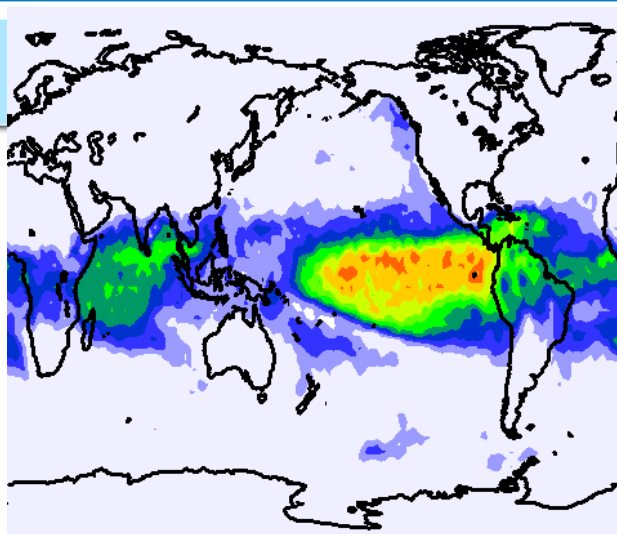




"LINC"

Learning about Interacting Networks in Climate



What have we learned about our climate by using networks and nonlinear analysis tools?

Cristina Masoller

Universitat Politècnica de Catalunya,
Terrassa, Barcelona, Spain
www.fisica.edu.uy/~cris



UNIVERSITAT POLITÈCNICA
DE CATALUNYA
BARCELONATECH

Campus d'Excel·lència Internacional

Analysis of Dynamic Networks and data
driven Modeling of the climate
(DyNeMo-Clim)

Potsdam, October 2015

analysis of **Dynamic**
Networks and
data driven **Modelling** of the
Climate



"LINC"

Learning about Interacting Networks in Climate

Climatelinc.eu

- Call: FP7-PEOPLE-2011-ITN
- December 1st 2011 - November 30th, 2015
- Budget: 3.7 M€
- Goals:
 - To train 15 young researchers (12 PhDs + 3 postdocs) in the complete set of skills needed to undertake a career in physics and geosciences (climatology, complex systems, computer science, data analysis).
 - To develop long-lasting collaborations among the partners.



UNIVERSITAT POLITÈCNICA
DE CATALUNYA
BARCELONATECH

Campus d'Excel·lència Internacional

Partners: 6 academic + 3 companies

Spain, Germany, The Netherlands, Uruguay and Israel



UNIVERSITAT POLITÈCNICA
DE CATALUNYA
BARCELONATECH



IMAU

Institute for Marine and
Atmospheric research Utrecht



FACULTAD DE
CIENCIAS

UDELAR fcien.edu.uy



VORTECH BV
THE SCIENTIFIC SOFTWARE ENGINEERS

climate risk
analysis **mudelsee**

ambrosys



POTSDAM INSTITUTE FOR
CLIMATE IMPACT RESEARCH

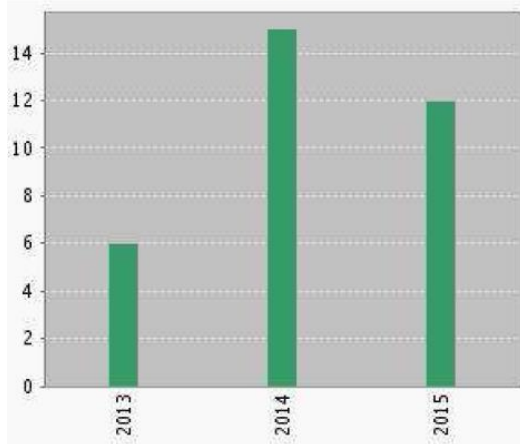


Bar-Ilan University

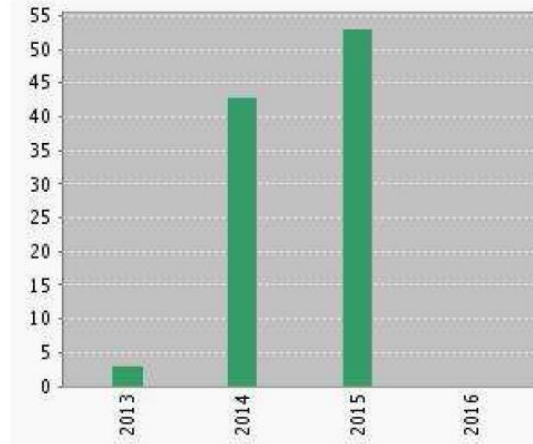


- Interdisciplinary journals (PRL, GRL, Nonlinear Processes in Geophys., Chaos, Entropy, etc.)

