

# Neural coding of weak signals in noisy environments using ordinal spike patterns

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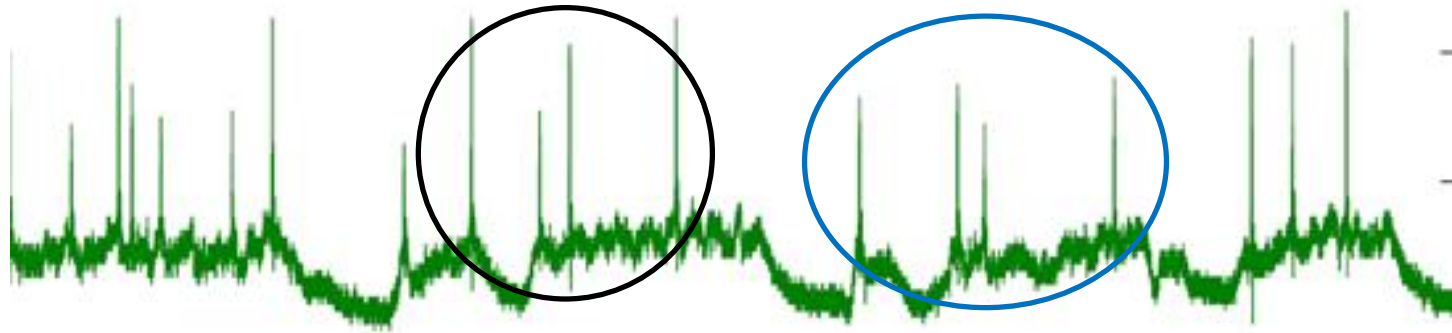
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**Ordinal methods: Concepts, applications, new developments and challenges**  
**Dresden, March 2, 2022**



# How neurons encode information?



- In the spike rate?
- In the timing of the spikes?
- In ordinal spike patterns?
- Our goal: try to understand how neurons encode and transmit information of a **weak** *input signal*.
- Exploit **noise**? / Robust to **noise**?



# Can lasers mimic real neurons?

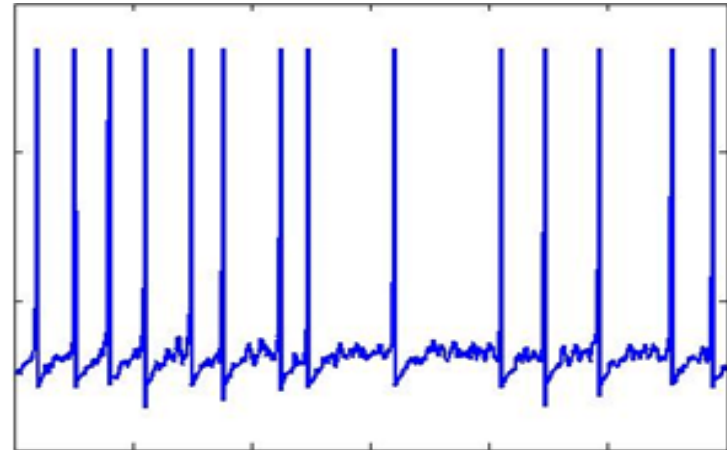
## Laser spikes



Time ( $\mu\text{s}$ )



## Simulated neuronal spikes



Time (ms)

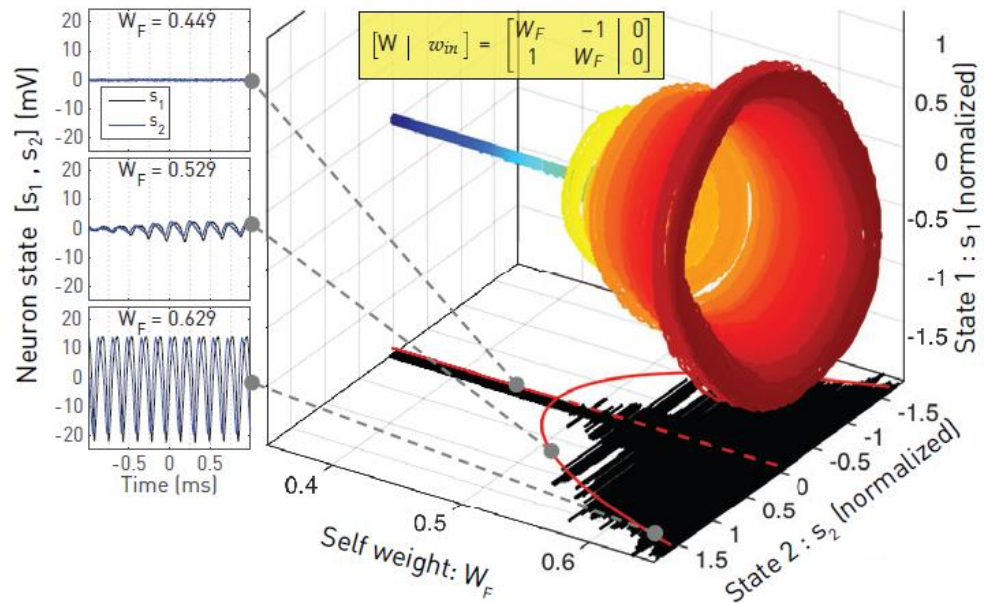
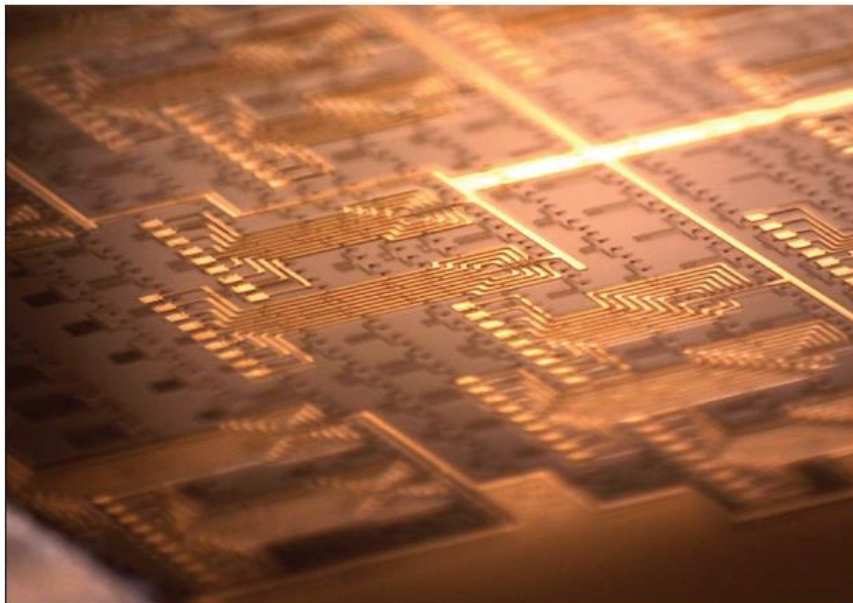


Motivation: Using **neural code** may lead to the development of fast and energy-efficient photonic neural networks.

# Photonic neurons

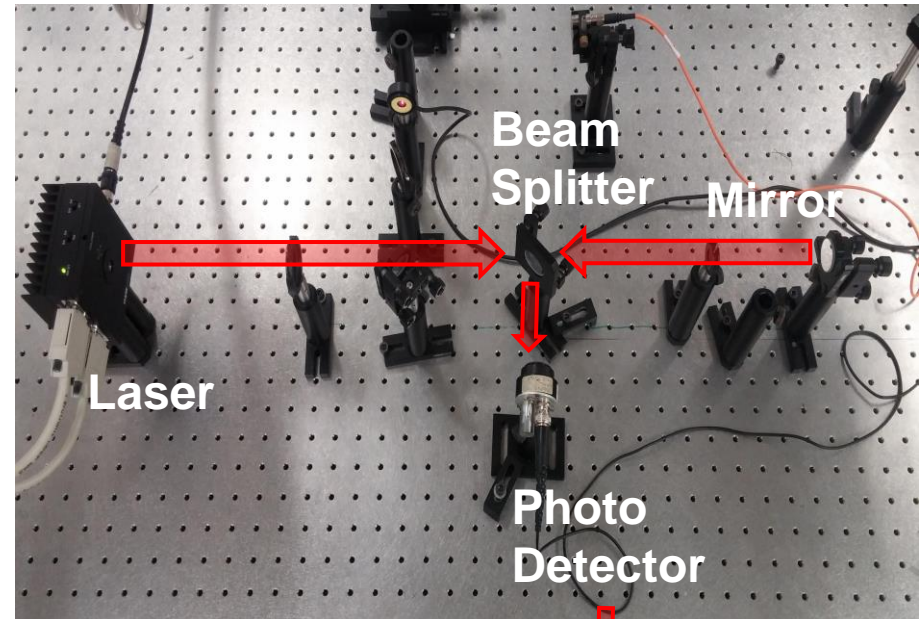
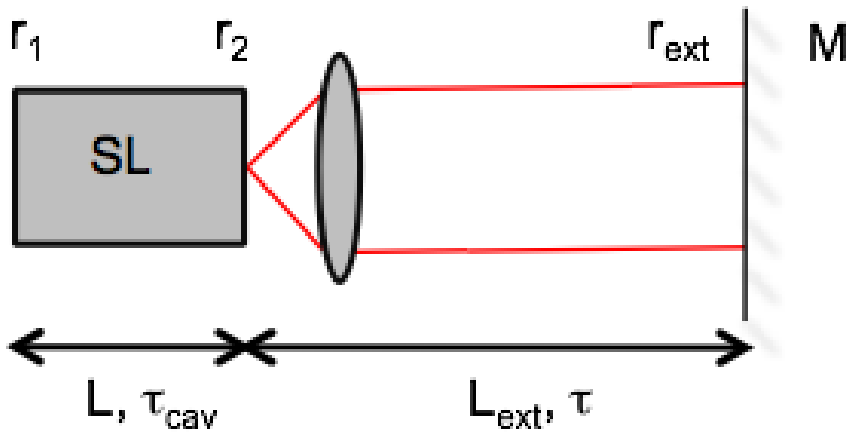
Semiconductor lasers (optically perturbed) can operate in excitable, spiking regimes.

Main advantages: inexpensive, fast, electrically pumped, energy efficient and can be integrated into chips.

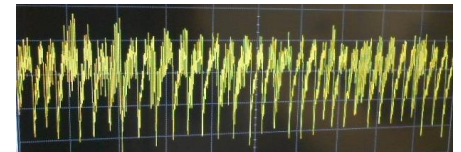


Left: A photonic neural network that can be implemented in silicon photonics. Right: The on-chip system with modulator neurons displays a characteristic oscillation called a Hopf bifurcation, which confirms the presence of an integrated neural network. Princeton University Lightwave Lab, 2017/ A. Tait et al., Sci. Rep. **7**, 7430 (2017).

