 - RWs can be **predicted** with a certain anticipation time.
 - RWs can be **controlled** via noise and/or modulation.
- C. Bonatto et al, *Deterministic optical rogue waves*, PRL 107, 053901 (2011).
 - J. Zamora-Munt et al, *Rogue waves in optically injected lasers: origin, predictability and suppression*, PRA 87, 035802 (2013).
 - J. M. Reinoso et al, PRE 87, 062913 (2013).
 - S. Perrone et al, PRA 89, 033804 (2014).

First setup: an optically injected laser

Master Laser

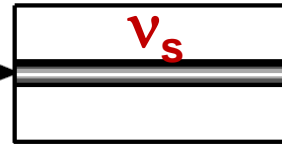


Tunable SCL



Isolator

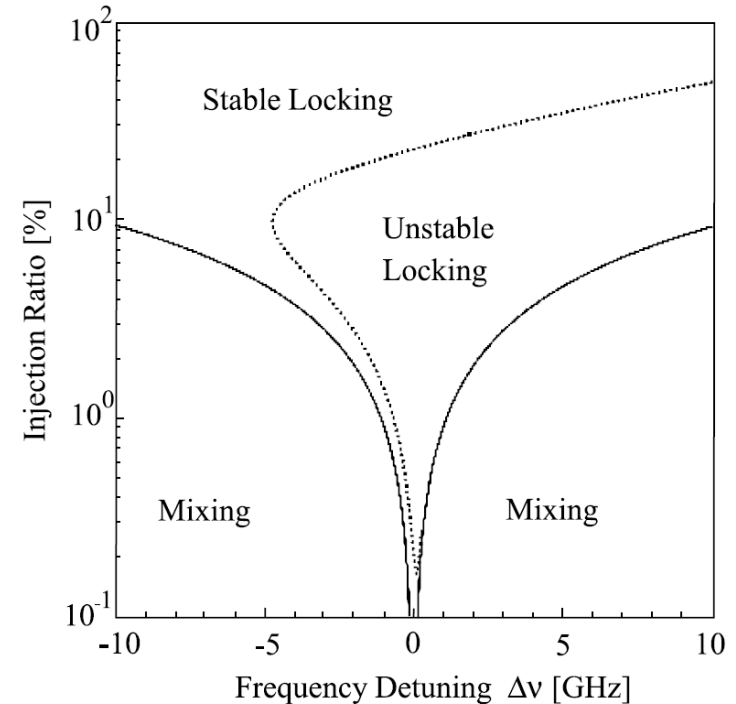
Slave Laser



VCSEL 980 nm

Detection system
(photo detector,
oscilloscope,
spectrum
analyzer)

- Parameters:
 - Injection ratio
 - Frequency detuning $\Delta\nu = \nu_s - \nu_0$
- Dynamical regimes:
 - Injection locking (cw output)
 - Period-one oscillation
 - Period-two oscillation
 - Chaos



Labyrinth bifurcations in optically injected diode lasers

V. Kovanis¹, A. Gavrielides², and J.A.C. Gallas^{3,4,5,a}

¹ Air Force Research Laboratory, 2241 Avionics Circle, Wright-Patterson AFB, Dayton OH 45433, USA

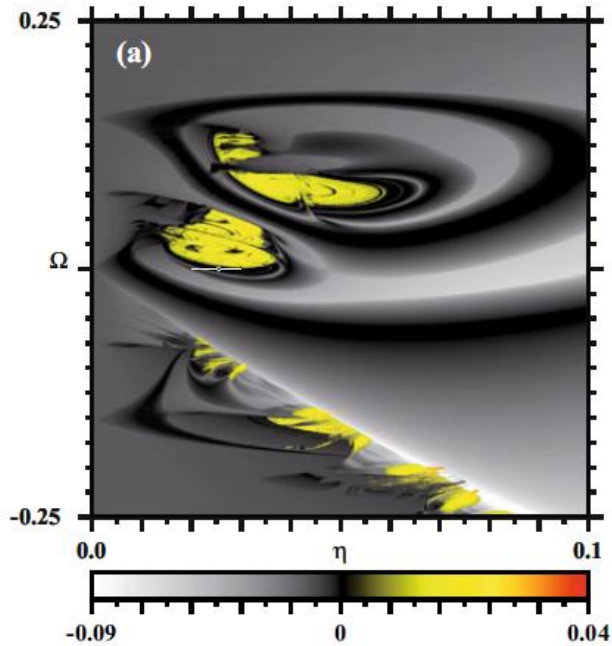
² USAF, Research Laboratory, High Power Solid State Lasers Branch, Kirtland AFB, NM 87117, USA

³ TecEdge, Wright Brothers Institute, 5100 Springfield Street, Dayton OH 45431, USA

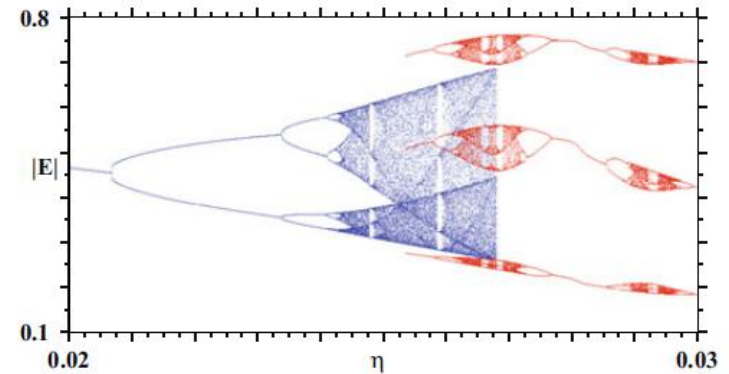
⁴ Departamento de Física, Universidade Federal da Paraíba, 58051-970 João Pessoa, Brazil

⁵ Instituto de Física, Universidade Federal do Rio Grande do Sul, 91501-970 Porto Alegre, Brazil

Lyapunov diagram



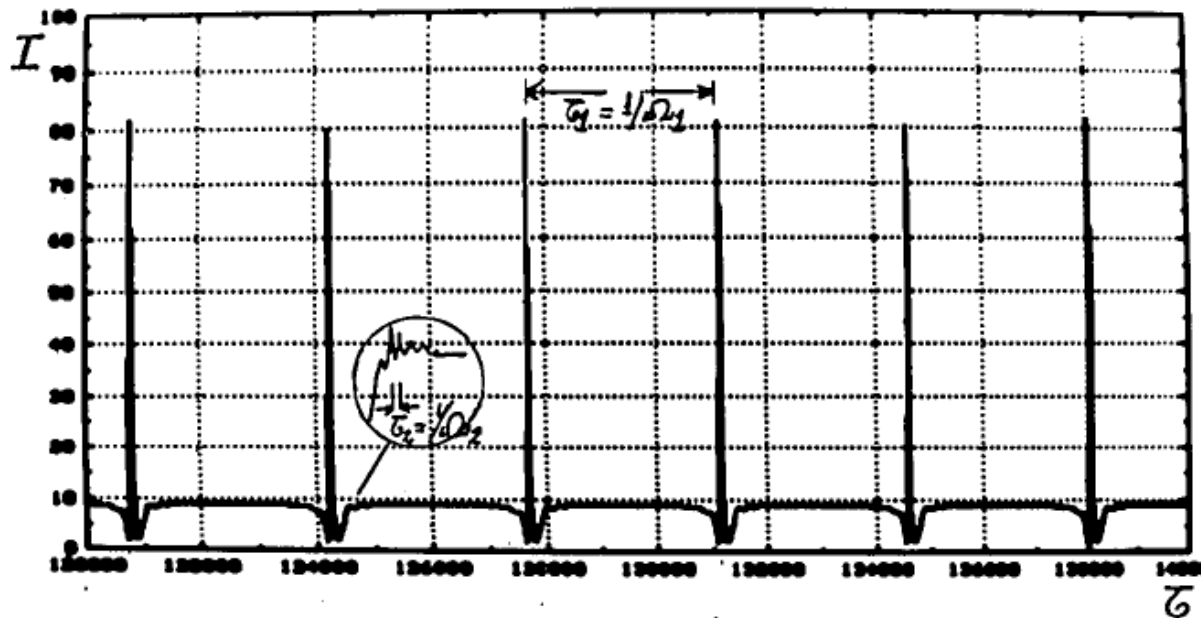
Bifurcation diagram



Instabilities in lasers with an injected signal

J. R. Tredicce, F. T. Arecchi, G. L. Lippi, and G. P. Puccioni

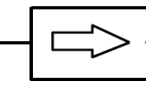
178 J. Opt. Soc. Am. B/Vol. 2, No. 1/January 1985



Master Laser



ν_0
(fixed)



Isolator

Slave Laser



ν_s
(variable)

- Photo detector: 9.5GHz
- Oscilloscope: 6 GHz, 20GS/s
- Spectrum analyzer: 72GHz

The **frequency detuning** between the lasers, $\Delta\nu = \nu_s - \nu_0$, is controlled by the slave laser pump current, I

When I increases:

- **Joule heating**
- **the temperature modifies the cavity refractive index**
- **decreases the cavity resonance frequency**

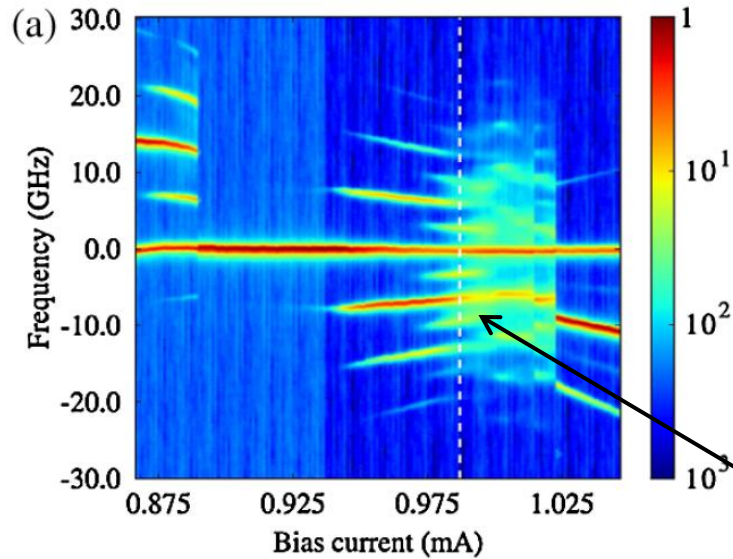
$$\nu_s = g(\text{Temp}) = f(I)$$

(f approximately linear)

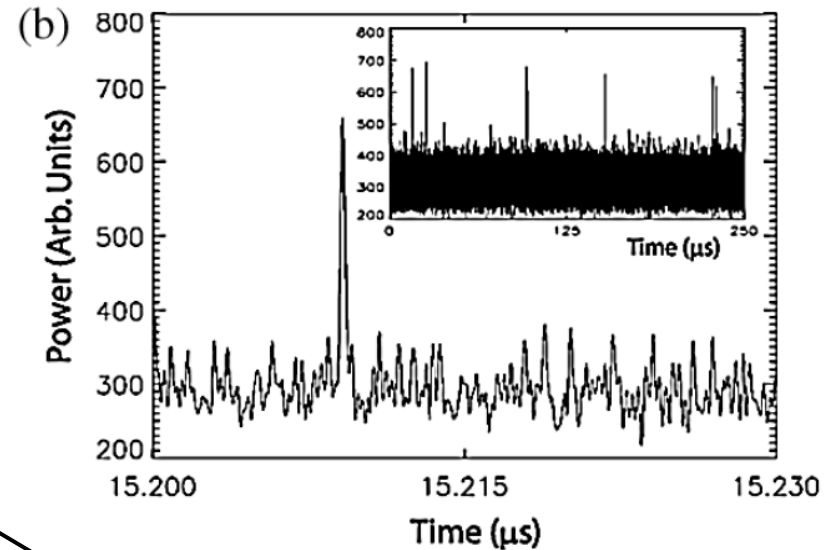
Observed laser output:

- **Intensity time - series (oscilloscope)**
- **Intensity Fourier spectrum (spectrum analyzer)**

Fourier spectrum of the laser intensity



Time series of the laser intensity

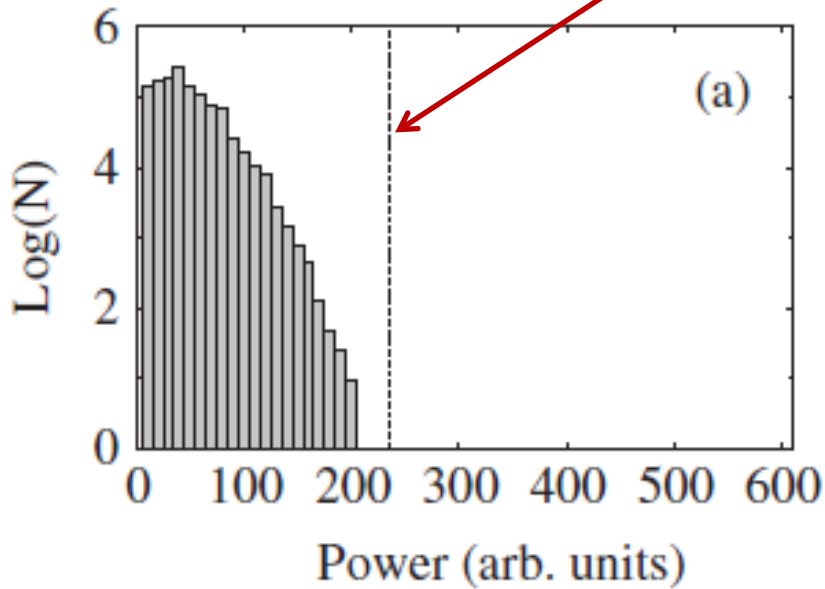


Five regions:

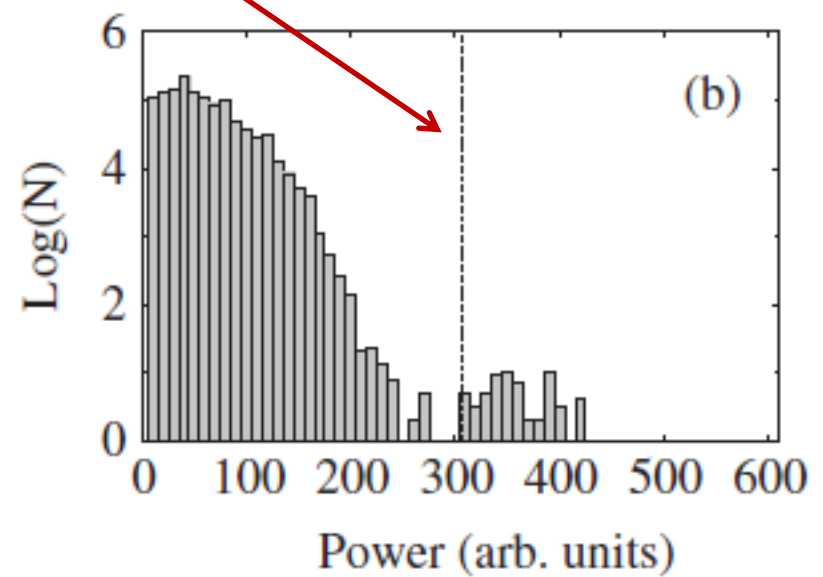
- Beating (independent lasers)
- Locking
- Period 2 of the beat note
- Chaos
- Beating (independent lasers again)

(In the chaotic region,
 $I = 0.976 \text{ mA}$, $\Delta\nu = -1.34 \text{ GHz}$)

RW threshold = mean value + 8 σ



$I = 0.972 \text{ mA}$



$I = 0.976 \text{ mA}$

Governing equations

- Complex field, \mathbf{E} (photon number $\propto |\mathbf{E}|^2$)
- Carrier density, \mathbf{N}

$$\frac{dE}{dt} = \frac{1}{2\tau_p} (1 + i\alpha)(N - 1)E + \underbrace{i\Delta\omega + \sqrt{P_{inj}}}_{\text{optical injection}} + \underbrace{\sqrt{2\beta_{sp} / \tau_N} \xi(t)}_{\text{spontaneous emission noise}}$$

$$\frac{dN}{dt} = \frac{1}{\tau_N} (\mu - N - N|E|^2)$$

optical injection
 η : injection strength
 $\Delta\omega$: frequency detuning

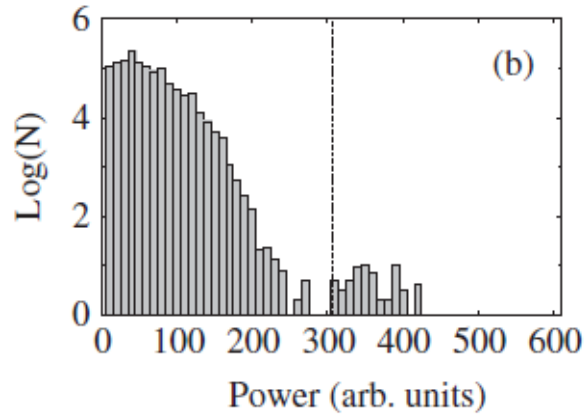
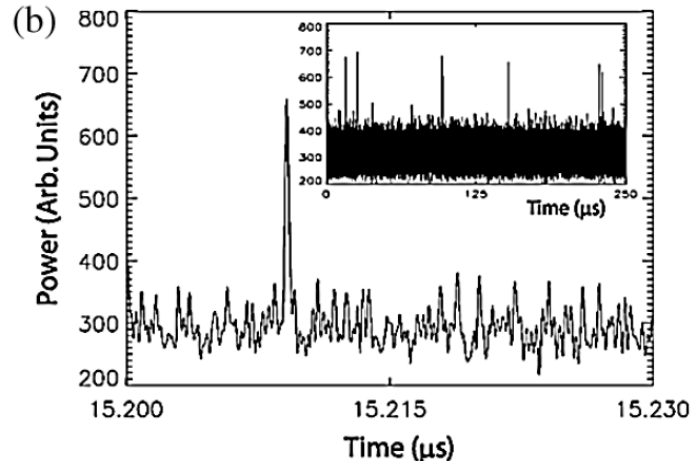
spontaneous
 emission
 noise

Solitary laser
 parameters: α τ_p τ_N μ

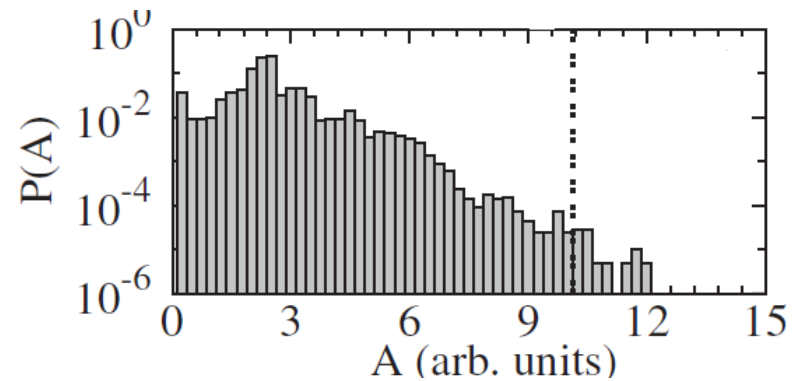
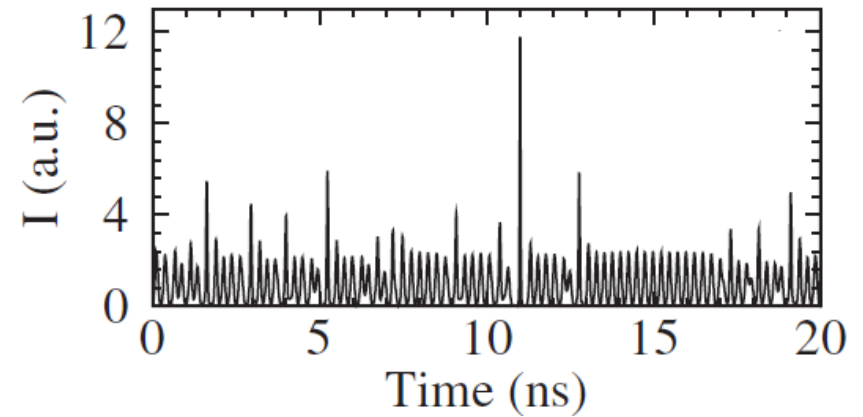
Typical parameter values:
 $\alpha = 3, \tau_p = 1 \text{ ps}, \tau_N = 1 \text{ ns}$