Elementos publicados cada año



Citas cada año



- Many available at climatelinc.eu
- 5 PhD theses completed, several are scheduled for the next months.
- Software and database also available in our web page.

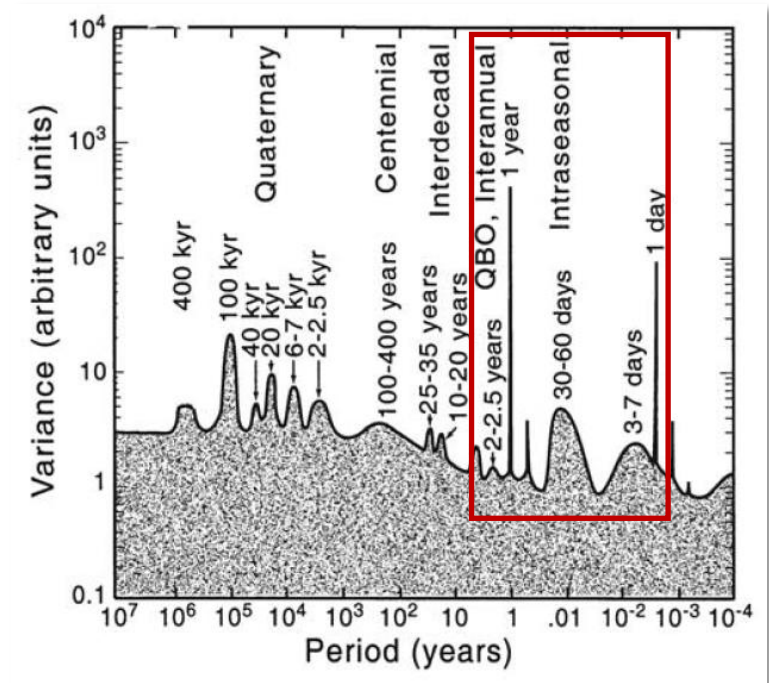


- First school (Mallorca, Spain, September 2012)
- Second school and Workshop 1 (The Netherlands, April 2013)
- Workshop 2 (Potsdam, November 2013)
- Workshop 3 (Montevideo, Uruguay, April 2014)
- Workshop 4 (Lucca, Italy, Sep. 2014 co-located with ECCS)
- Final Conference (Viena, April 2015, co-located with EGU)



- Introduction to nonlinear tools for climate data analysis (motivation and methodology)
- Results
- Summary
- Ongoing and future work

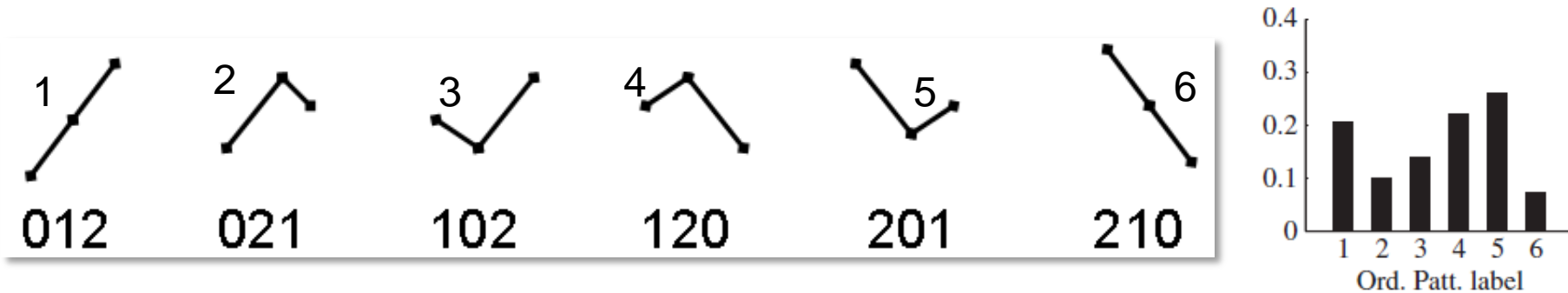
- Improving our understanding of climate dynamics requires the identification of recurrent patterns and their underlying causes.
- Wide range of time-scales.
- Methods of data analysis remain dominated by linear thinking (e.g., extrapolation of trends).
- Nonlinear thinking is important (e.g., for identifying precursors of extreme events and regime shifts).