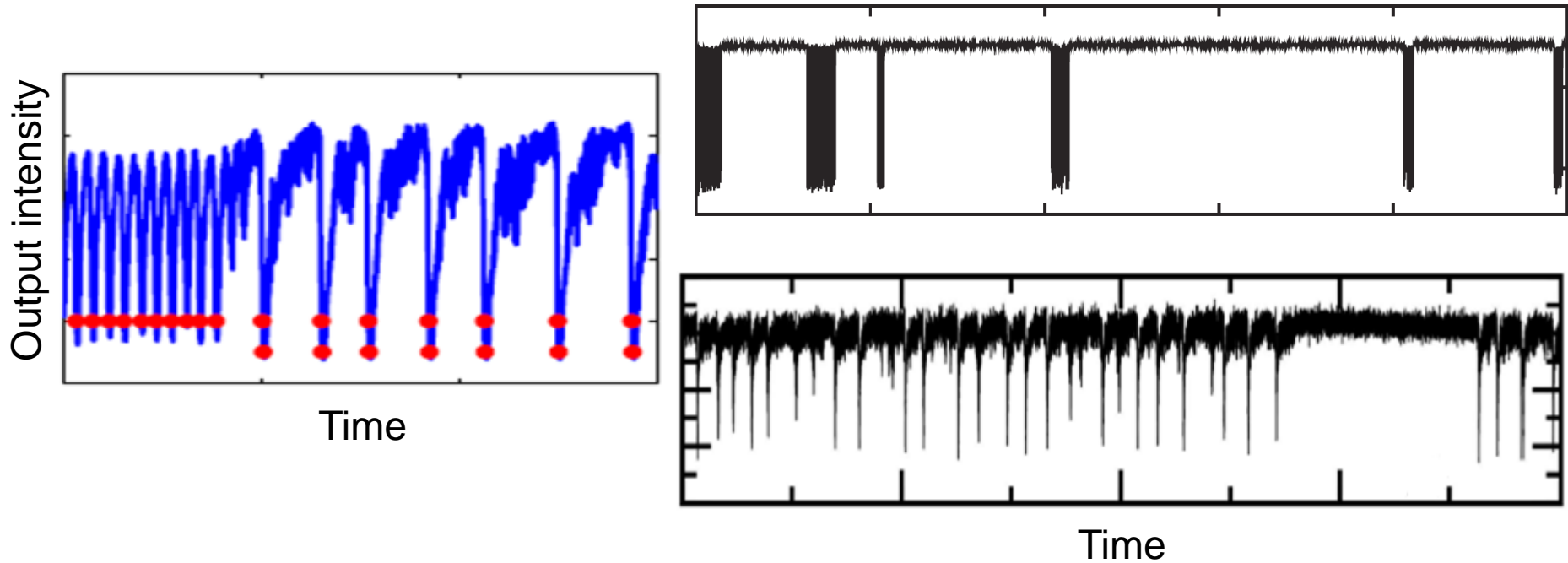
# Experimental setup in our lab



Oscilloscope



# Observed behavior: excitability, tonic spikes, bursting. Similar to real neurons?



A. Aragonese, S. Perrone, T. Sorrentino, M. C. Torrent and C. Masoller, "*Unveiling the complex organization of recurrent patterns in spiking dynamical systems*", Sci. Rep. **4**, 4696 (2014).

C. Quintero-Quiroz, J. Tiana-Alsina, J. Roma, M. C. Torrent, and C. Masoller, "*Characterizing how complex optical signals emerge from noisy intensity fluctuations*", Sci. Rep. **6** 37510 (2016).

# With a weak periodic input, are there statistical similarities between neuronal and laser spikes?

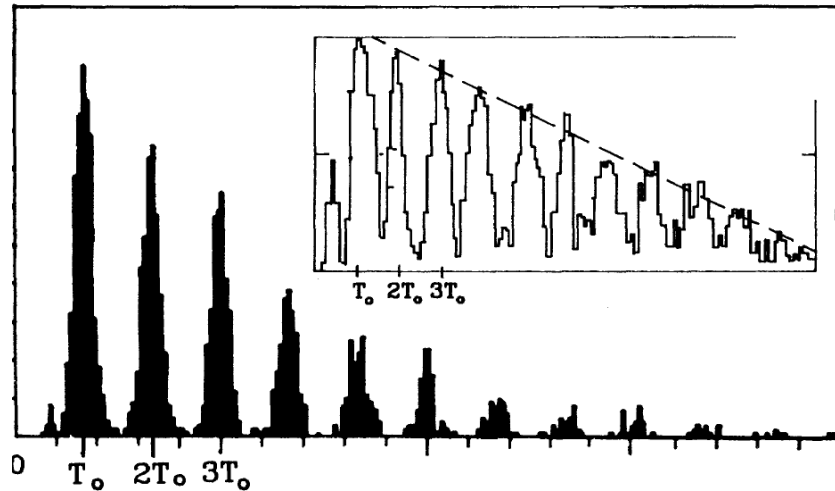
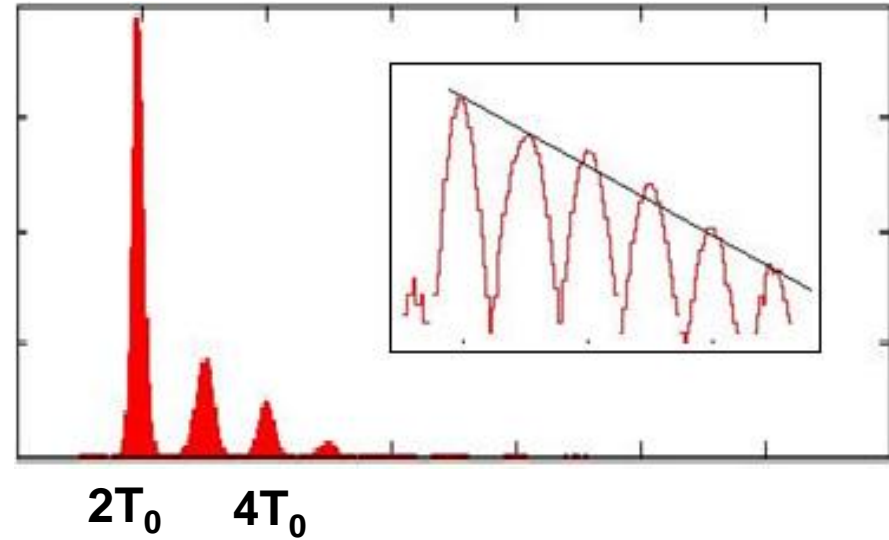


FIG. 1. (a) An experimental ISIH obtained from a single auditory nerve fiber of a squirrel monkey with a sinusoidal 80-dB sound-pressure-level stimulus of period  $T_0 = 1.66$  ms applied at the ear. Note the modes at integer multiples of  $T_0$ . Inset:



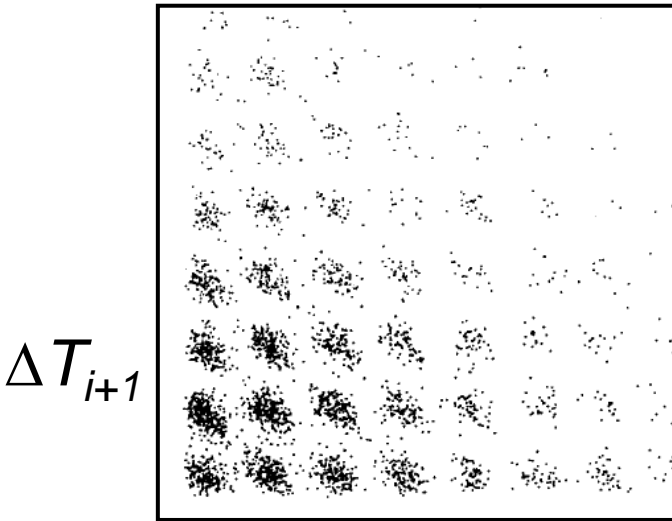
Experimental data when *the laser pump current is modulated with a weak sinusoidal signal of period  $T_0$ .*

[A. Aragonese et al.](#)  
[Optics Express \(2014\)](#)

*A. Longtin et al. PRL (1991)*

# Return maps of the inter-spike-intervals (ISIs)

Neuronal ISIs

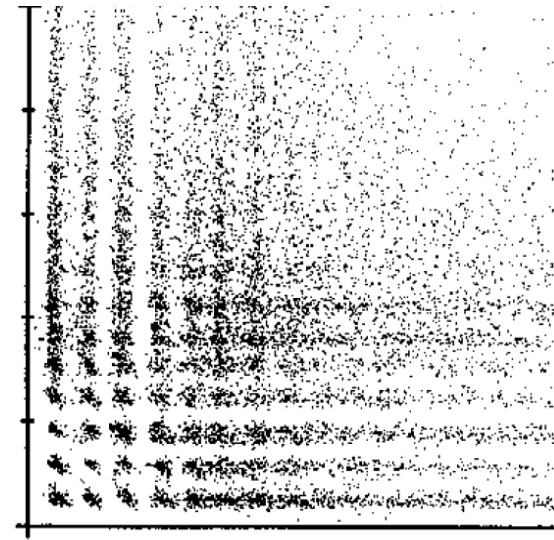


$\Delta T_i$

A. Longtin

*Int. J. Bif. Chaos* (1993)

Laser ISIs



*M. Giudici et al PRE* (1997)

[A. Aragonese et al  
Optics Express](#) (2014)