μ : normalized pump current parameter

Experiments



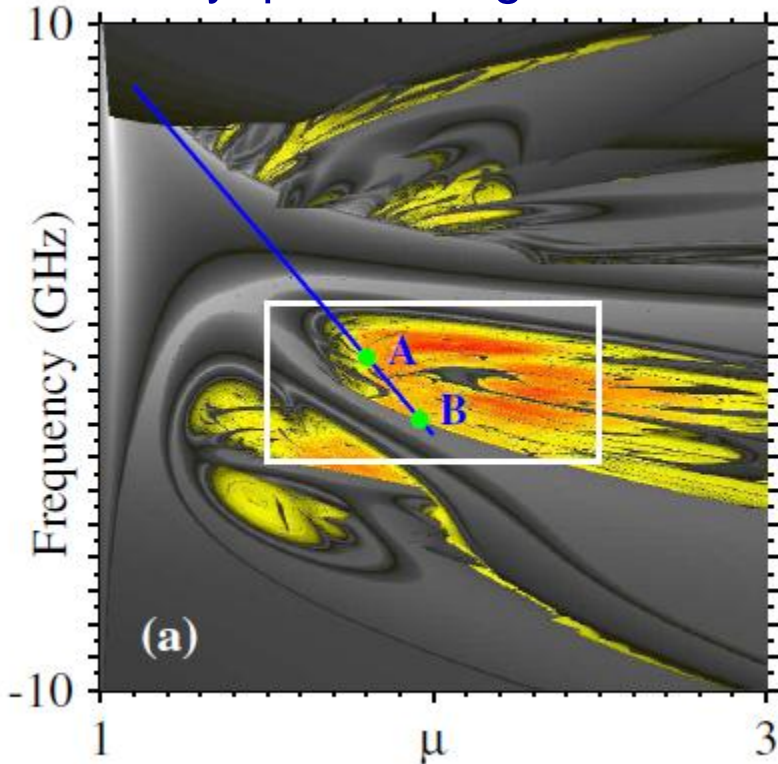
Simulations



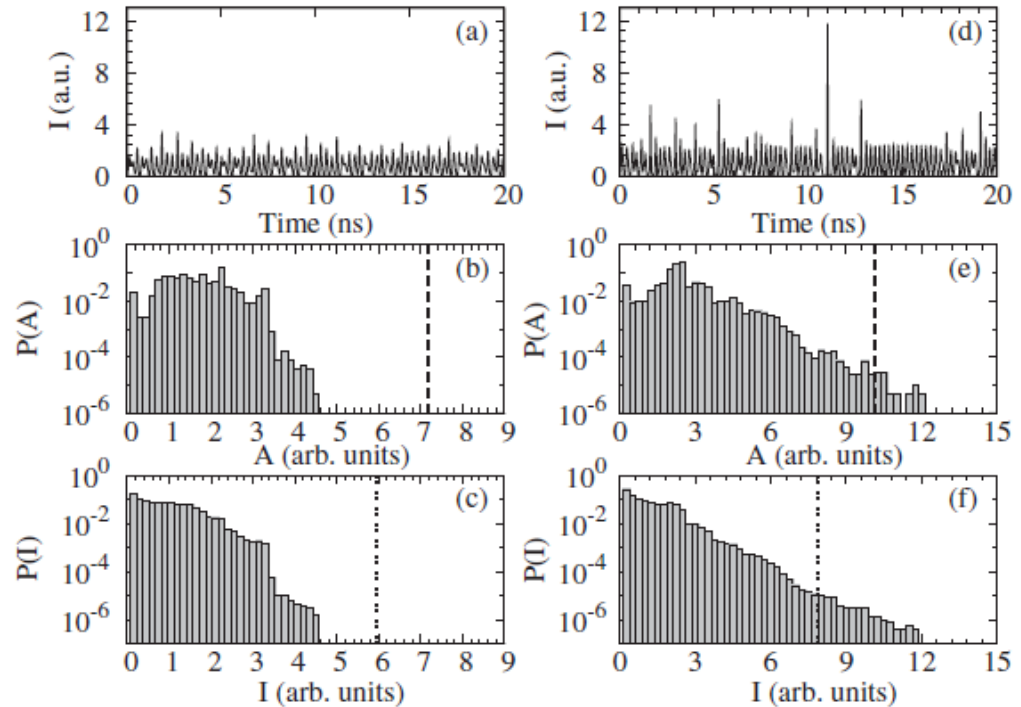
Deterministic simulations

$$(\beta_{sp}=0)$$

Lyapunov diagram



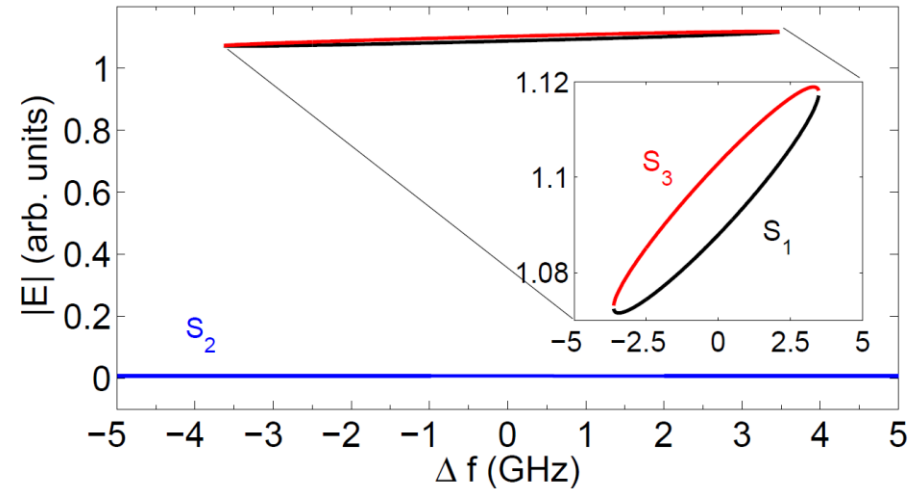
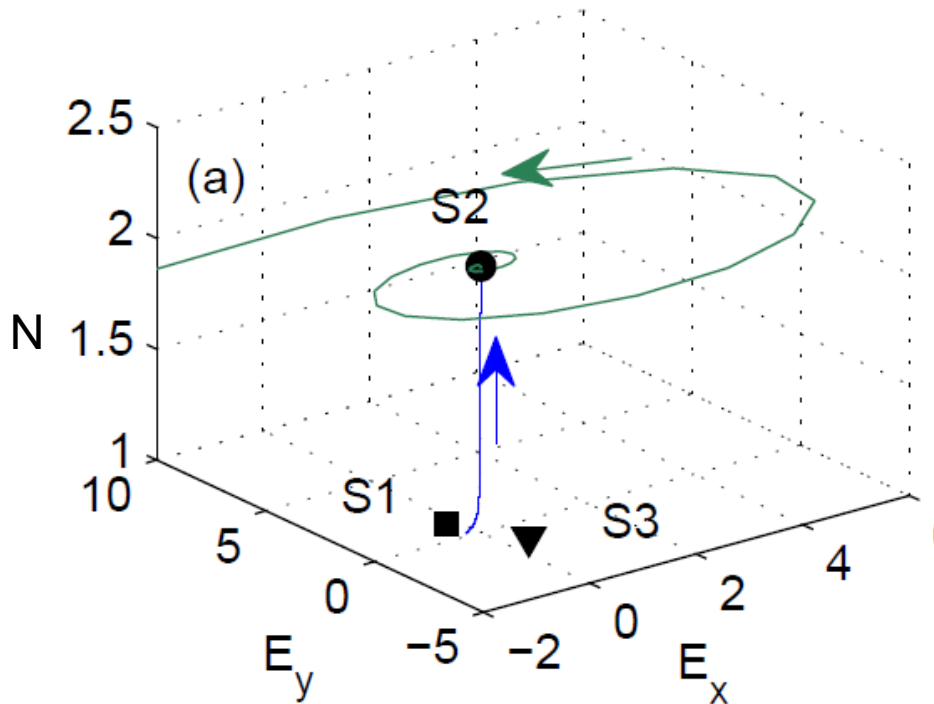
Pump current parameter



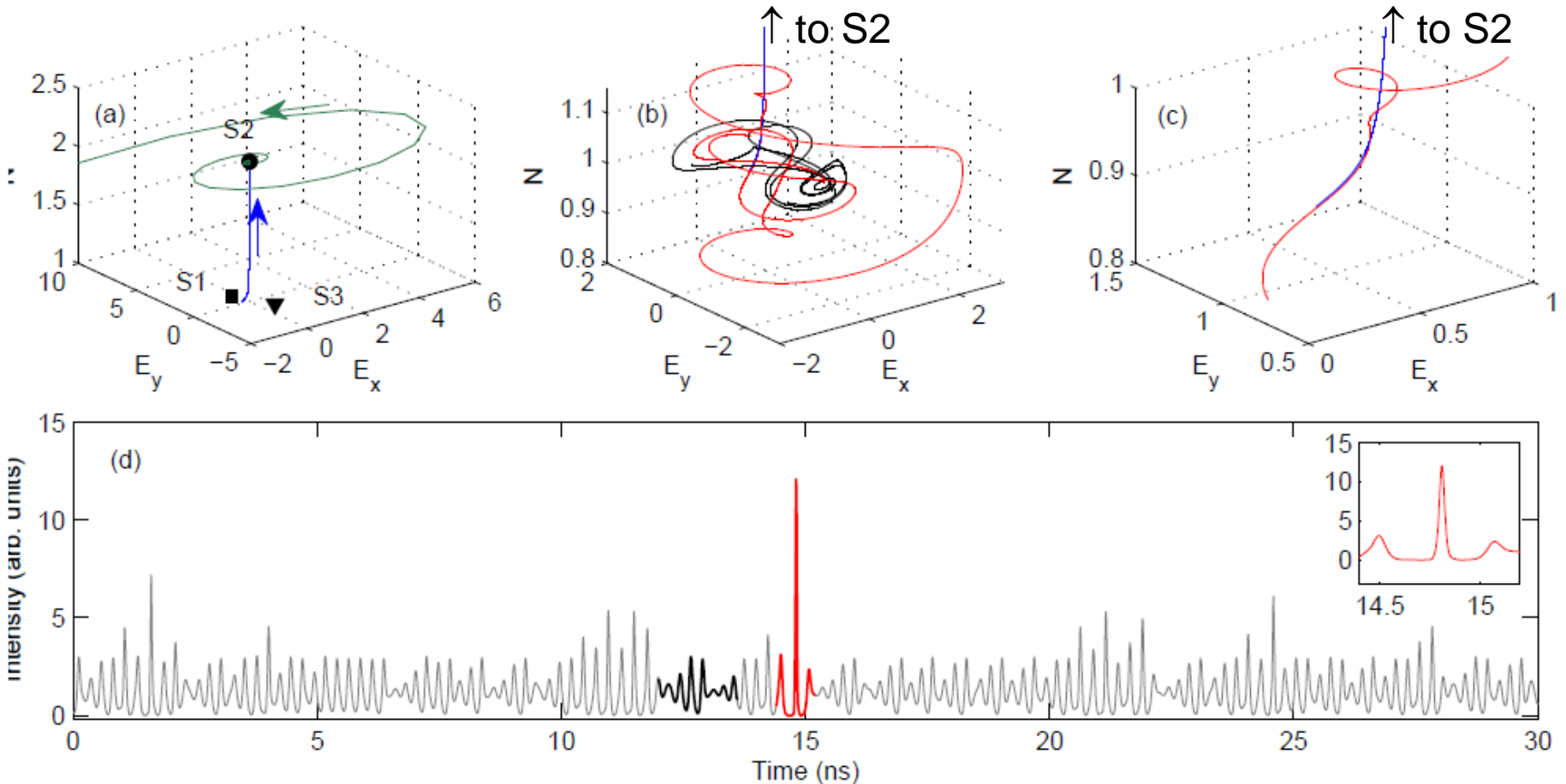
Point A: No RWs

Point B: RWs

Three fixed points in the phase space

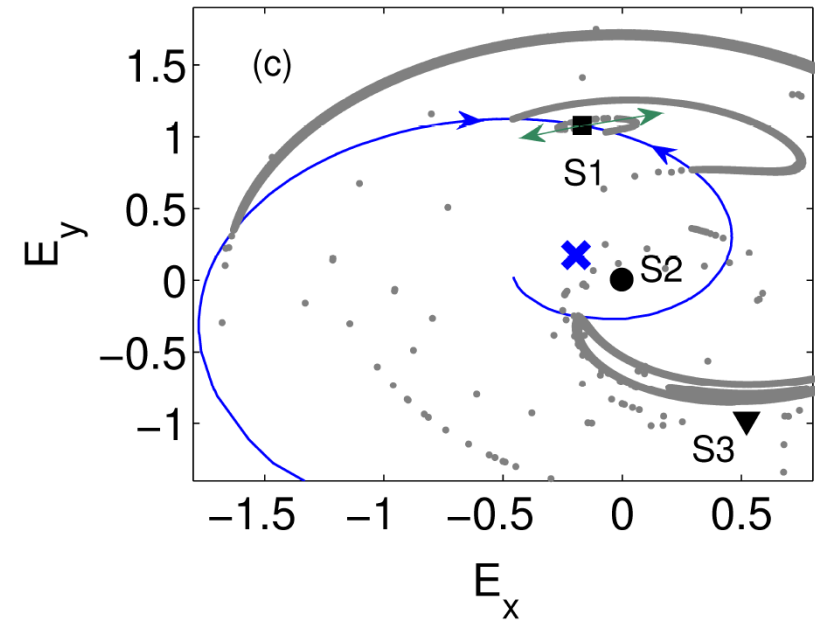
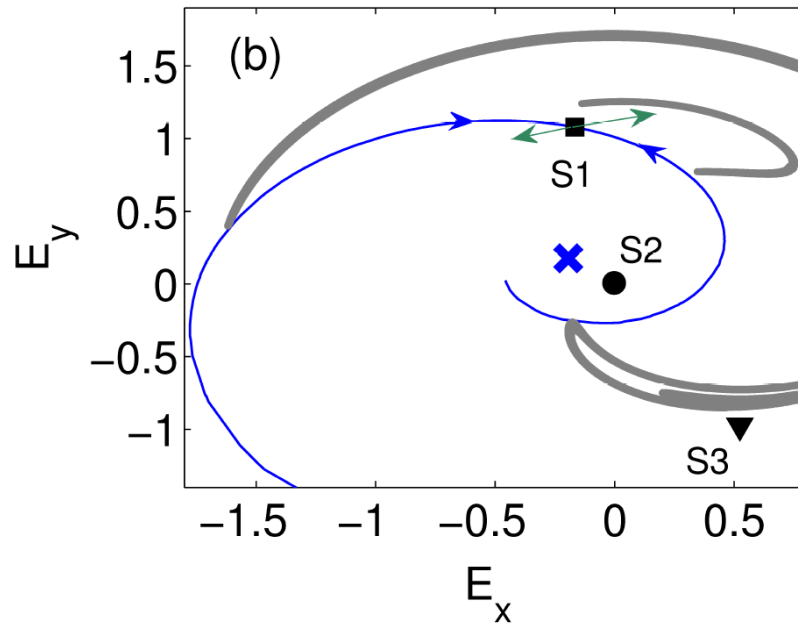