Method of time-series analysis: ordinal patterns

■ $X = \{\dots x_i, x_{i+1}, x_{i+2}, \dots\}$

Brandt & Pompe, PRL 88, 174102 (2002)



The OP probabilities allow to identify frequent patterns in the ordering of the data points

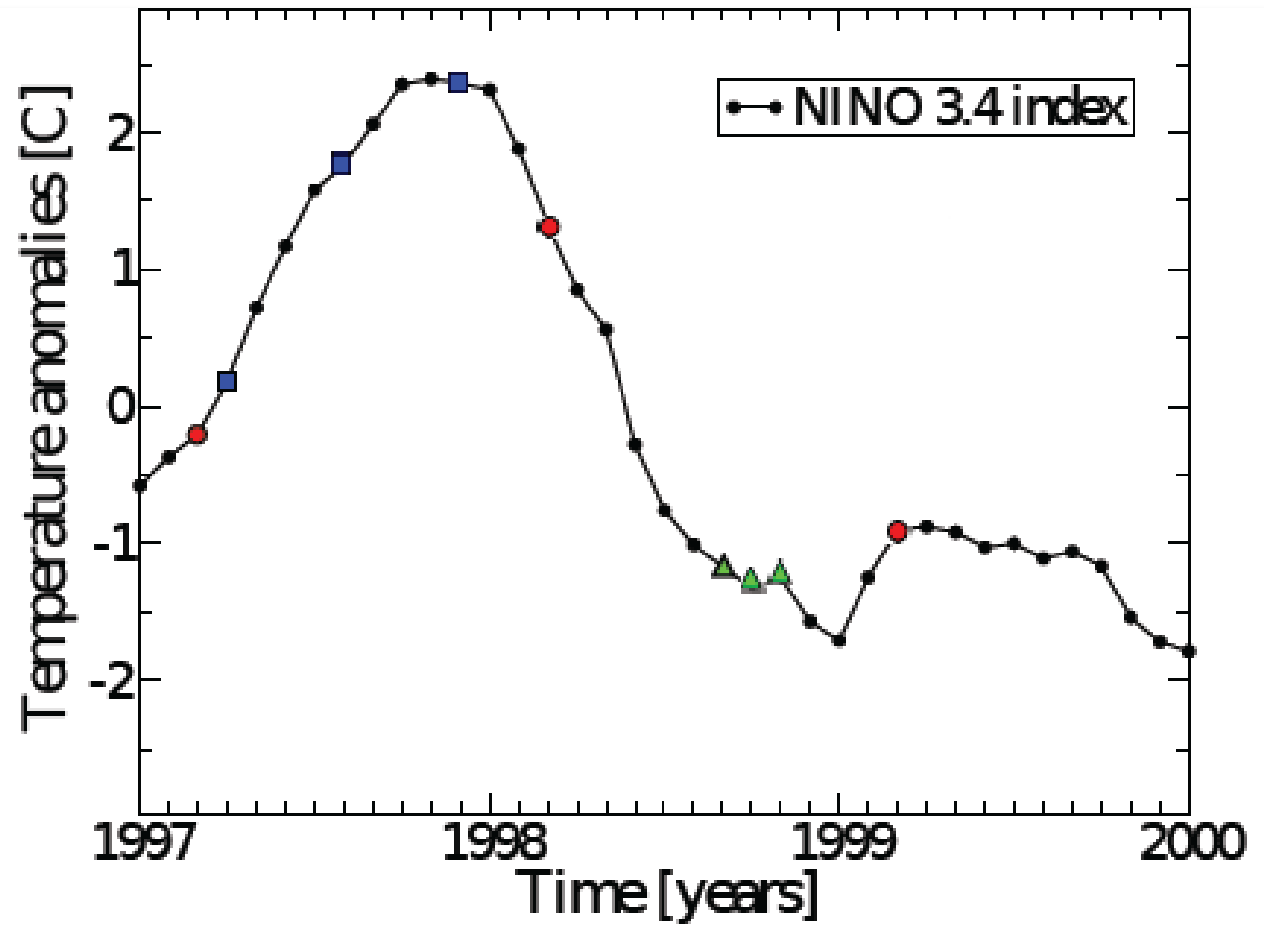
- Drawback: the *values* of the data points are not considered.
- Advantages:
 - We take into account temporal correlations.
 - We can select specific time-scales.