## SIMILAR SPIKE PATTERNS?

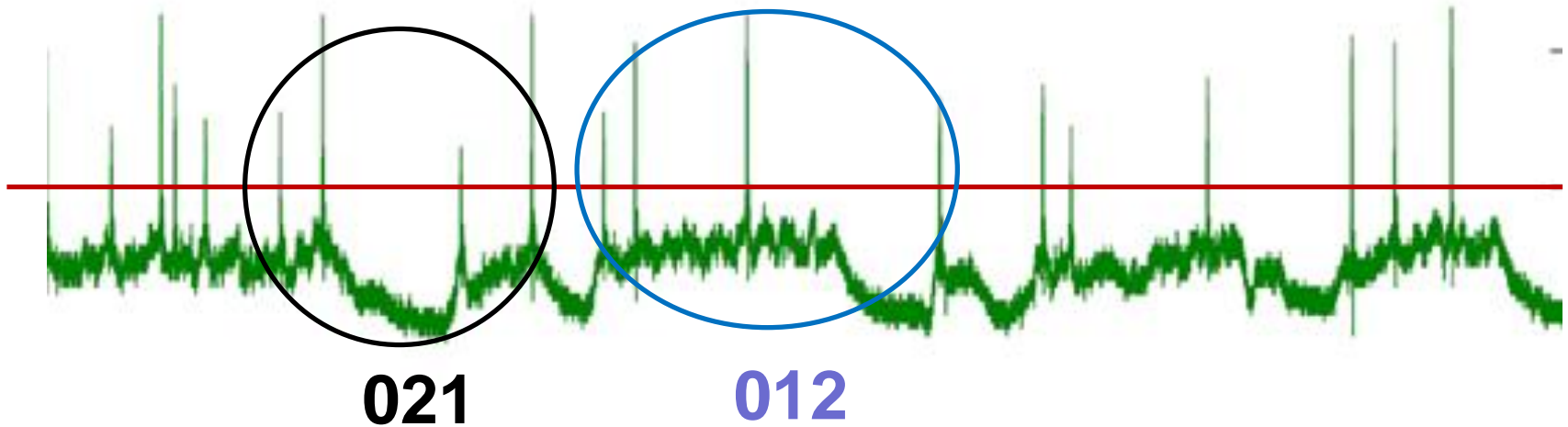
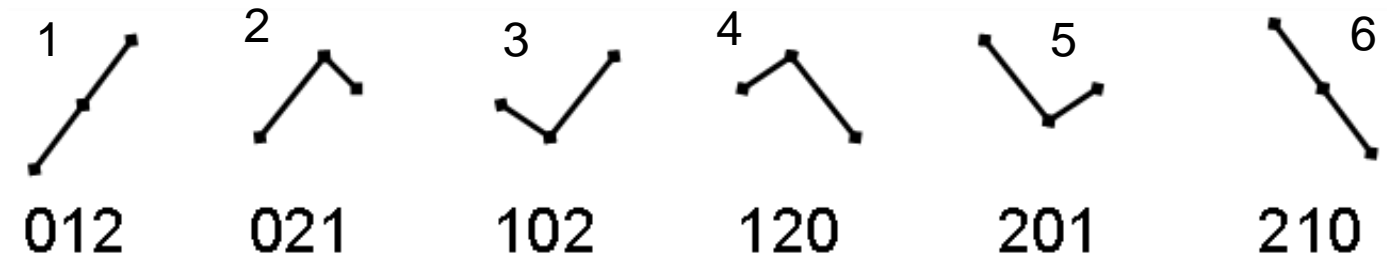


# **Ordinal method of analysis of sequences of inter-spike-intervals**

# Relative order of **three** consecutive intervals

$$l_i = t_{i+1} - t_i$$

$$\{\dots l_i, l_{i+1}, l_{i+2}, \dots\}$$

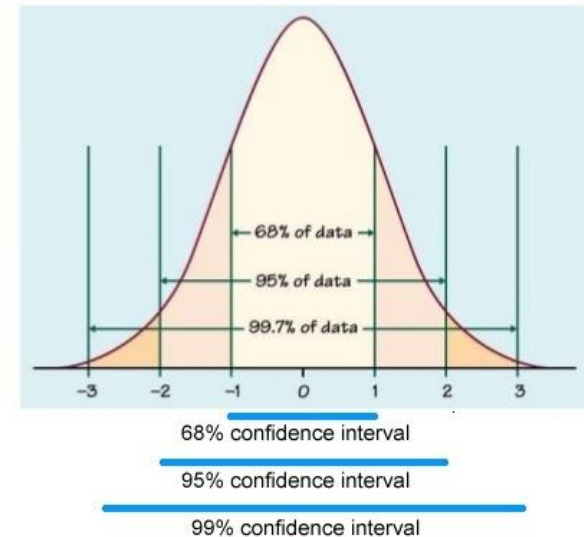


# Are differences in ordinal probabilities significant?

- **Null hypothesis:**

$$p_i = p = 1/D! \quad \text{for all } i = 1 \dots D!$$

- **If at least one probability is not** in the interval  $p \pm 3\sigma$  with  $\sigma = \sqrt{p(1-p)/N}$  and  $N$  the number of ordinal patterns: we **reject** the NH (with 99.74% confidence level).



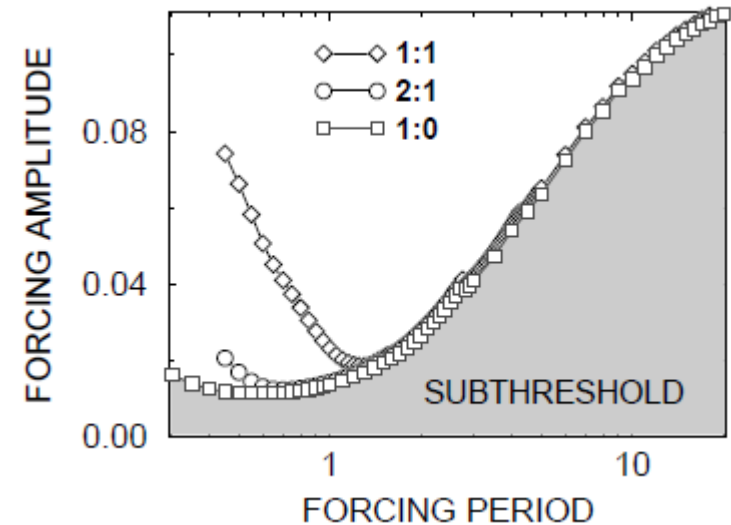
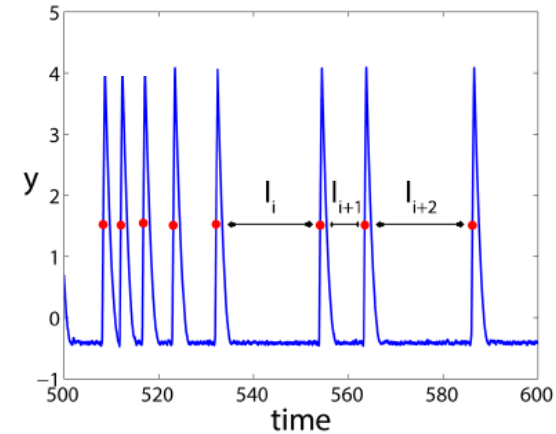
# **Single neuron**

**More / less frequent ordinal spike patterns  
encode information about a weak input?**

# FitzHugh-Nagumo model

$$\epsilon \frac{dx}{dt} = x - \frac{x^3}{3} - y,$$

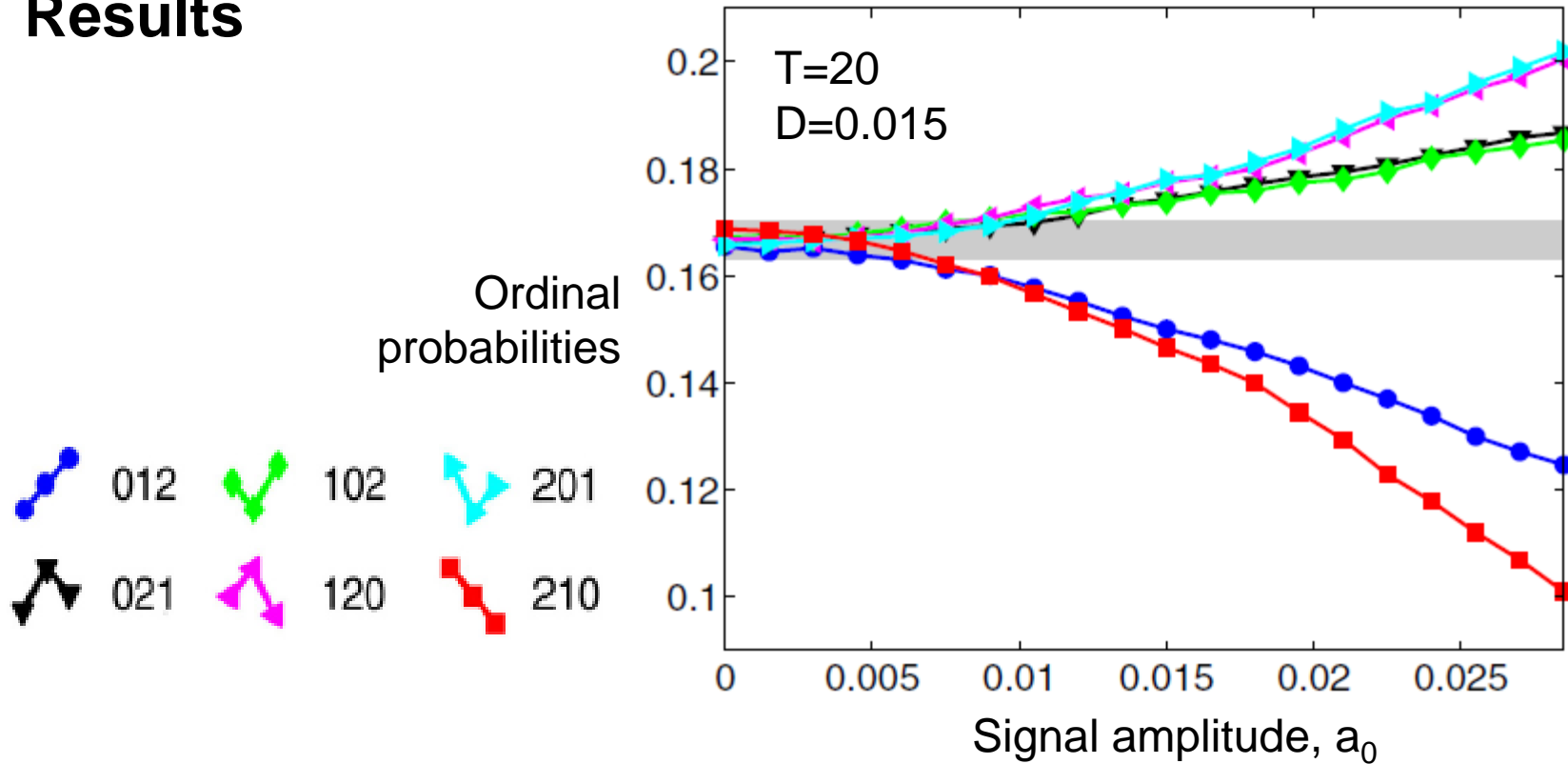
$$\frac{dy}{dt} = x + a + a_0 \cos(2\pi t/T) + D\xi(t),$$



*Longtin and Chialvo, PRL 1998*

- $a=1.05$ ,  $\epsilon=0.01$
- Gaussian white noise
- Subthreshold signal:  $a_0$  and  $T$  such that **spikes are noise-induced**.
- Time series with  $M=100,000$  spikes.