A narrow channel: the RW "door"



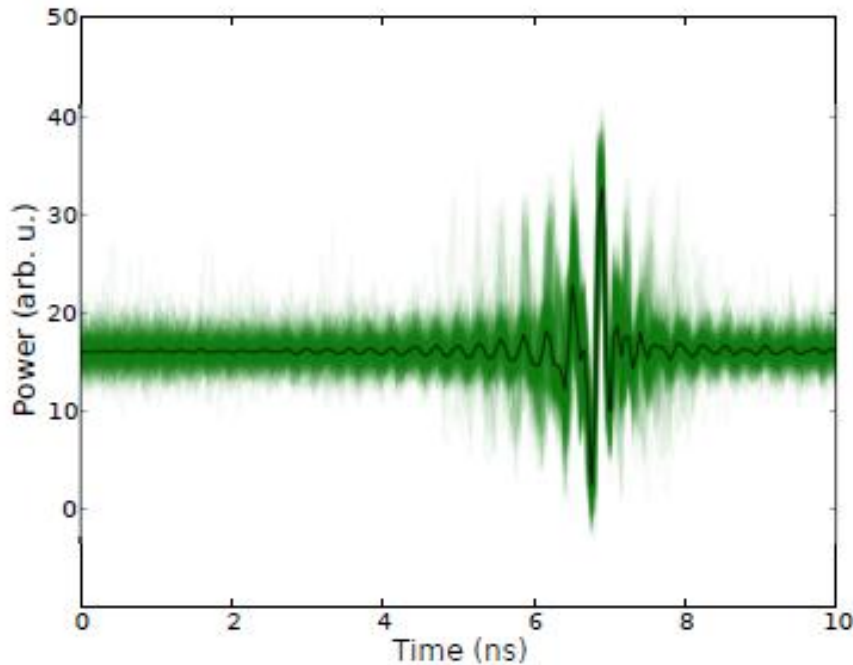
A **RW** is triggered whenever the trajectory closely approaches **the stable manifold of S2**

Why chaos with RWs and chaos without them?

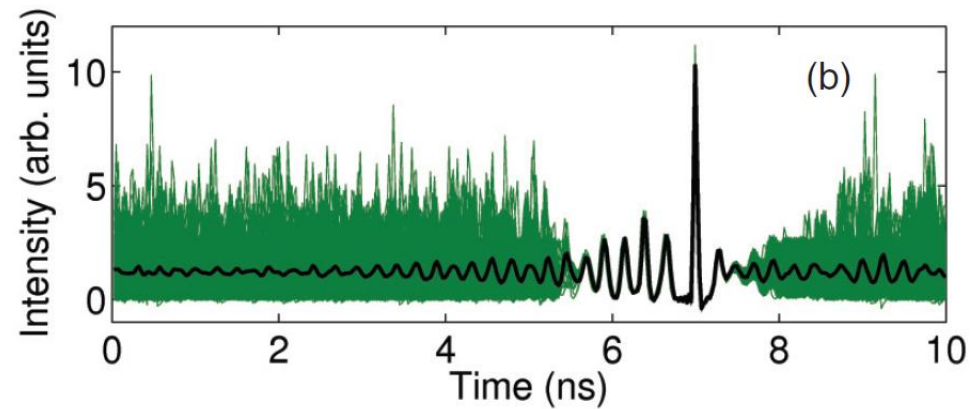


An **external crises-like** process enables access to the region of phase space where the **stable manifold of S2 (x)** is.

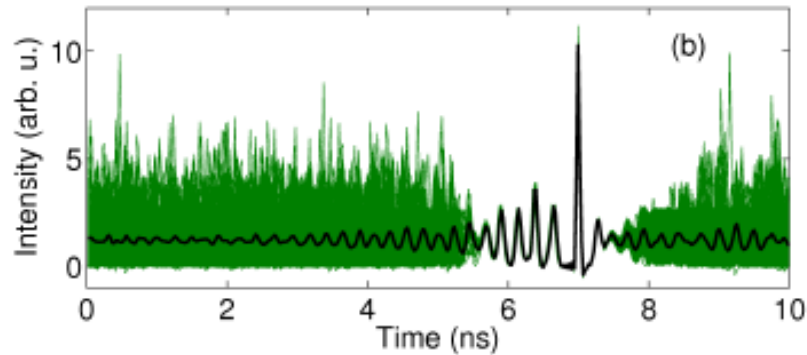
Experiments



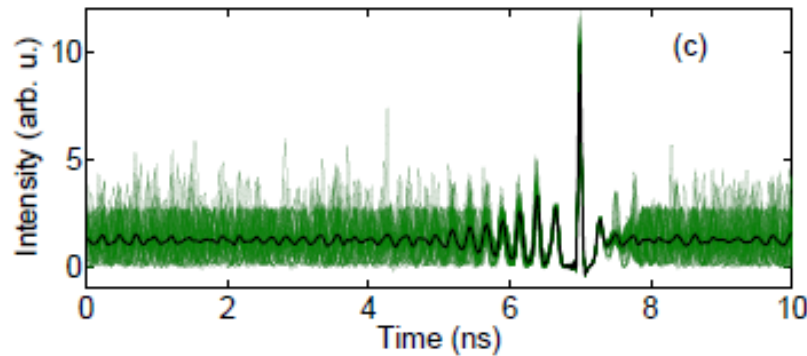
Simulations



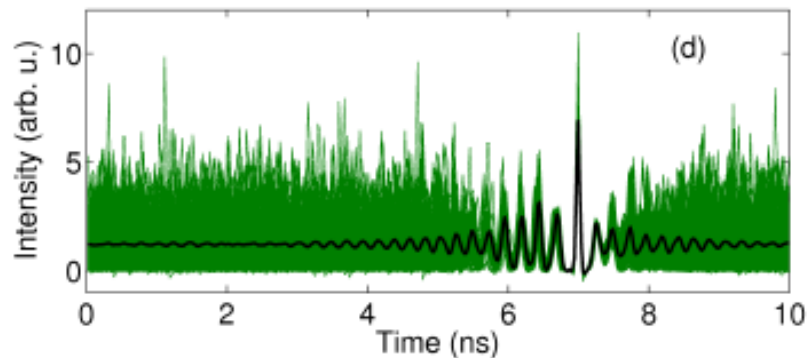
Superposition of 500 time series at the RW peak



$\langle H \rangle + 8\sigma$
 $\beta_{sp} = 0$
459 RWs



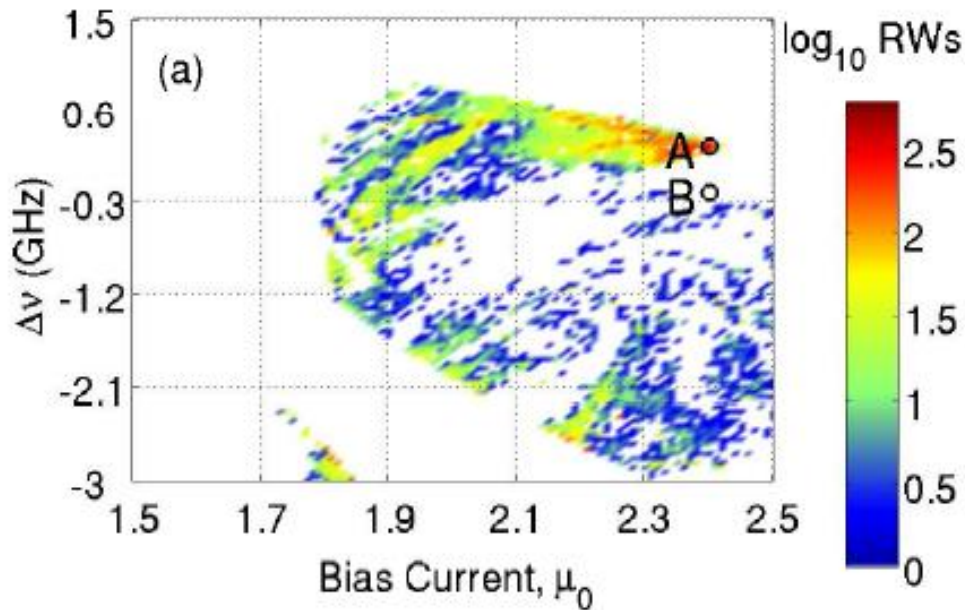
$\langle H \rangle + 8\sigma$
 $\beta_{sp} = 10^{-2}$
53 RWs



$\langle H \rangle + 4\sigma$

Number of RW in the parameter space (pump current, detuning)

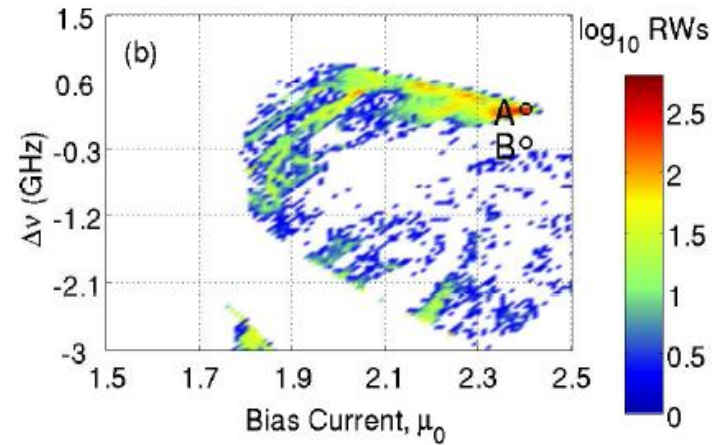
Deterministic RWs ($\beta_{sp}=0$)



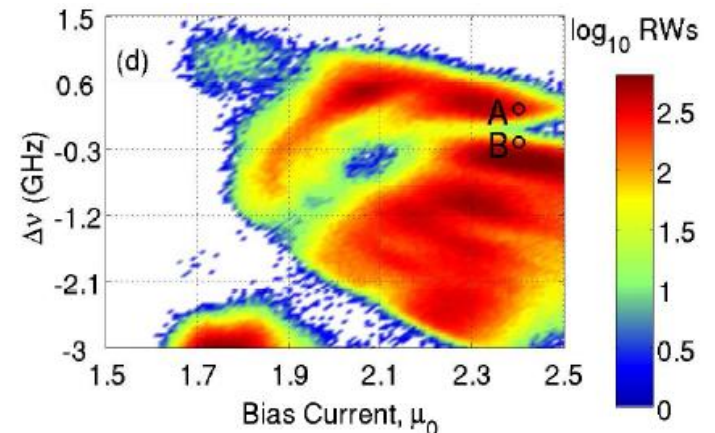
White = No RWs

Weak noise reduces the number of RWs, but strong noise increases the number of RWs