**Intra-
season 102**

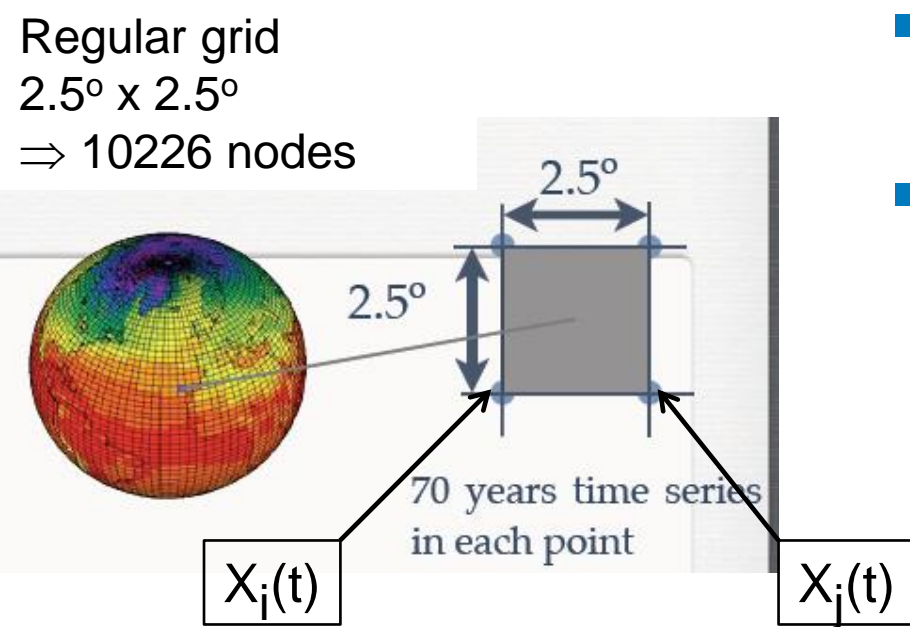
**Intra-
annual 012**

**Inter-
annual 120**

■ Monthly data



Climate networks: construction and visualization



- Data: monthly SAT **anomalies**
NCEP/NCAR reanalysis
- Similarity measure: mutual information

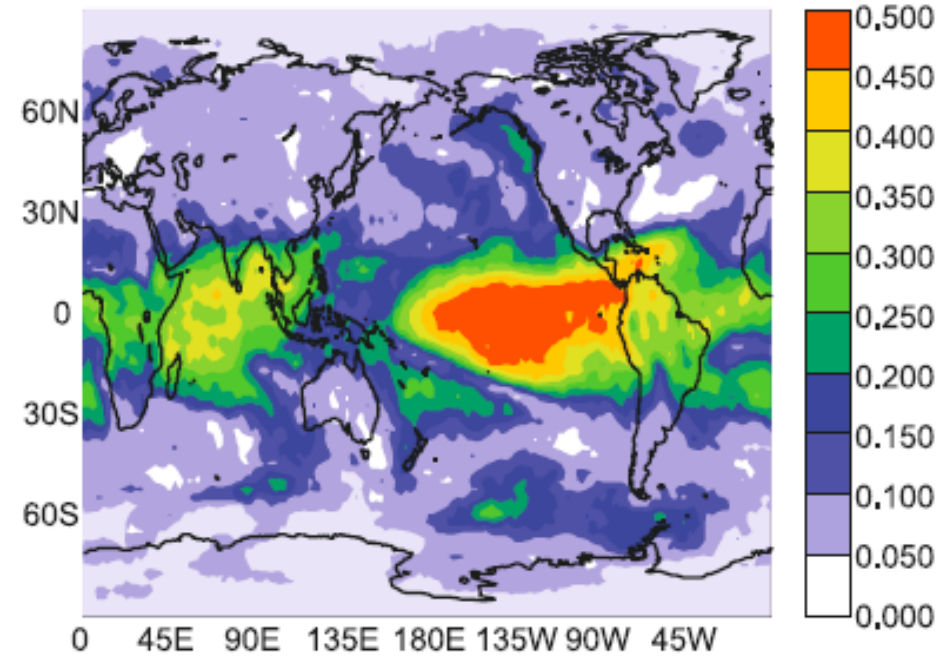
$$M_{ij} = \sum_{m,n} p_{ij}(m,n) \log \frac{p_{ij}(m,n)}{p_i(m)p_j(n)}$$