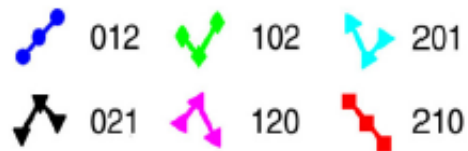
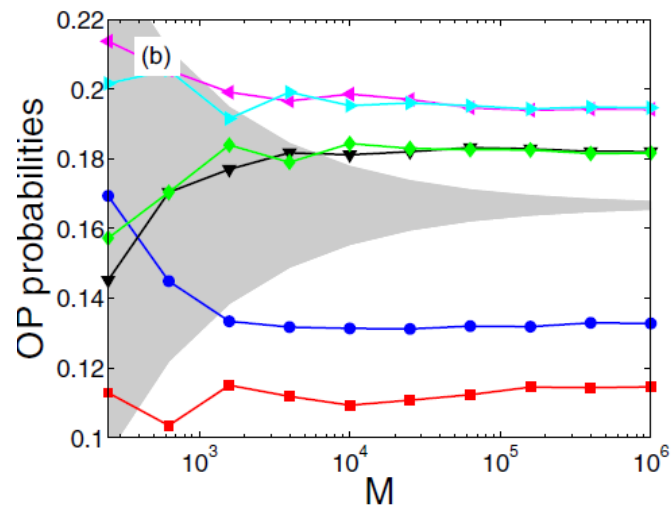
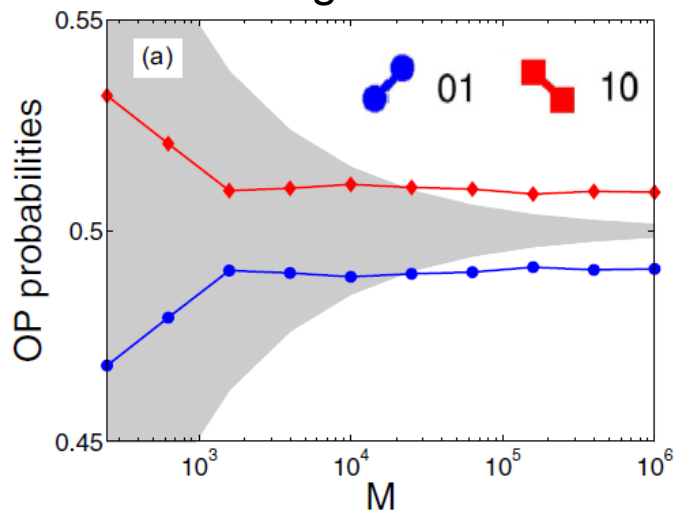
# Results



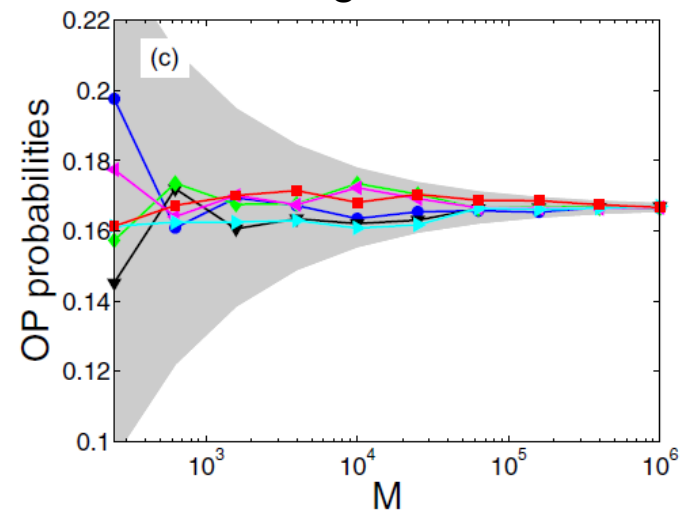
- Gray region:  $3\sigma$  confidence level.

# Data requirements

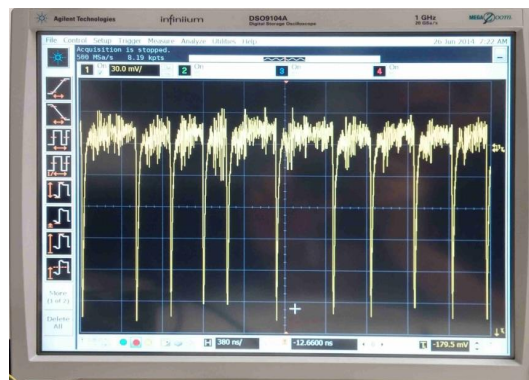
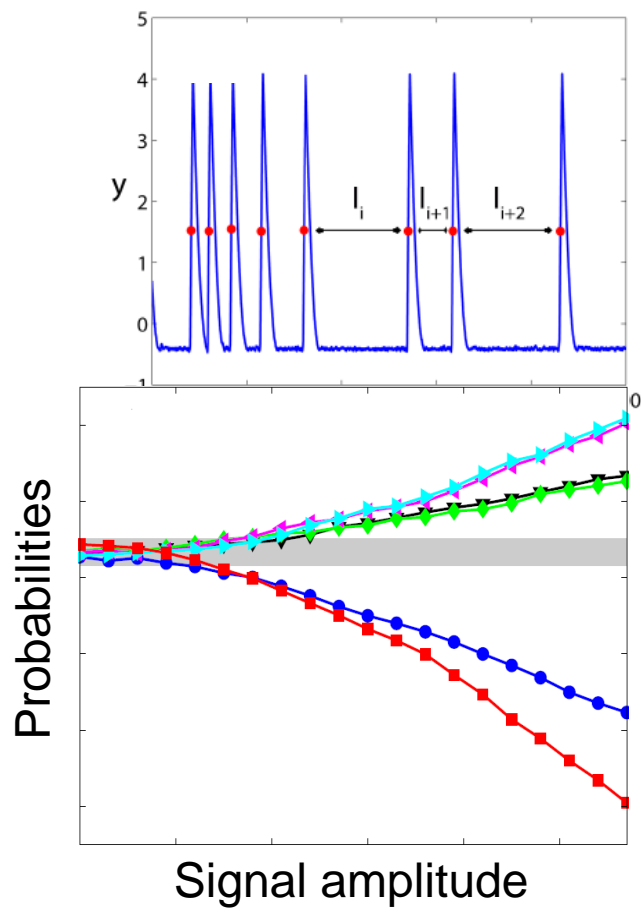
With signal



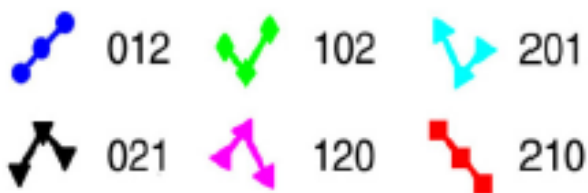
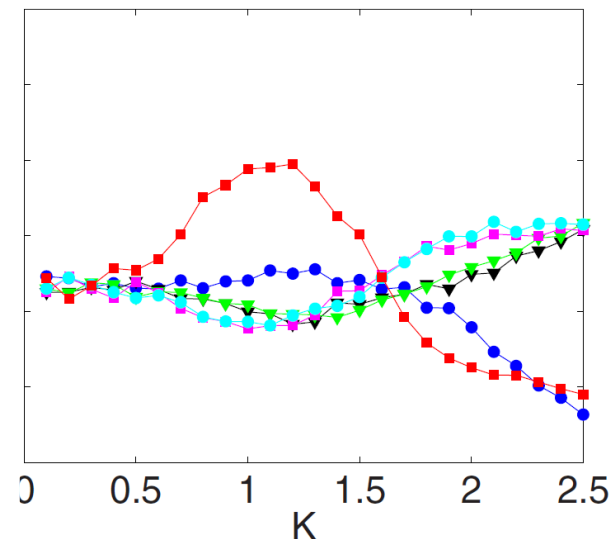
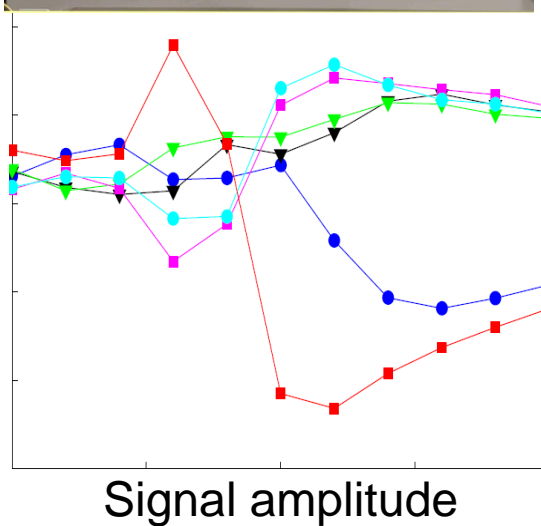
Without signal



