

## **WP4: Neural Inspired Information Processing**

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**NETT Fellows' Induction** Nottingham, UK, April 2013





# Two fellows in WP4: ESR 9 & ESR 10

- ESR9 (to be recruited) will develop semiconductor laser networks that mimic the information processing capabilities of small neuronal networks.
- To be recruited may 2013
- Supervised by C. Masoller, M. C. Torrent and J. Garcia Ojalvo

- ESR10 (Maciej Jedynak) will model at a mesoscopic level neuronal activity.
- Supervised by A. Pons and J. Garcia Ojalvo
- A focus of the study will be the effect of noise and the relation with coordination malfunctions that modify normal patterns of synchronized behaviour, which in turn lead to neurological disorders.





- ESR 9: From neuronal to photonic networks and back
  - Internship: Cairn
  - Secondments: CNR or UNOTT
- ESR 10: Stochastic effects in neuronal tissue at the mesoscopic level
  - Internship: INRIA
  - Secondments: CNR





### ESR9

- Relating structural coupling with dynamical correlation in laser networks (Deliverable number 9.1, Month 30)
- Information processing capabilities in lasers and neuronal networks (9.2, M48)

### ESR10

- Understanding sources of noise in neural mass models (10.1, M10)
- Ordering effects of random fluctuations at the mesoscopic level (10.2 M36)





## ESR 9 time table and work plan

- Characterize semiconductor lasers (SCLs) as optical neurons (first and second year)
- Coupled lasers: neuro-inspired laser networks (3<sup>rd</sup> year)
- Characterization of optical spikes and comparison with neuronal spikes via symbolic ordinal analysis.
- Relating coupling directionality with dynamical correlation in laser networks via symbolic ordinal analysis (9.1, M30)
- Quantifying information transmission (via a small modulation of the laser pump current) in coupled lasers (9.2, M48)
- Explore the road back to neuronal networks





- Experimental and numerical work will be carried out at the semiconductor laser laboratory in Terrassa, Barcelona
- In collaboration with Andres Aragoneses, PhD student finishing his third year.







## **Semiconductor lasers lab**









- Why semiconductor lasers?
- Coupling schemes
- Method of analysis: ordinal patterns
- On going and future work
- Concluding remarks





## **Semiconductor lasers**

- Semiconductor lasers are compact, reliable and inexpensive.
- Mainly used for fiber optics communications and optical data storage (CDs, DVDs).
- Also in printers, bar-code scanners, sensors, etc.
- Recent developments include Green and Blue lasers for applications in the life sciences (optogenetics, biomedical imaging, etc).









**Semiconductor lasers** 

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- "solitary" (free-running) semiconductor lasers emit a stable output intensity.
- Under optical feedback (self coupling) or with optical coupling (to another laser) these lasers display various types of dynamical outputs, that can resemble neuronal spikes.



 A range of coupling schemes provides access to different types of dynamical outputs.





## **Coupling schemes**





Optical Injection





Optical Feedback

 $x(t\text{-}\tau) \to x$ 



Two SCLs mutually coupled

 $x_1 \leftrightarrow x_2$ 

Orthogonal coupling





Orthogonal feedback

 $y(t-\tau) \to x$ 



 $\begin{array}{c} y_1 \rightarrow x_2 \\ y_2 \rightarrow x_1 \end{array}$ 

(Adapted from A. Gavrielides, AFOSR, US)



## Two types of dynamical output

 With *coherent* optical feedback or coupling: spikes



 With *orthogonal* feedback or coupling: switching







## And also more complex behaviours

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Prof. Coombes' presentation: Complexity, the NETT glue





## **Optical spikes**



These setups induce a similar type of spiking optical output





# The spike rate can be controlled by the laser parameters



This dynamics is explained by a simple laser model (stochastic delay differential rate equations)

Laser output for increasing pump current (adapted from J. Tiana PhD thesis, UPC 2011)





## **Optical spikes: excitability**





## Optical spikes: coherence and stochastic resonance



FIG. 1. Temporal behavior of the laser intensity for increasing input noise amplitude. From top to bottom: noise = -60.8 dBm/MHz (a), -52.5 dBm/MHz (b), and -44.3 dBm/MHz (c). The horizontal scale is 100 ns/div. The vertical scale is the same for the three plots.

#### Giacomelli et al, PRL 2000





FIG. 1. Time traces of the laser output for a fixed noise level  $(-60.8 \text{ dBm V MHz}^{-1/2})$  and forcing frequency 0.4 MHz (a), 1.1 MHz (b), and 1.8 MHz (c). The vertical scale is the same for the three plots.