- Visualization: area weighted connectivity (weighted degree)

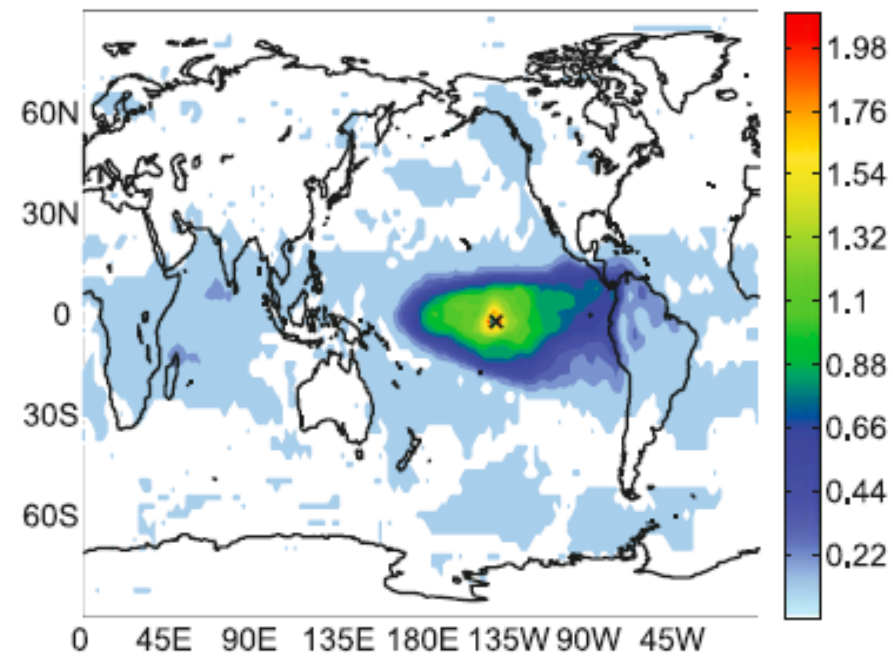
$$AWC_i = \frac{\sum_j^N A_{ij} \cos(\lambda_j)}{\sum_j^N \cos(\lambda_j)}$$

Results: inter-annual OPs (3 consecutive years)