# Comparison with the laser spikes, when a small sinusoidal signal is added to the laser current



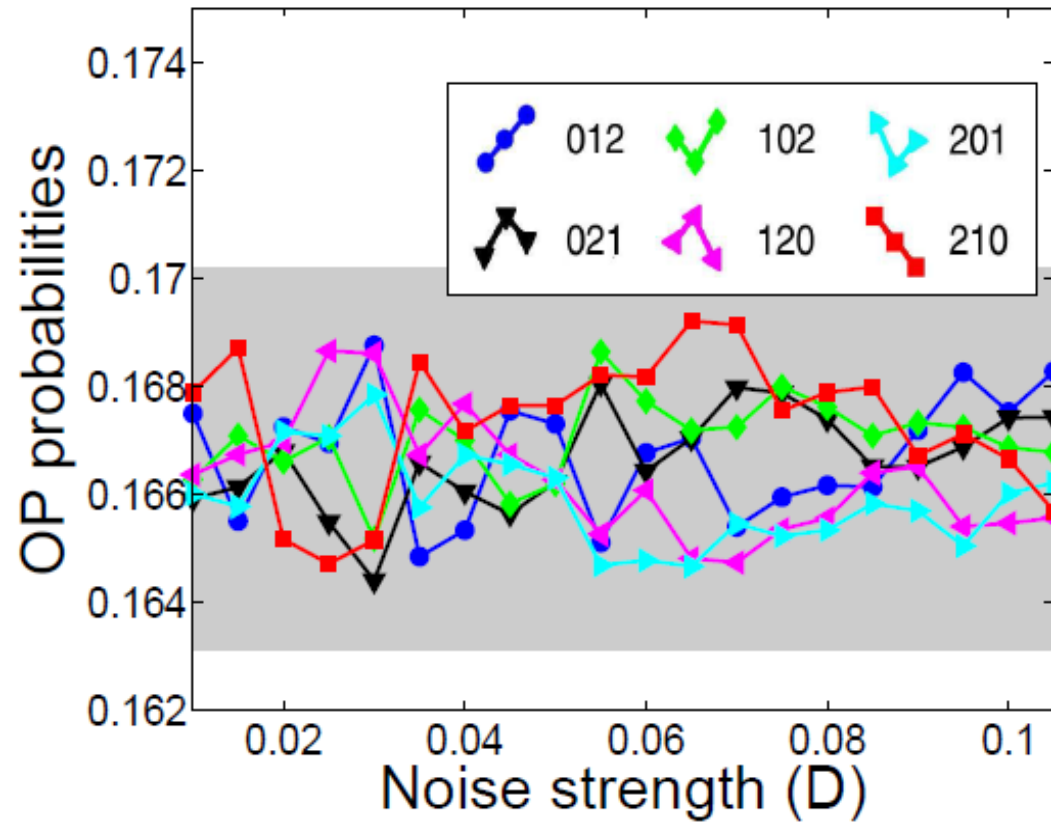
$$\phi(i+1) = \phi(i) + \rho + \frac{K}{2\pi} [\sin(2\pi\phi(i)) + \alpha_c \sin(4\pi\phi(i))] + \beta_c \xi(i)$$





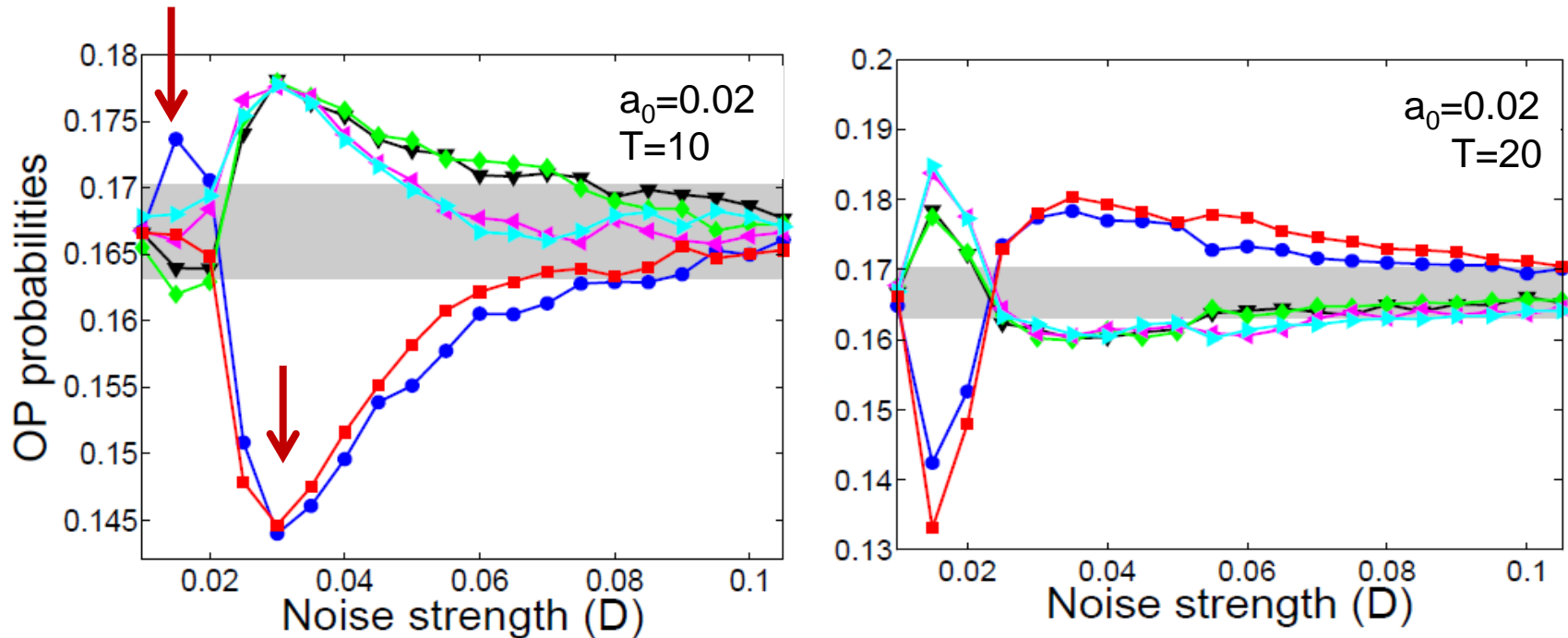
# Role of the level of noise

$$a_0=0$$



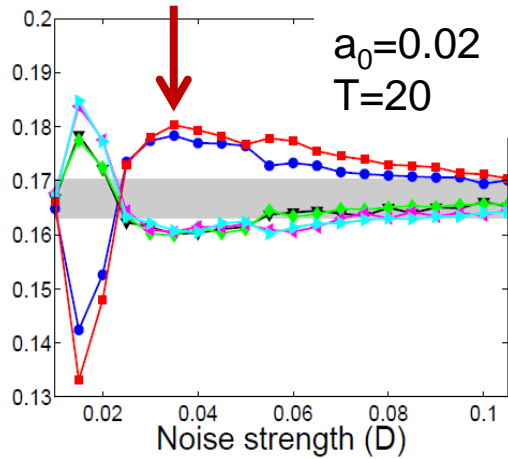
No signal  $\Rightarrow$  no preferred spike patterns

# With a sinusoidal input

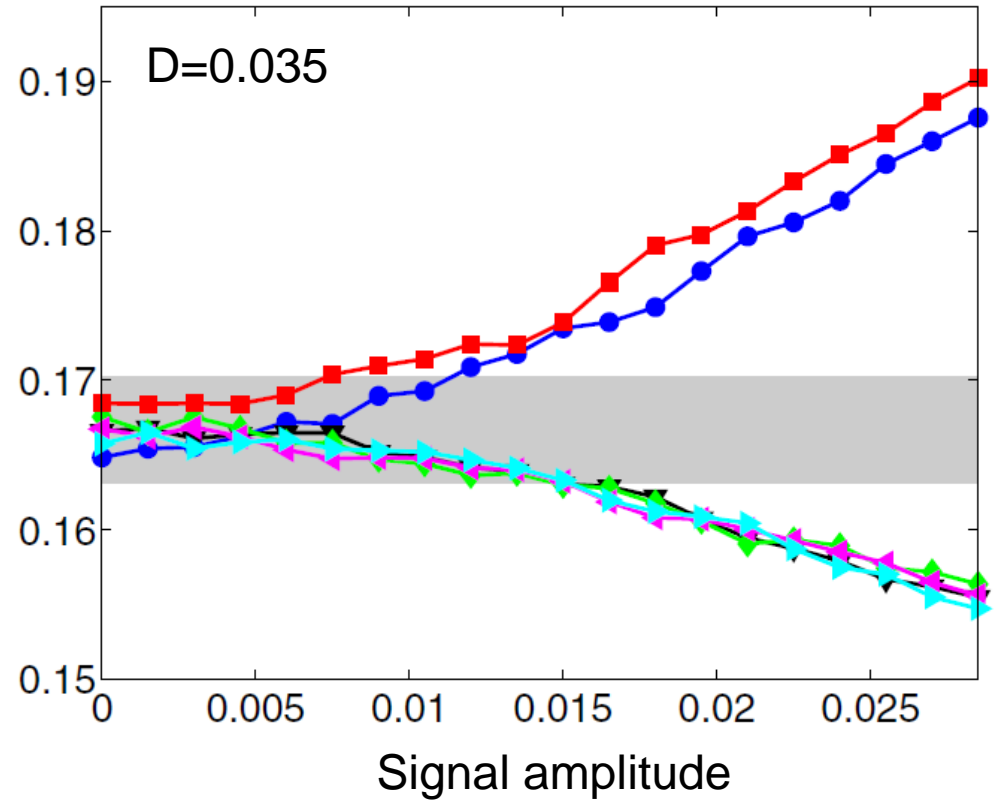


- The signal induces more / less expressed patterns.
- They depend on the amplitude, period and noise strength.
- Resonant-like behavior.

# Role of the signal amplitude

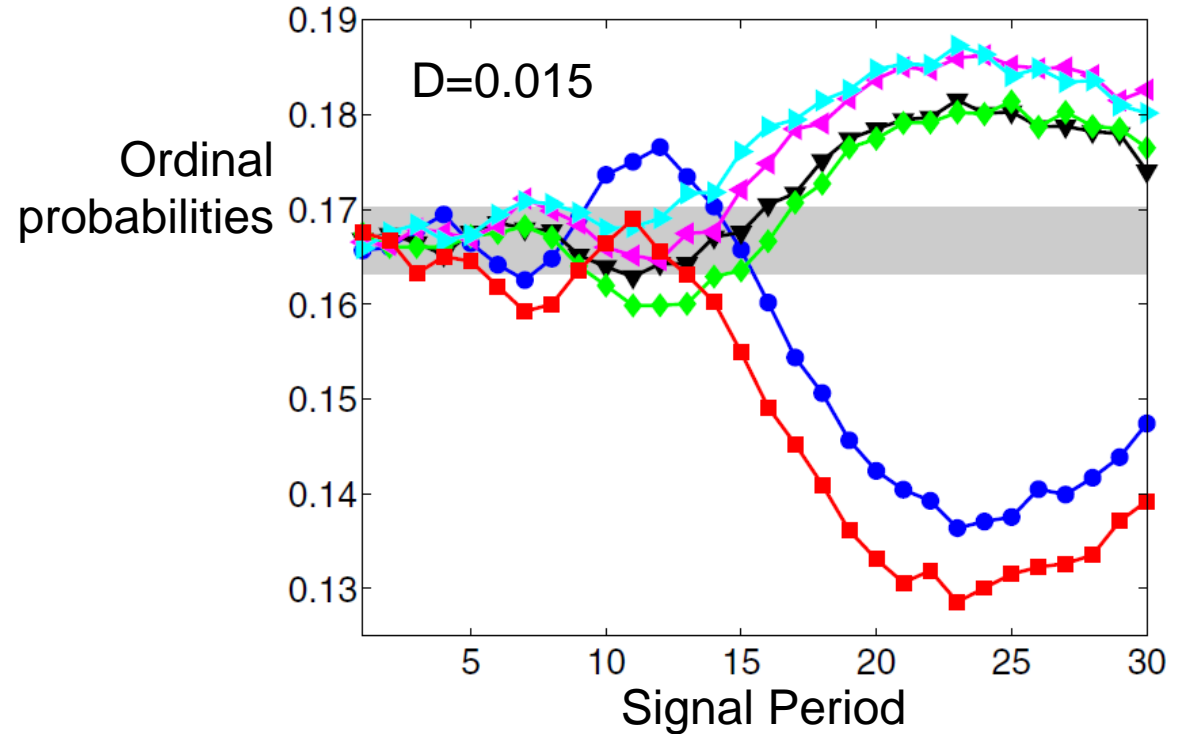
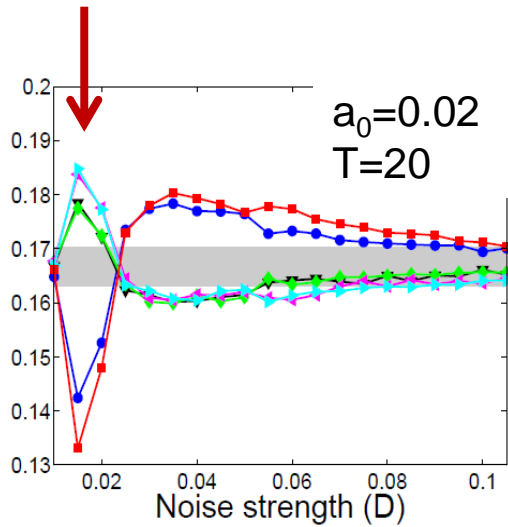