Weak noise ($\beta_{cn}=0.0001$)



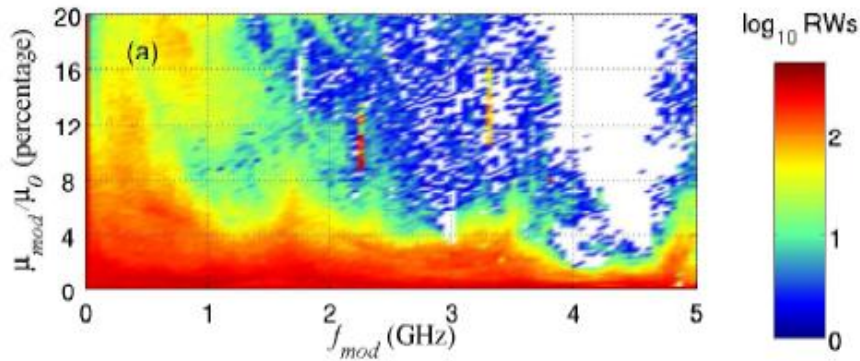
Stronger noise ($\beta_{sp}=0.01$)



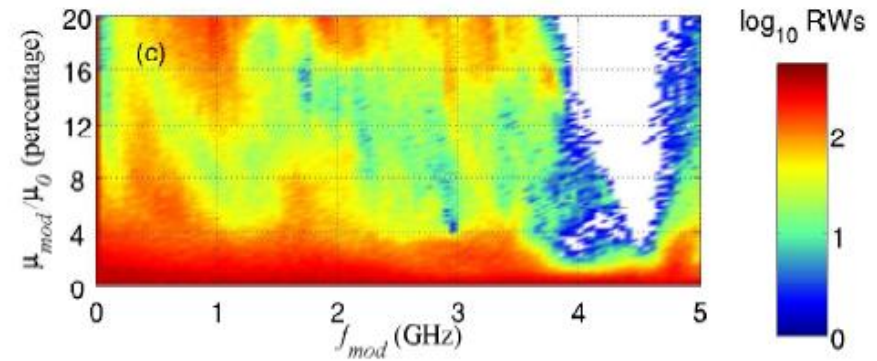
RW control in Point A (deterministic RWs)

$$\mu = \mu_0 + \mu_{\text{mod}} \sin(2\pi f_{\text{mod}} t)$$

$\beta_{\text{sp}}=0$



$\beta_{\text{sp}}=0.01$

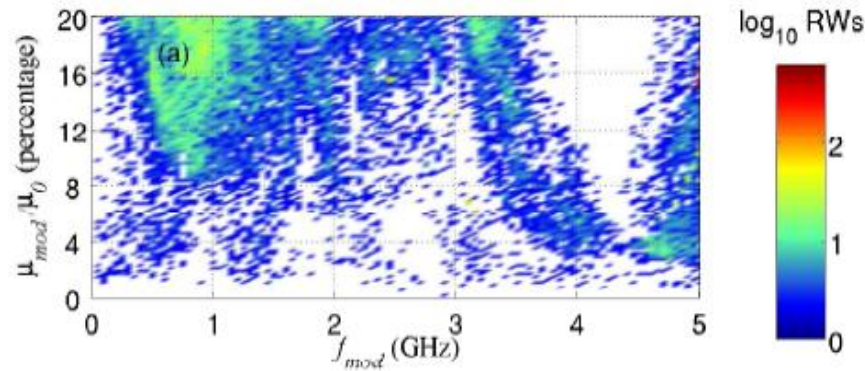


White = No RWs

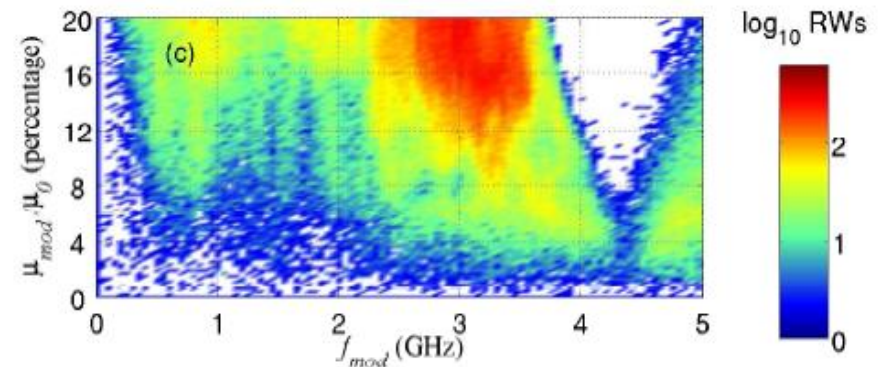
Current modulation with appropriated amplitude and frequency can completely suppress the RWs.

Controlling noise-induced RWs in point B (no deterministic RWs)

$\beta_{sp}=0$



$\beta_{sp}=0.01$



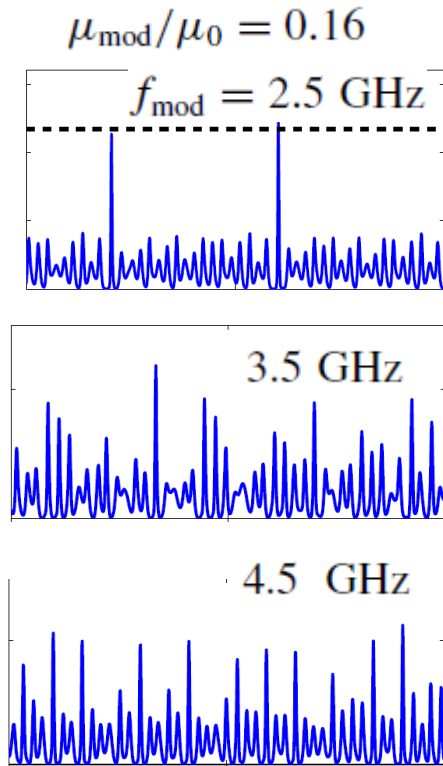
White = No RWs

Current modulation provides a “**safe**” parameter region (amplitude, frequency) where no RWs occur.

Histograms of pulse amplitudes

Point A

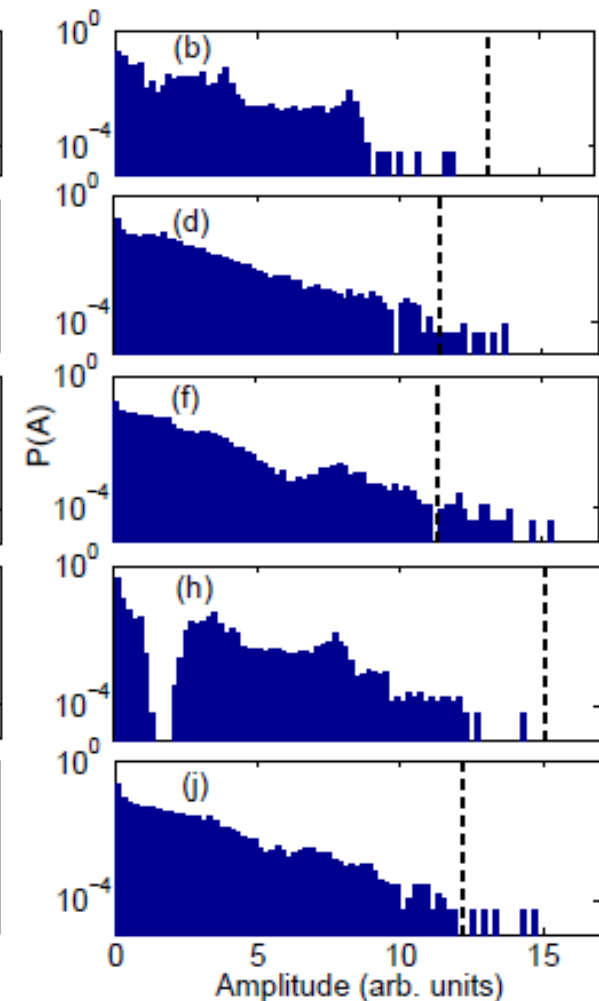
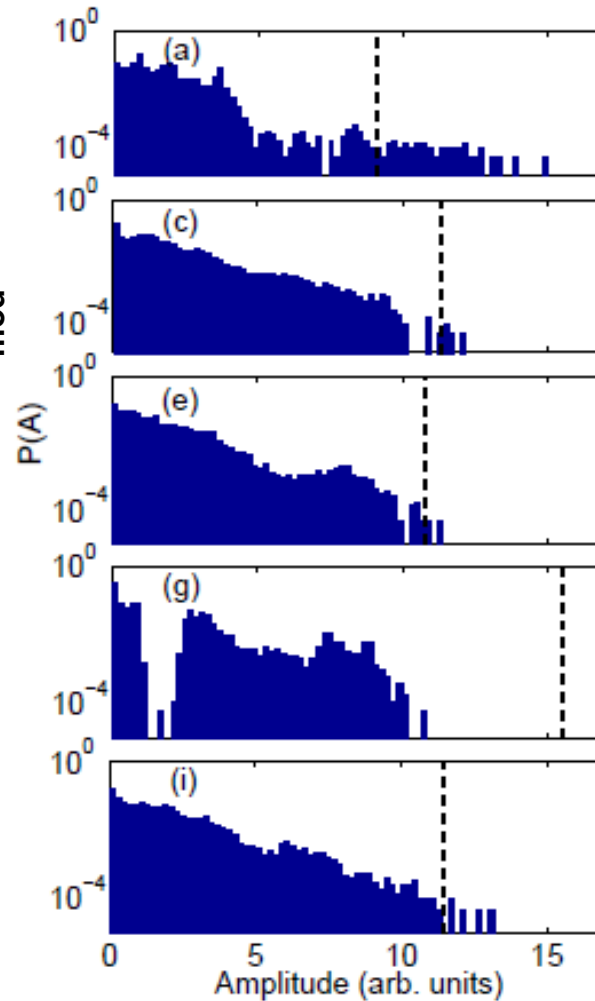
Point B