AWC

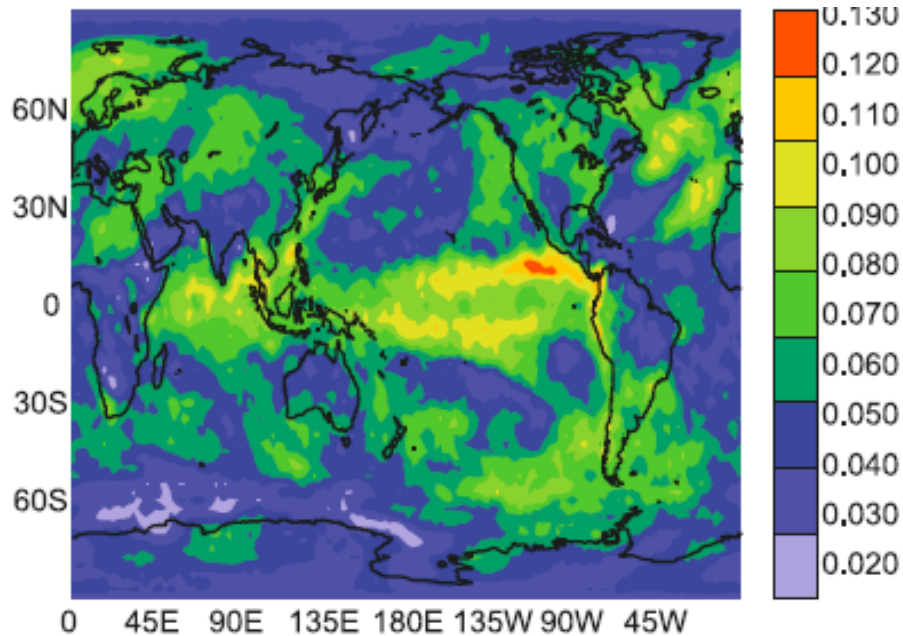


Links of a node in Central Pacific

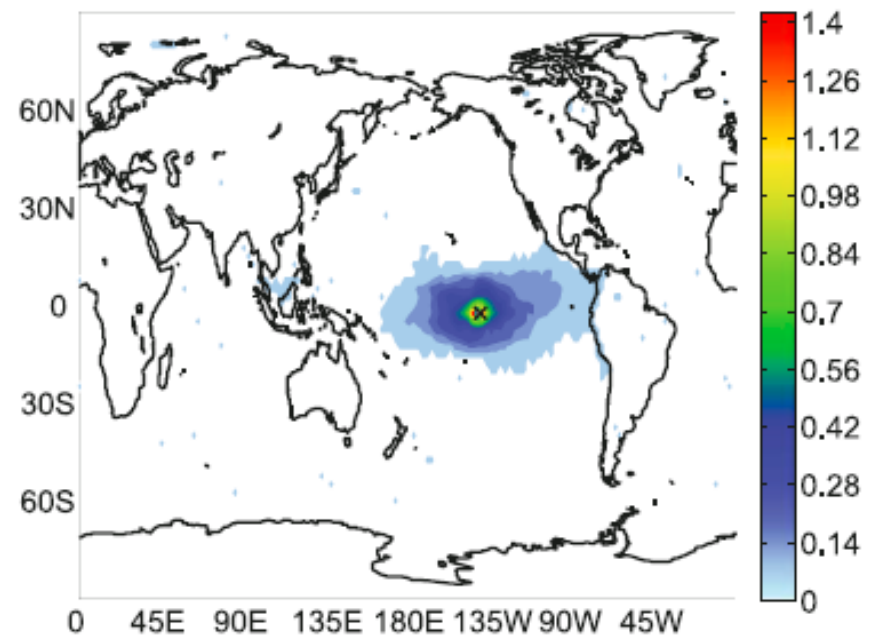


Intra-season (3 consecutive months)