Ordinal probabilities



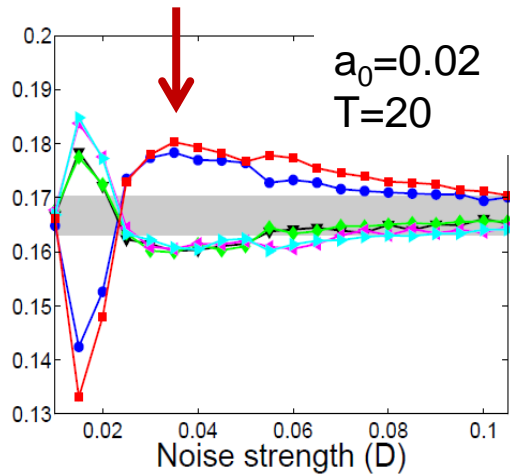
The values of the probabilities may encode the amplitude of the signal?

# Role of the signal period

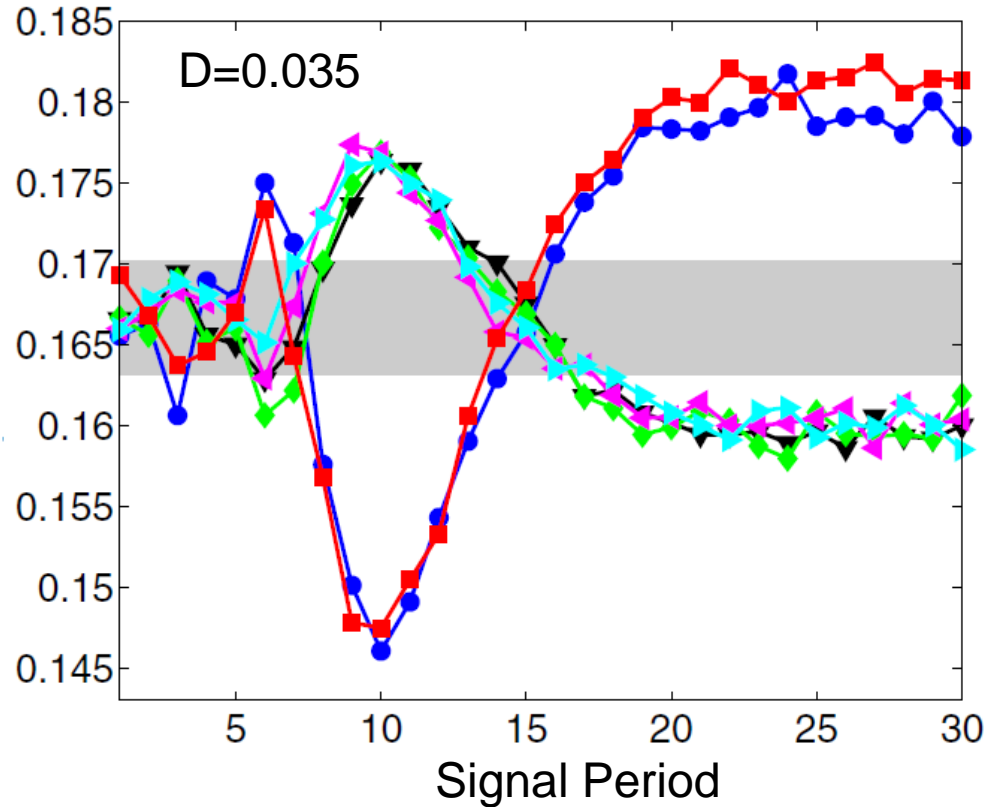


More / less expressed patterns depend on the signal's period.

# Role of the signal period

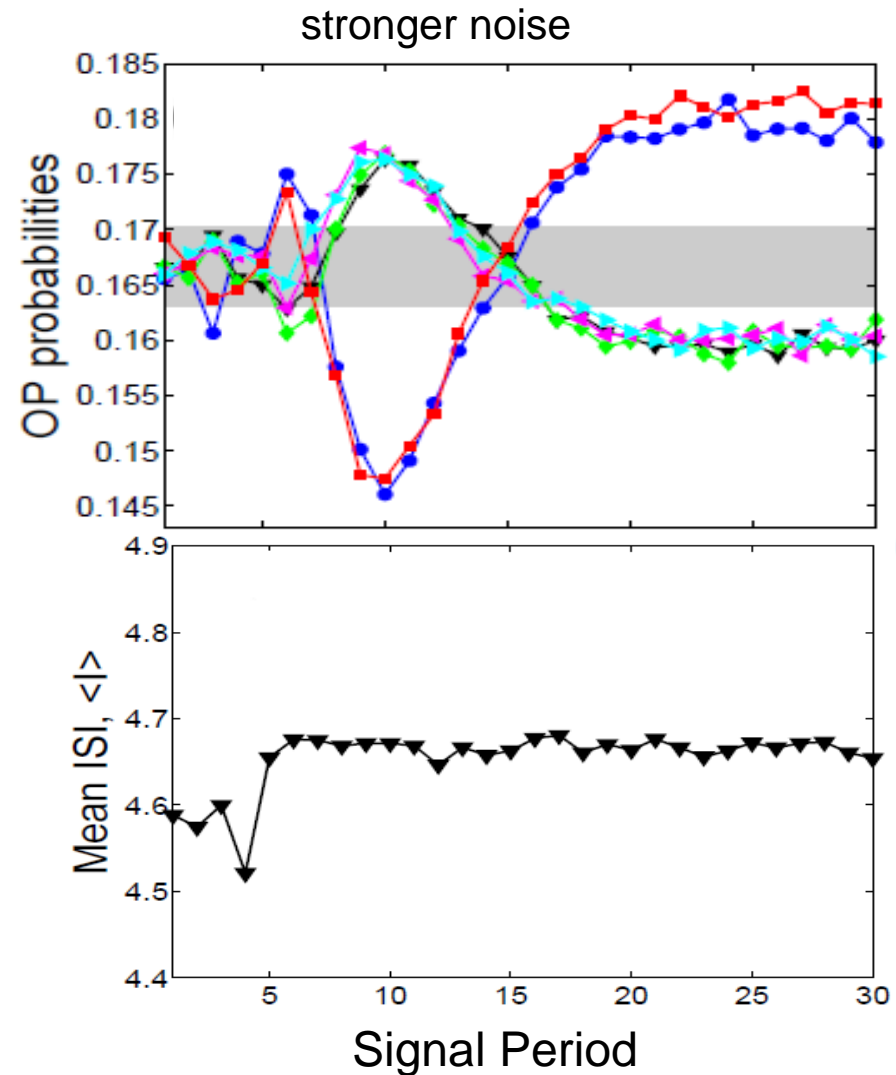
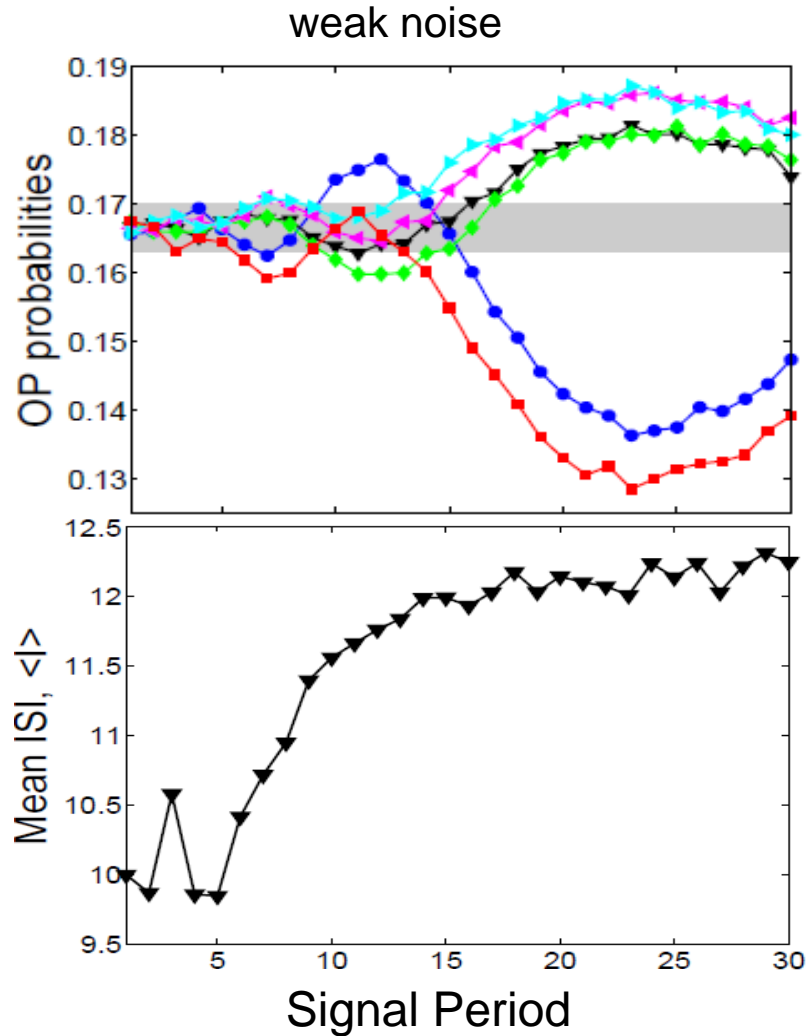


Ordinal probabilities



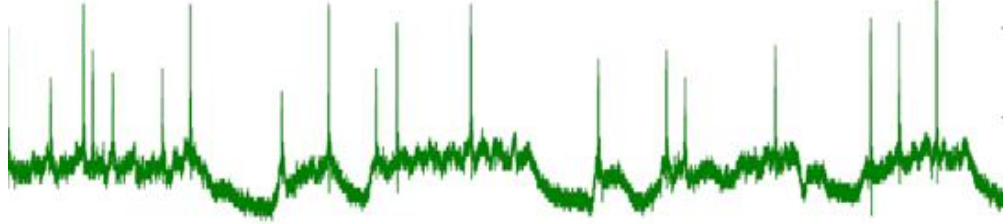
More / less expressed patterns also depend on the noise strength.