Increasing

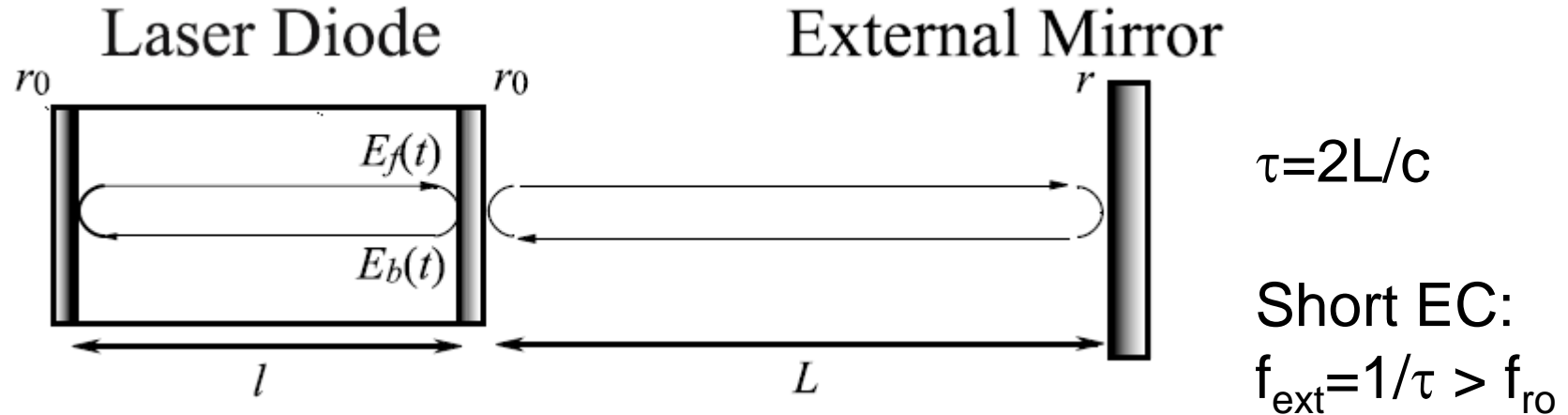


f_{mod}



RWs are suppressed because high (but not ultra high) pulses are frequent

Second setup: a laser diode with optical feedback



$$dE/ds = (1 + i\alpha)NE(s) + \eta e^{-i\omega\theta} E(s - \theta) + \beta\xi,$$

$$TdN/ds = J - N - (1 + 2N)|E(s)|^2.$$

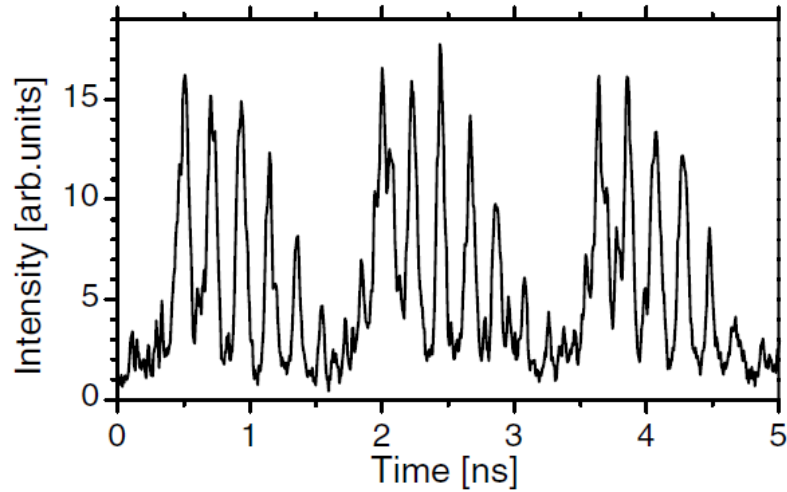
Typical parameter values:
 $\alpha = 5, T = 1710, \theta = 70, J = 1.155$

$$s = t/\tau_p \quad \theta = \tau/\tau_p$$

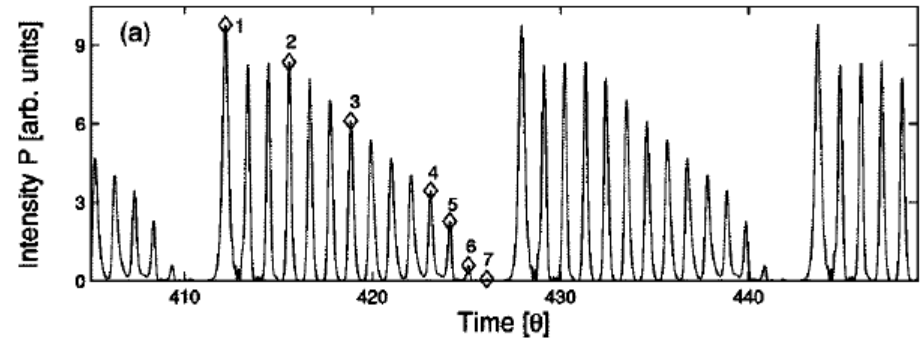
$$T_{RO} = \pi\sqrt{2T/J} = 171$$

Dynamics: Regular Pulse Packages (RPPs)

■ Experiments



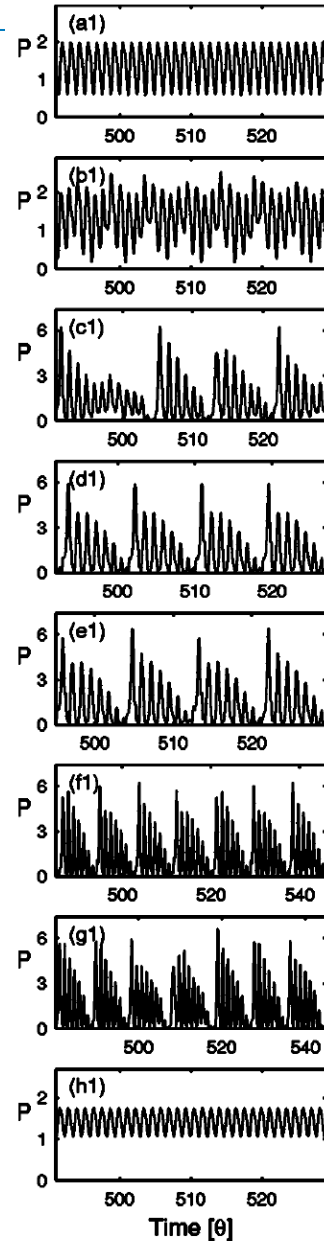
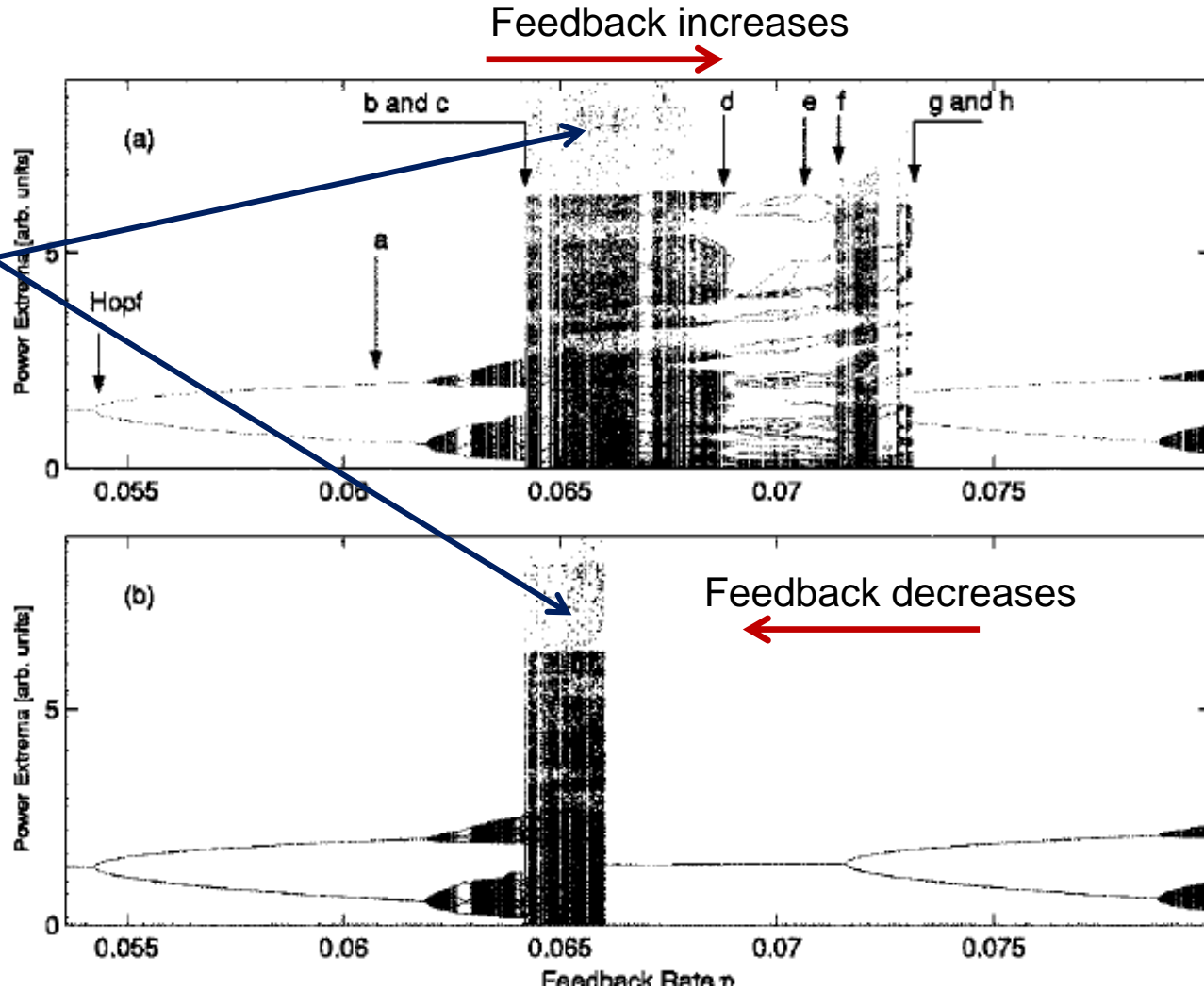
■ Simulations



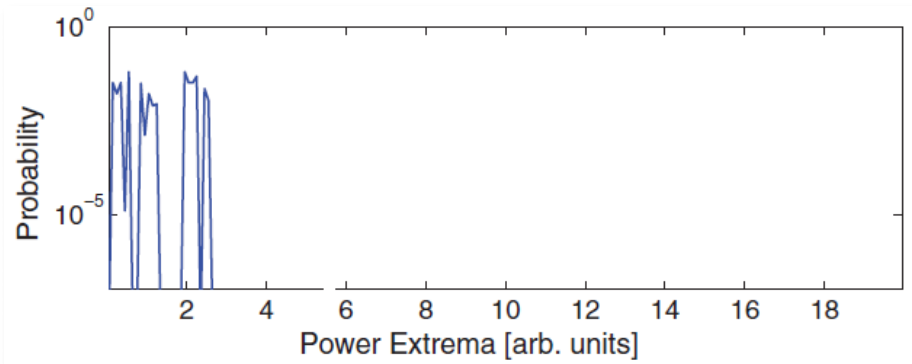
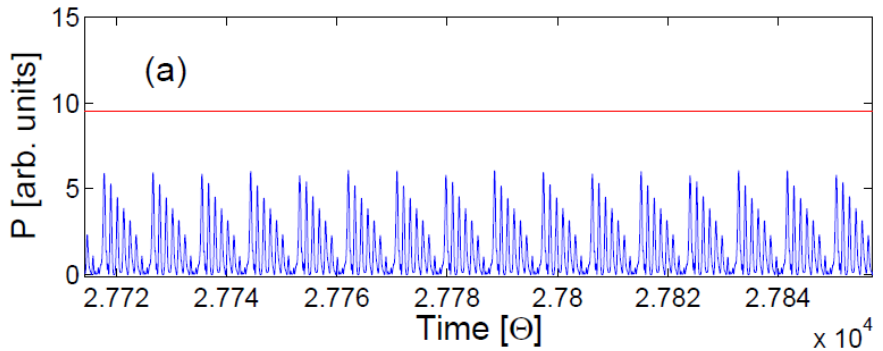
T. Heil et al, PRL 87, 243901 (2001)