#### Marino et al, PRL 2002



## Optical spikes: bistability or noisesustained transient dynamics

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Weak noise

Stronger noise



A. Torcini et al, PRA 74, 063801 (2006)





## Two coupled lasers: lagsynchronization



T. Heil et al, PRL (2001)





J. F. Martinez Avila and J. R. Rios Leite, Opt. Express (2009)



## Towards optical neural networks: three coupled lasers

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I. Fischer et al, PRL 2006



M. W. Lee et al, JOSAB 2006



zero-time-lag synchronization



I. Fischer et al, PRL 2006



## **Clustering in a small laser network**

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C. Martinez, C. Masoller, M. C. Torrent and J. García Ojalvo, EPL 2007



In these configurations (self-feedback or coupling) the laser spiking dynamics results from the interplay of

- Intrinsic nonlinear light-matter interactions
- Internal and external noise (optical, electrical, thermal, mechanical)
- Time-delay effects (light propagation time)

 $\Rightarrow$  We have a stochastic and high-dimensional complex system (the phase space is infinite due to the delay)





- Main problem: we can measure only one "output" variable (the intensity)
- Also a problem: the measure system (photodiode, oscilloscope) has a finite resolution bandwidth that gives low temporal resolution.



I. Fischer et al, PRL 1996

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6





To characterize the underlying dynamics and test for determinism and nonlinearity, the two popular approaches are

- Phase-space reconstruction
  - Time-delay coordinates
  - Derivative coordinates
- Symbolic analysis
  - Phase space partition

They allow for model verification, forecasting, characterization, classification, etc.





- Ordinal analysis is a form of symbolic analysis that was proposed by Bandt and Pompe in 2002 (Phys. Rev. Lett. 88, 174102).
- It has been successfully applied to many complex systems (biological, physics, socio-economics, geoscience, etc)
  - To distinguish stochasticity and determinism
  - To classify dynamical behaviours
  - To quantify complexity
- Suitable for event-level description of dynamical systems (e.g., for the analysis and classification of spike trains)





Symbolic analisys

- We consider a time series {x<sub>1</sub>, x<sub>2</sub>, x<sub>3</sub>, ...} that describes a dynamical system
- The time series is transformed (using an appropriated rule) into a sequence of symbols {s<sub>1</sub>, s<sub>2</sub>, ...}
- Which are taken from an "alphabet" of possible symbols {a<sub>1</sub>, a<sub>2</sub>, ...}





- Next we consider "blocks" of symbols ("patterns" or "words")
- All the possible words form a "dictionary"
- And we can then analyze the "language" of the symbolic dynamics, i.e.,
  - the probabilities of the words,
  - missing/forbidden words,
  - transition probabilities,
  - symbolic information measures (entropy, mutual information, etc).





**Examples** 

 Binary transformation. Consider a time series {x<sub>1</sub>, x<sub>2</sub>, x<sub>3</sub>, ...}. The rule

if  $x_i > x_{th} \Rightarrow s_i = 0$ ; else  $s_i = 1$ 

transforms the time-series into a sequence of 0s and 1s

Ordinal transformation. The rule

if  $x_i > x_{i-1} \Rightarrow s_i = 0$ ; else  $s_i = 1$ 

also transforms the time-series into a sequence of 0s and 1s





# Construction principle of ordinal patterns (OPs) of length D

Computers in Biology and Medicine 42 (2012) 319-327



Classifying cardiac biosignals using ordinal pattern statistics and symbolic dynamics

U. Parlitz<sup>a,b,\*</sup>, S. Berg<sup>c</sup>, S. Luther<sup>a,b,d</sup>, A. Schirdewan<sup>e</sup>, J. Kurths<sup>f,g</sup>, N. Wessel<sup>f</sup>

For D=2 there are only two possible directions from  $x_1$  to  $x_2$ : up (pattern 01) or down (pattern 10)









## For OPs of length D there are D! possible patterns



U. Parlitz et al. / Computers in Biology and Medicine 42 (2012) 319-327



#### D=5





# Ordinal analysis of optical spikes



#### UNIVERSITAT POLITÈCNICA





## Statistics of the inter-dropoutintervals

4000

4



Is there any information in the IDI sequence? (analogy with foreign text as in Prof. Russell's presentation)





## "language" analysis: word probabilities

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PHYSICAL REVIEW E 84, 026202 (2011)

#### Language organization and temporal correlations in the spiking activity of an excitable laser: Experiments and model comparison

Nicolas Rubido,<sup>1</sup> Jordi Tiana-Alsina,<sup>2</sup> M. C. Torrent,<sup>2</sup> Jordi Garcia-Ojalvo,<sup>2</sup> and Cristina Masoller<sup>2</sup>





Consistent with stochastic dynamics at low pumps, but signatures of determinism at higher pump currents





# "language" analysis: transition probabilities

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Consistent with stochastic dynamics at low pumps, but signatures of determinism at higher pump currents





## At low pump currents: inter-dropoutintervals not fully random





A. Aragoneses, et al submitted (2013)



## **Ongoing work: model comparison**

### **Experiments**



### **Simulations**







# Ongoing work: spiking under the influence of a periodic forcing

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### Histogram of inter-dropout-intervals



IDIs (in units of the modulation period)





## Ongoing work: influence of forcing parameters





OP probabilities and transition probabilities depend on the modulation amplitude (A) and frequency (f)





## **Concluding remarks**

- Ordinal analysis is a powerful technique for classifying different types of dynamics.
- It allows inferring signatures of determinism and stochasticity.
- Our goal is to use this tool for
  - characterizing and classifying optical spikes (single unit, coupled units) and
  - comparing with spikes of biological neurons (via ordinal analysis of inter-spike-intervals).
- Potential application: building optical neurons for all-optical ultra-fast neuro-inspired information processing