# How about “rate coding”? Does the mean inter-spike-interval carry information of the period of the signal?

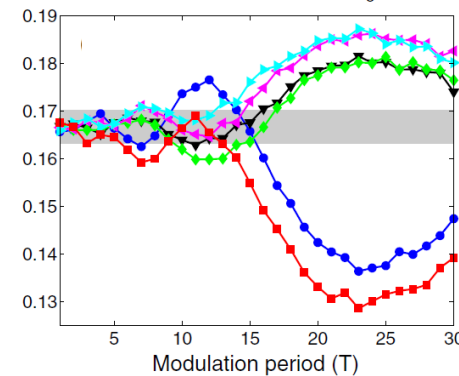
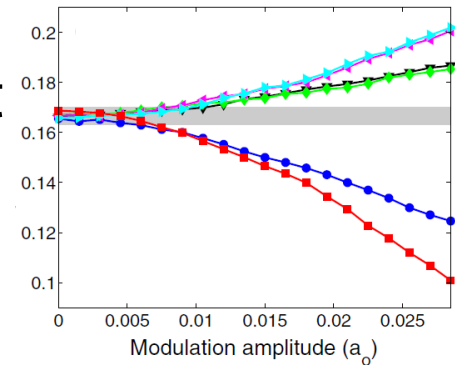


⇒ Not always.

# So... how neurons might encode a weak periodic signal?



- The amplitude and the period of the signal might be encoded in more / less expressed patterns.
- Single-neuron encoding: very **slow** because long spike sequences are needed to estimate the probabilities.
- Ensemble encoding: **fast** because few spikes per neuron can be enough to estimate the probabilities.
- Role of neural coupling?

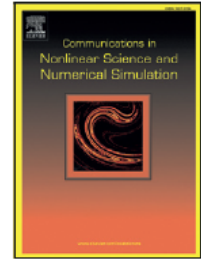




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Research paper

## Neuronal coupling benefits the encoding of weak periodic signals in symbolic spike patterns

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Universitat Politècnica de Catalunya. Departament de Física. Edifici Gaia, Rambla de Sant Nebridi 22, Terrassa, Barcelona, 08222, Spain



$$\epsilon \dot{u}_i = u_i - \frac{u_i^3}{3} - v_i + a_0 \cos(2\pi t/T) + \frac{\sigma}{k_i} \sum_j^N a_{ij} (u_j - u_i) + \sqrt{2D} \xi_i(t), \quad i \neq j$$

$$\dot{v}_i = u_i + a.$$

$$k_i = \sum_j a_{ij}$$

$$a_{ij} = a_{ji} = 1$$

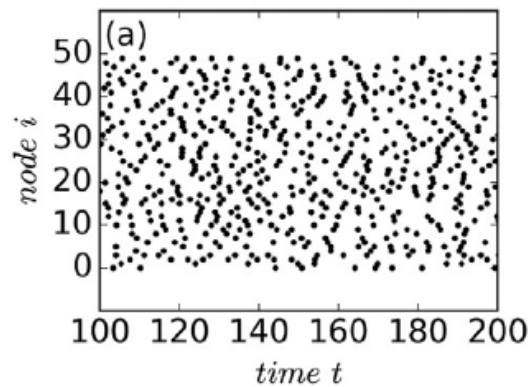
$$a_{ij} = a_{ji} = 0$$

The ordinal probabilities are calculated from the ISI sequences of all the neurons.

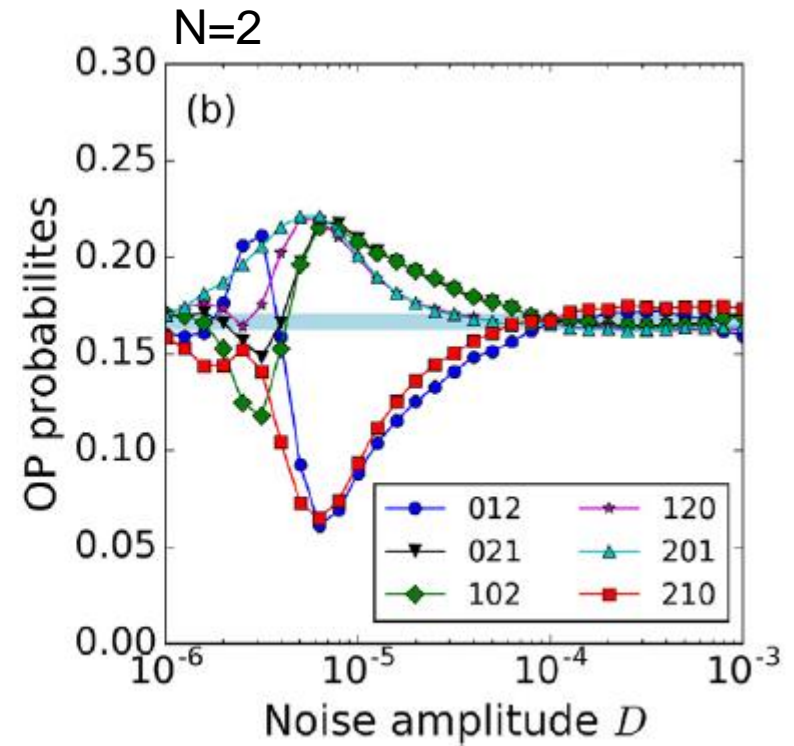
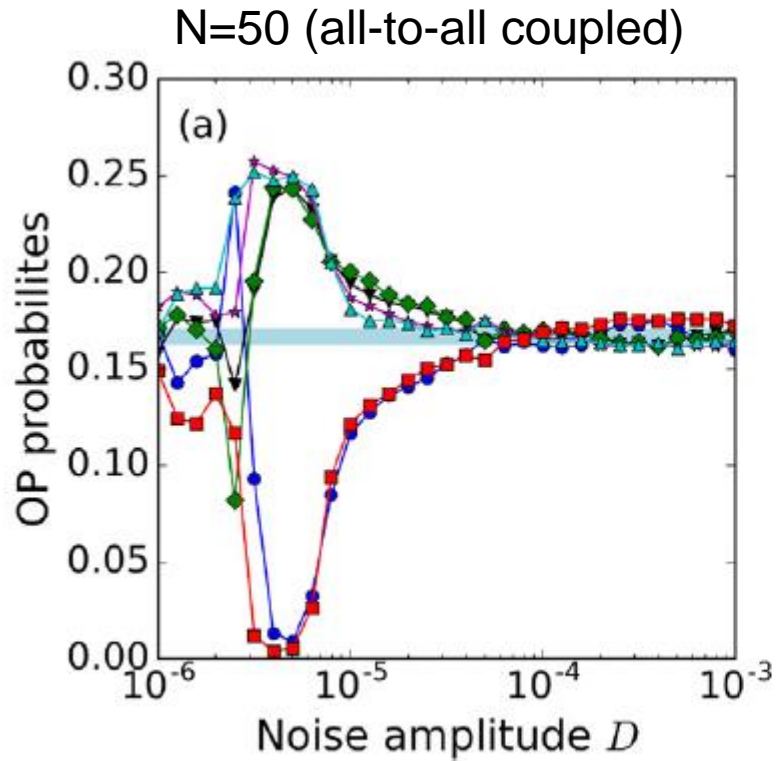


# Dynamics of an ensemble of 50 neurons, all-to-all coupled, for input signals that have different periods

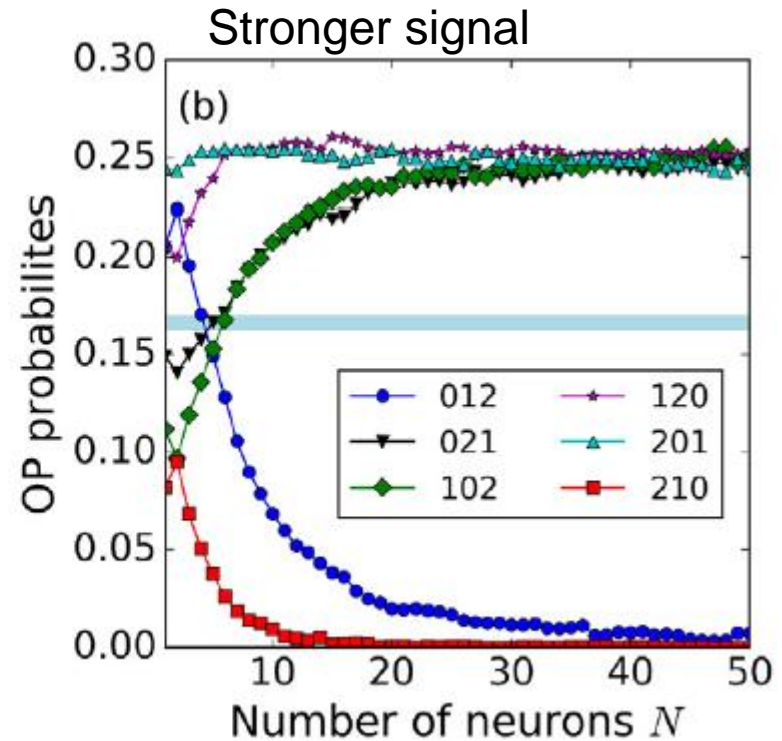
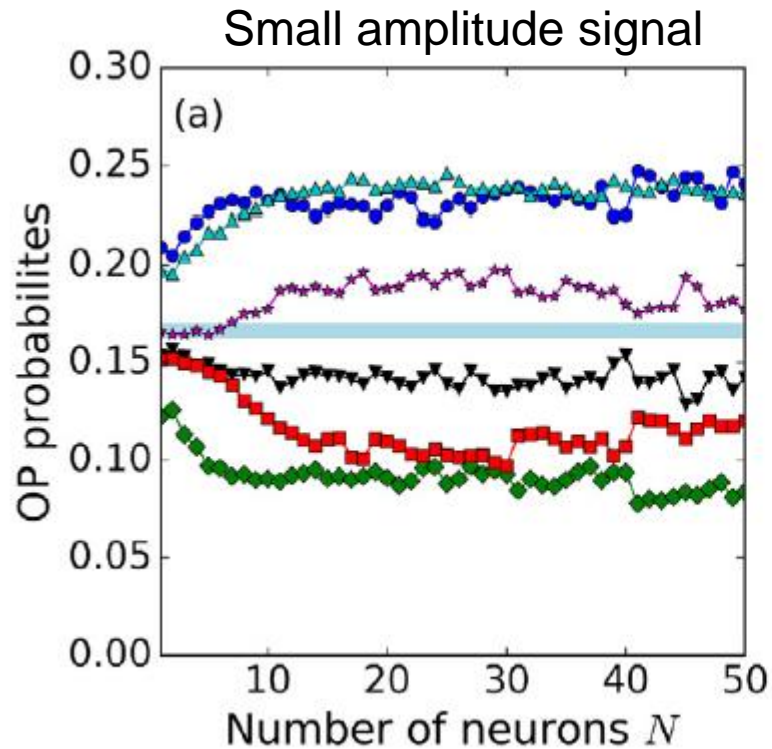
No coupling,  
no signal