A. Tabaka, et al. PRE 70, 036211 (2004)

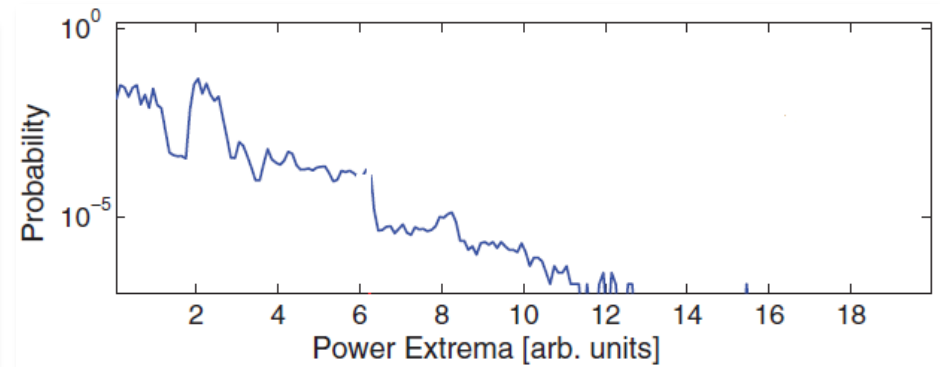
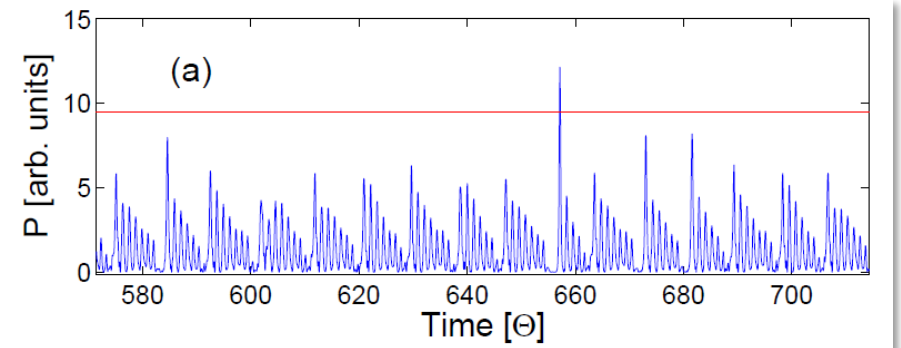
Numerical bifurcation diagram



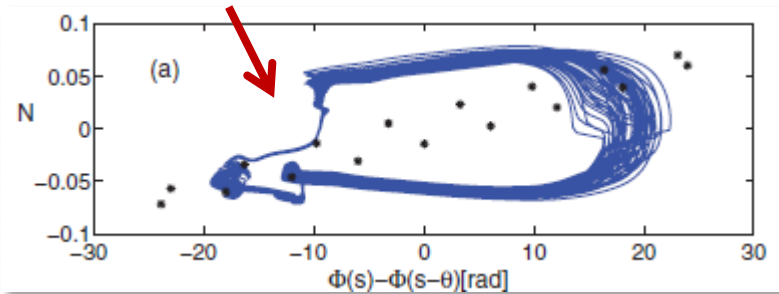
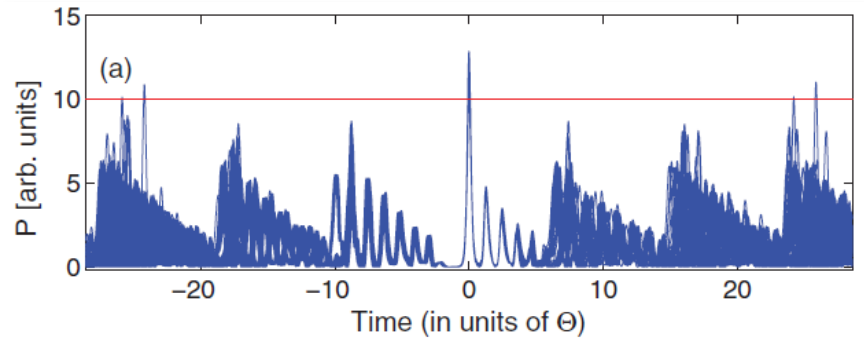
Regular pulse packages



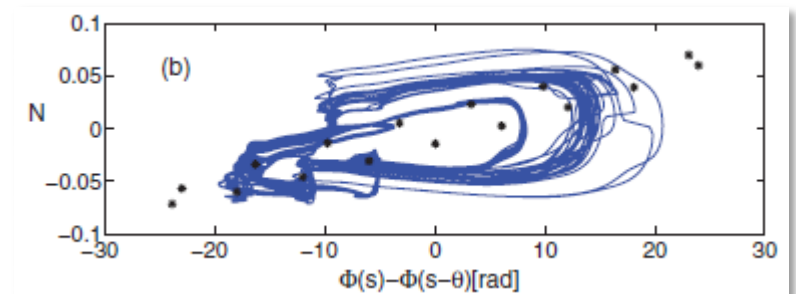
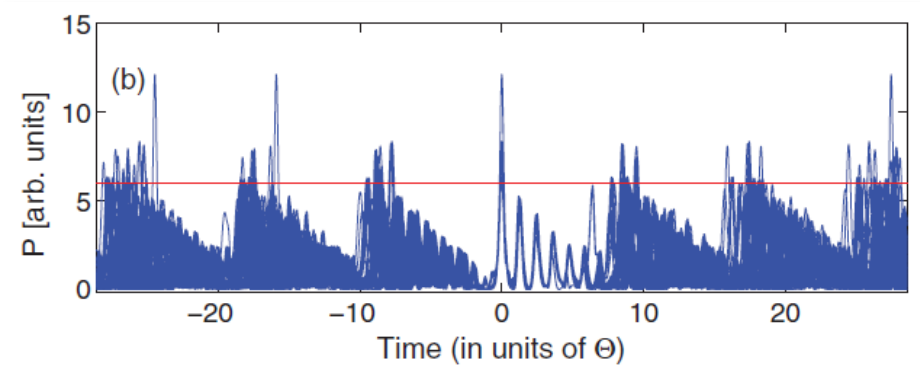
Extreme pulses