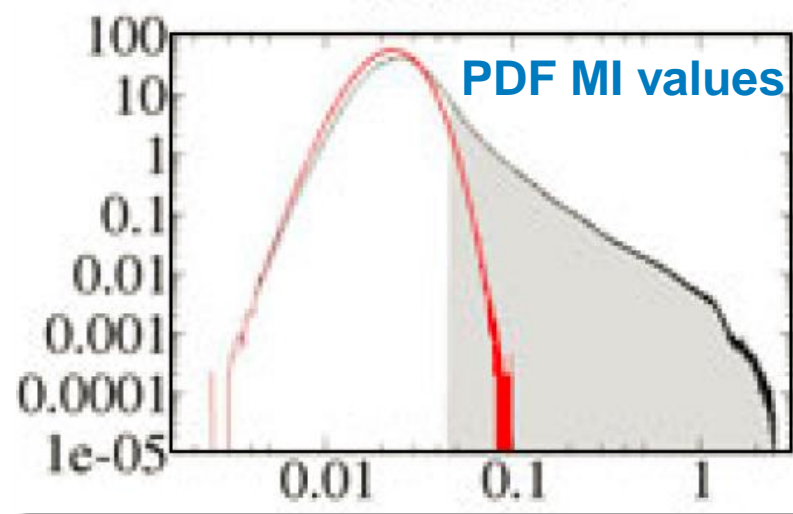
AWC



Links of a node in Central Pacific

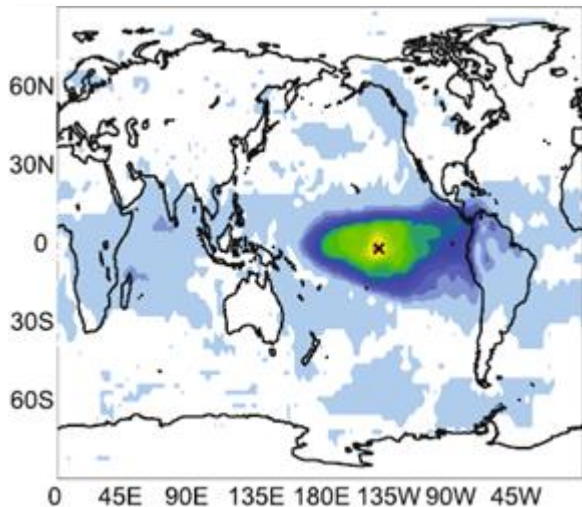


Significance test

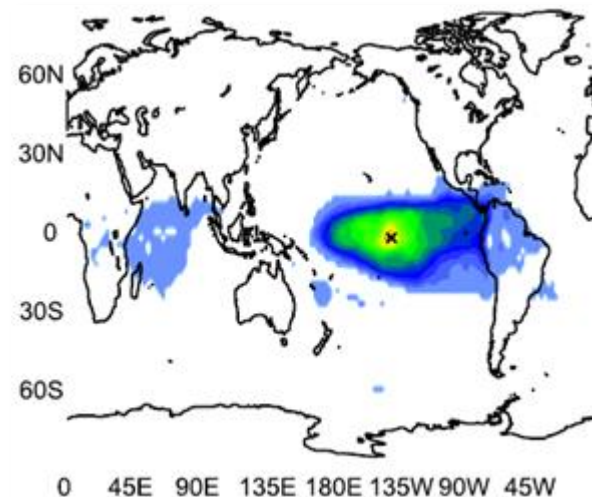


Surrogated data
Original data

Low threshold



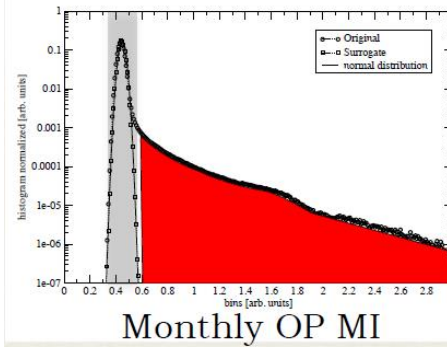
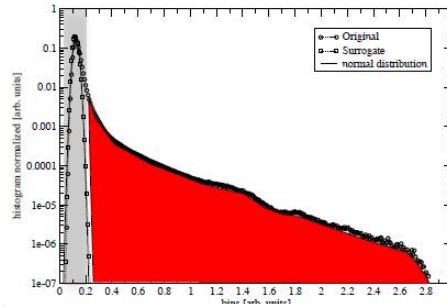
Higher threshold



Network comparison

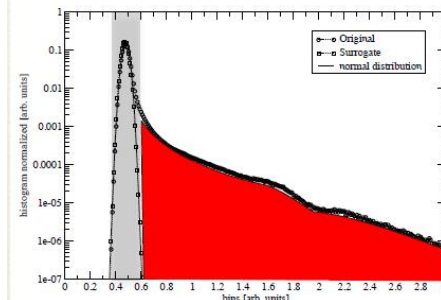
■ MIH

■ Intra-season (4 months)

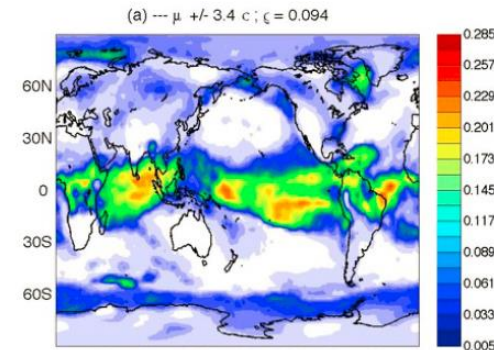


Monthly OP MI

■ Inter-annual (4 years)