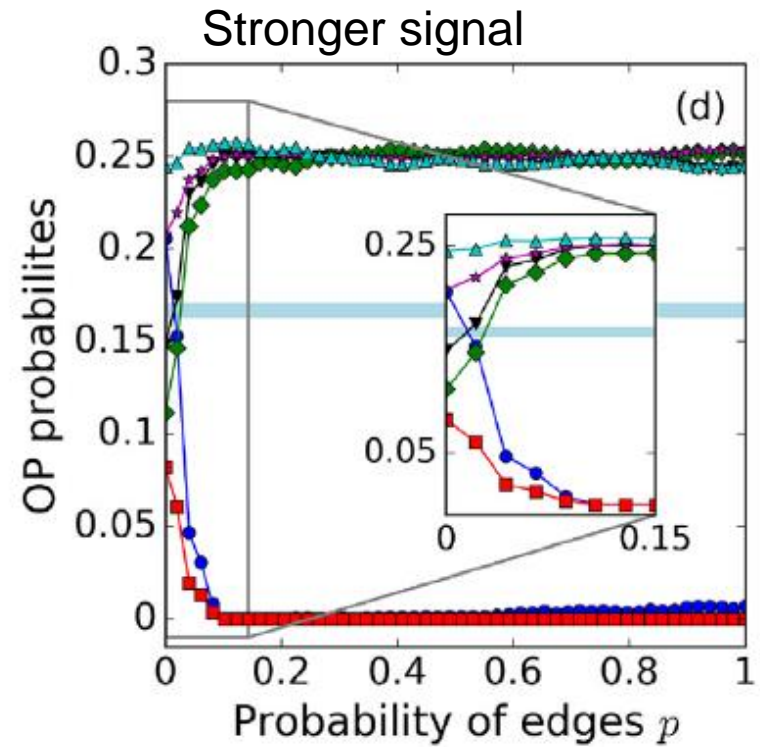
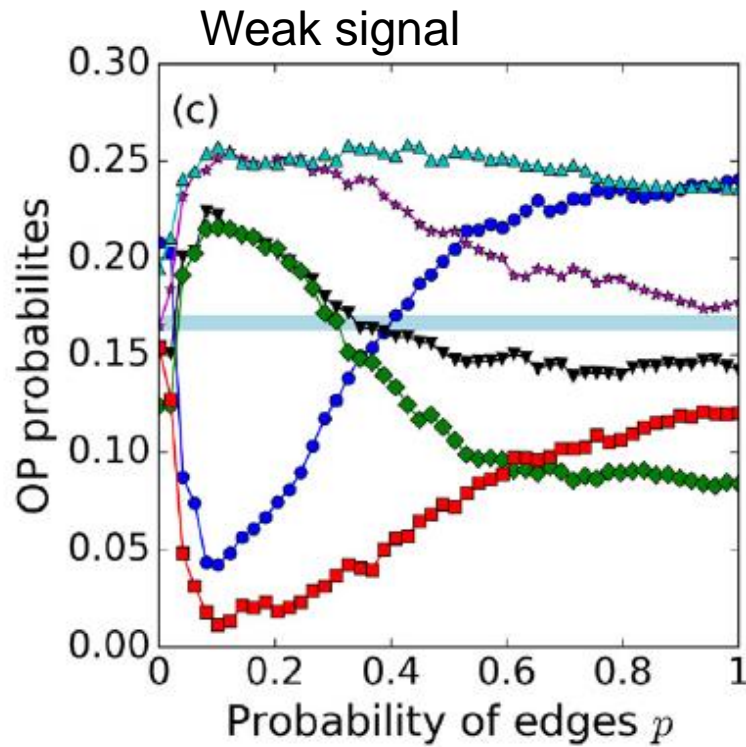
# Role of noise?



# Role of the networks size? (all-to-all coupling)



# Role of the number of connections? (random network)



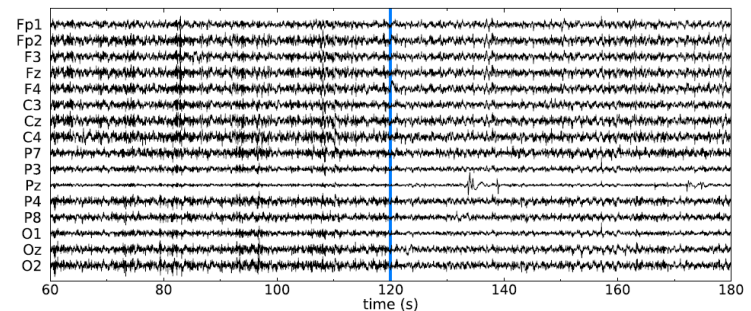
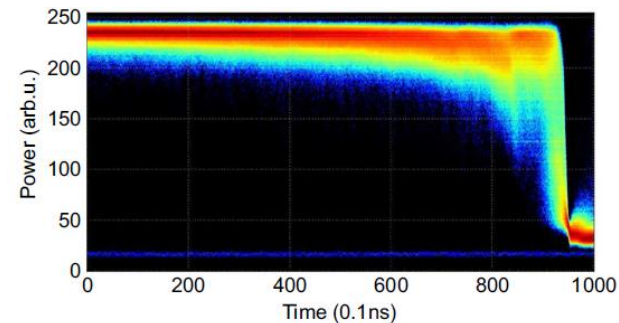
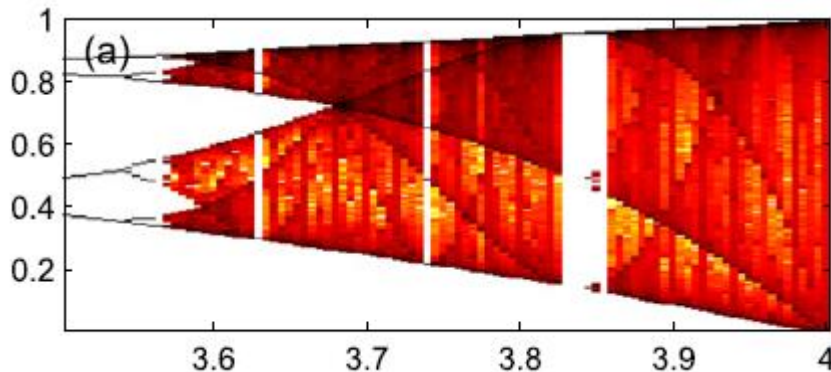
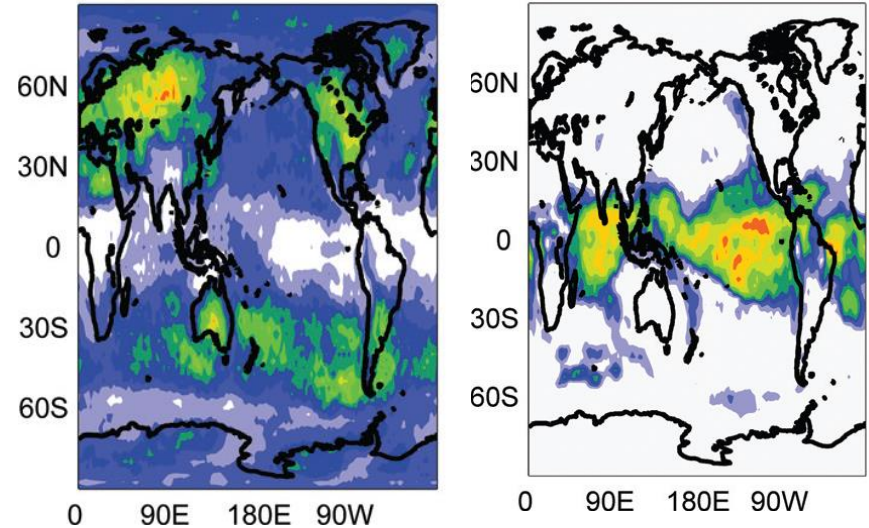
# Conclusions

# Summary

- Conclusions:
  - The ordinal probabilities may carry information of a weak sinusoidal input (amplitude and period).
  - Resonance with the noise strength.
  - In a neuronal ensemble the encoding of the signal is more pronounced.
- Ongoing work: can we recover quantitative information of the signal from the analysis of the ISI sequences?
- Future work: Aperiodic signals? Comparison with laser arrays?

# Other problems in which I have used ordinal analysis

- Climate data analysis: identification of interactions acting in different time-scales (Chaos 2011).
- Ordinal networks: identify transitions between different regimes (New J. Phys 2015, Chaos 2018).



**THANK YOU FOR YOUR ATTENTION !**

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<http://www.fisica.edu.uy/~cris/>

***Emergence of spike correlations in periodically forced excitable systems***

J. A. Reinoso, M. C. Torrent and C. Masoller, PRE 94, 032218 (2016).

***Neuronal coupling benefits the encoding of weak periodic signals in symbolic spike patterns***

M. Masoliver, C. Masoller,

Commun. Nonlinear Sci. Numer. Simulat. 88, 105023 (2020).