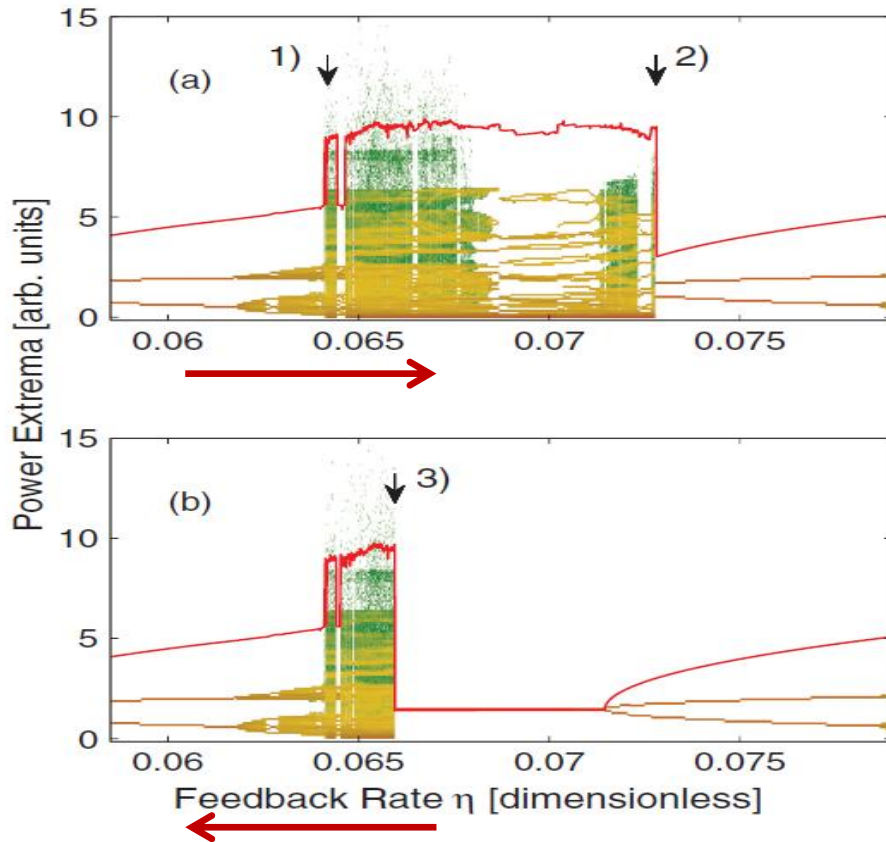
Using a high threshold



Using a lower threshold

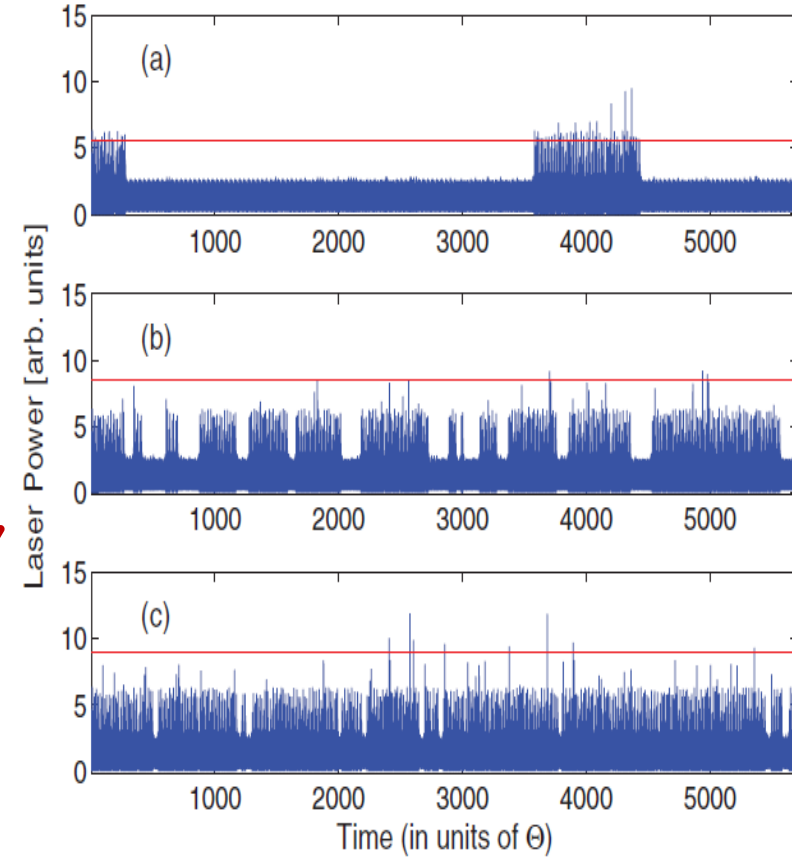


Deterministic intermittency

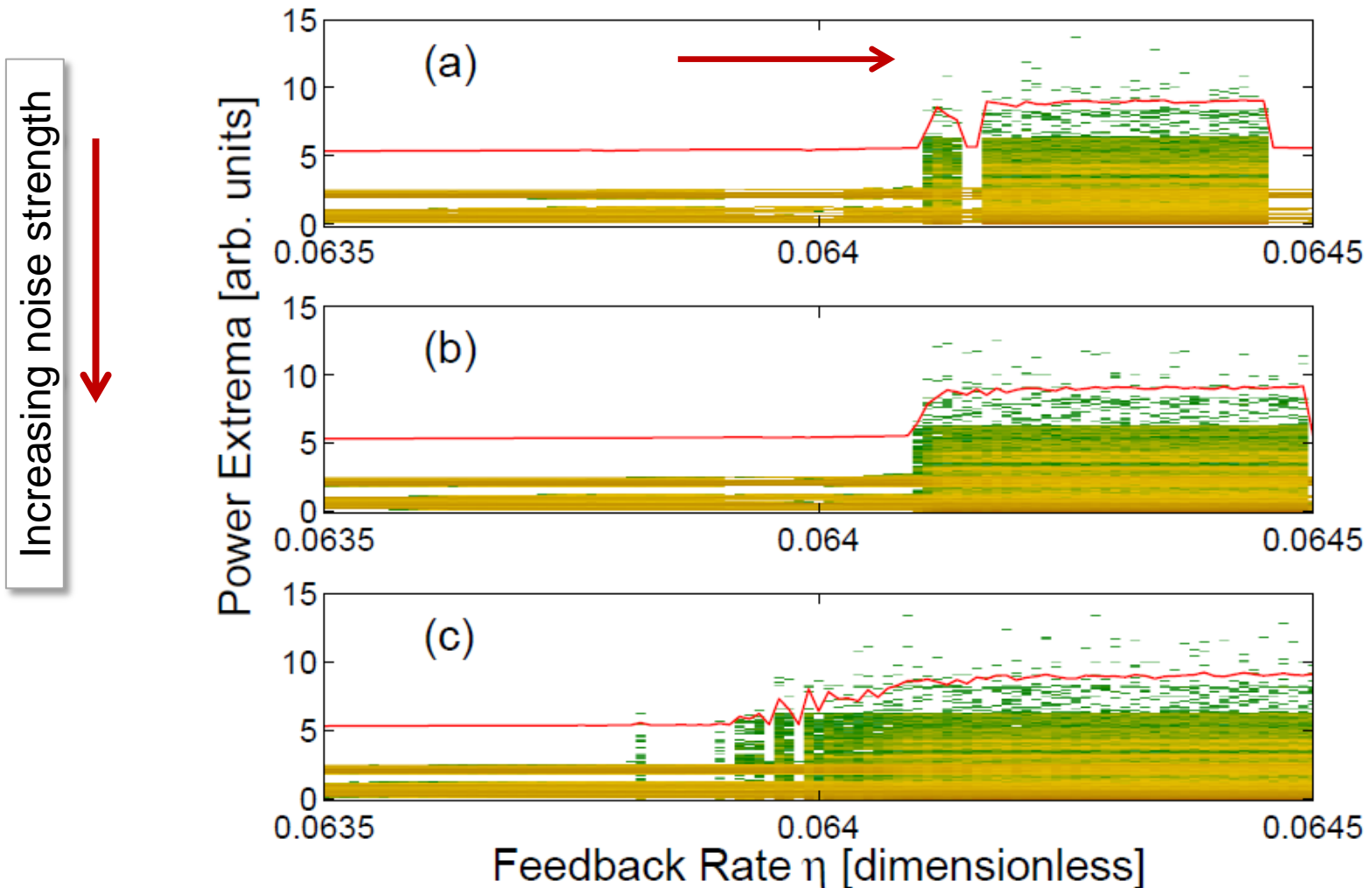


At transition 1:

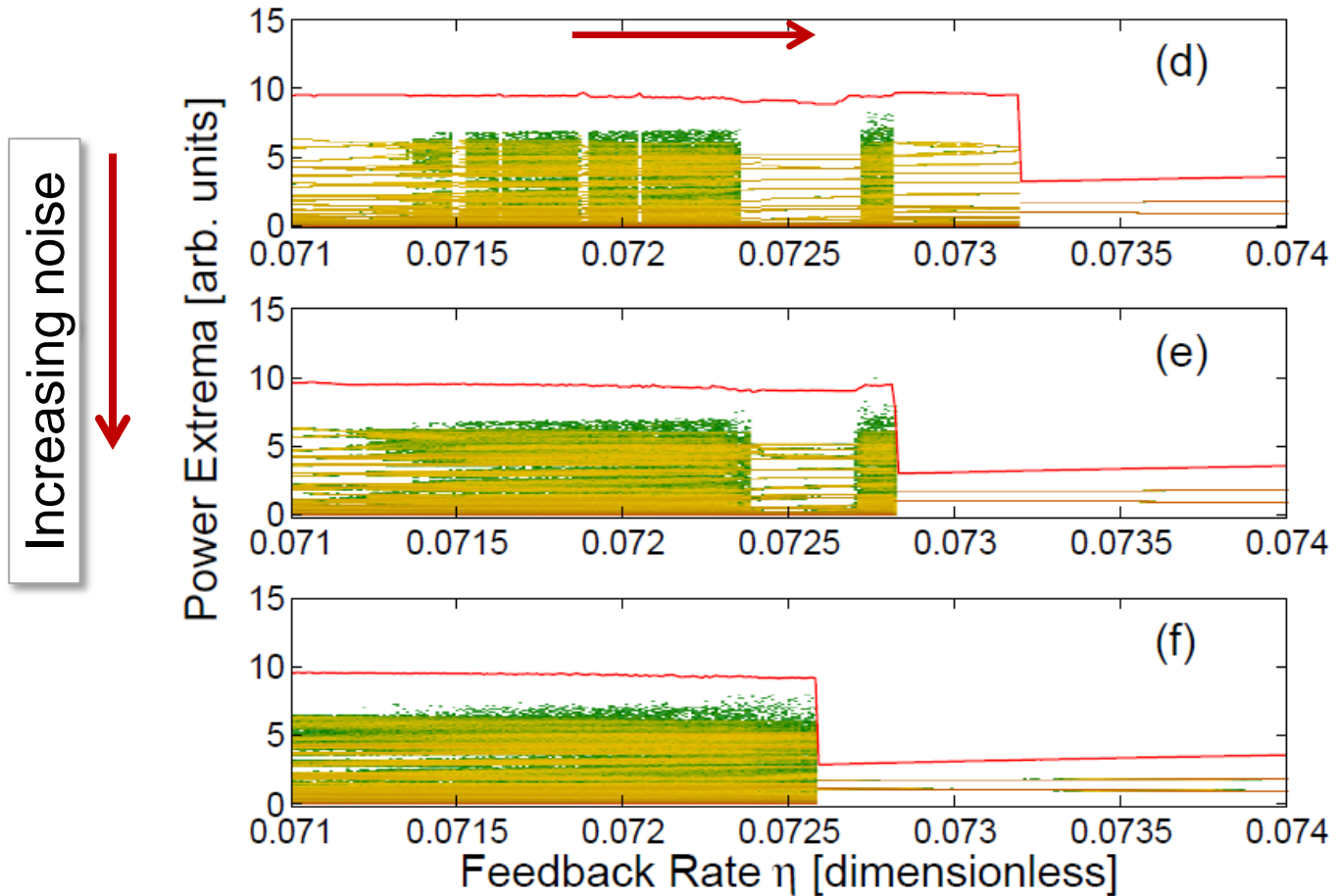
Feedback increases



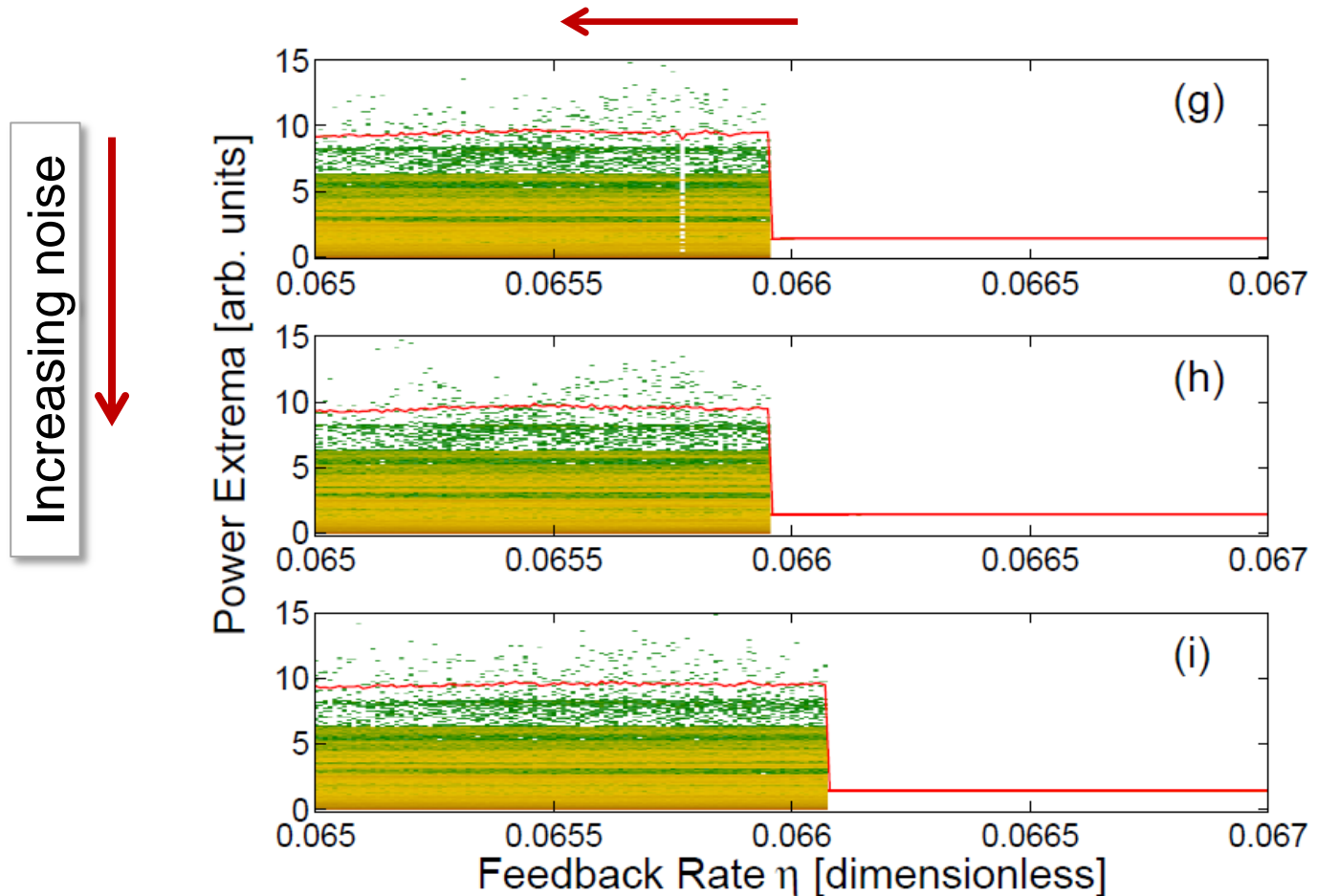
- Transition 1: noise induced extreme pulses



- Transition 2: noise advances the switching



- Transition 3: noise advances the switching



Laser with optical injection:

- **Origin** of RWs: an external crises-like process enables access to the region in phase space where RWs can be triggered.
- **Predictability**: RWs can be predicted with some anticipation.
- **Control**: noise and modulation strongly affects their probability of occurrence.

Lasers with optical feedback:

- Similar results, intermittency is the route to extreme pulses.

Ongoing work: modulation-induced periodicity in the RW waiting times?



THANK YOU FOR YOUR ATTENTION !

<crisina.masoller@upc.edu>

Universitat Politecnica de Catalunya

<http://www.fisica.edu.uy/~cris/>

- C. Bonatto et al, PRL 107, 053901 (2011).
- J. Zamura-Munt et al, PRA 87, 035802 (2013).
- J. M. Reinoso et al, PRE 87, 062913 (2013).
- S. Perrone et al, PRA 89, 033804 (2014).