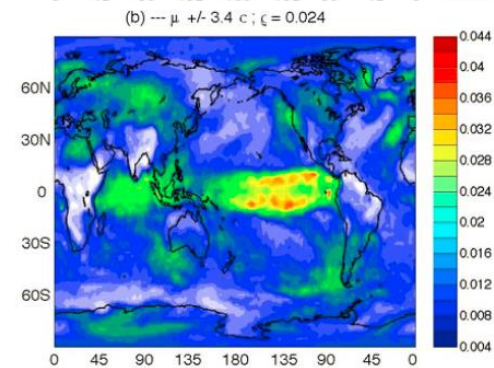


Yearly OP MI

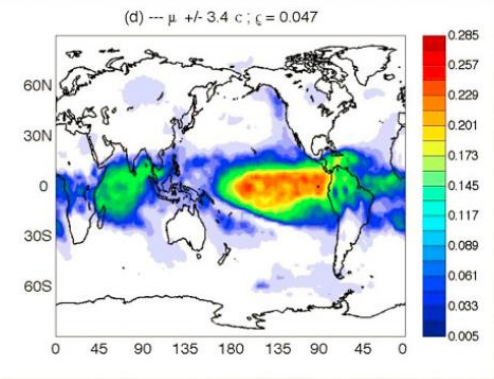


Link density

0.094



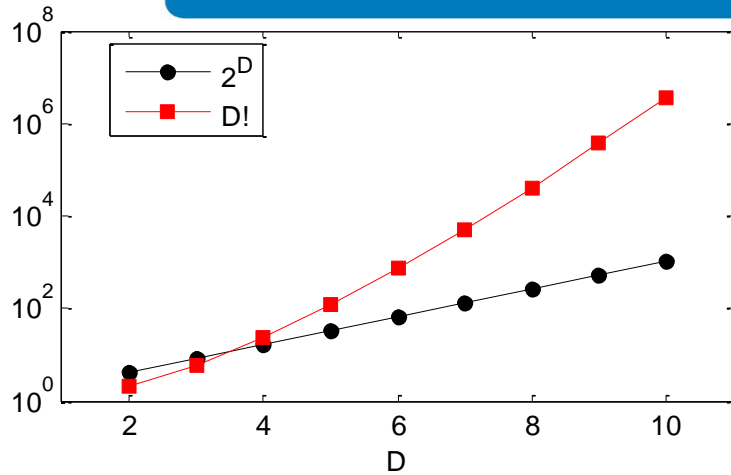
0.024



0.047

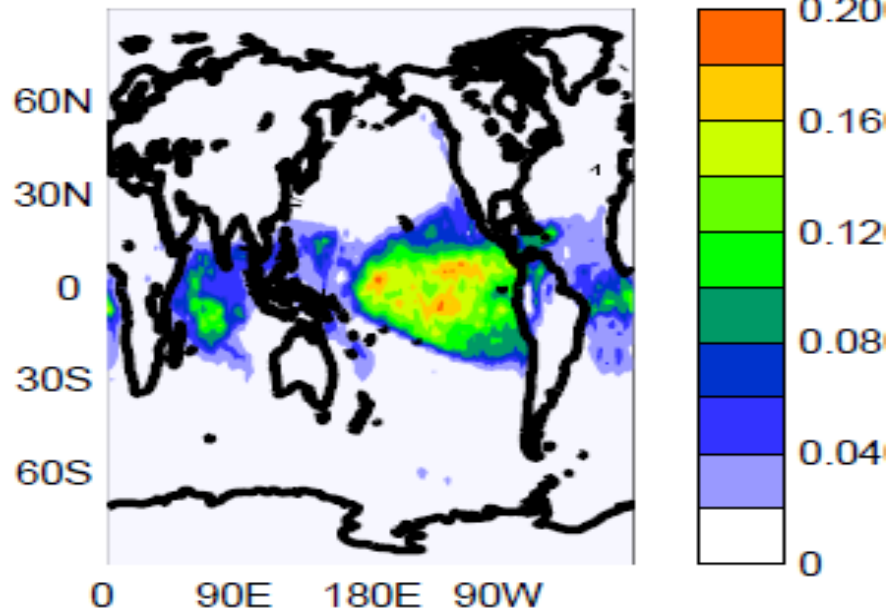
Longer time intervals: binary representation

$$X = \{\dots X_i, X_{i+1}, \dots, X_{i+D}, \dots\}$$



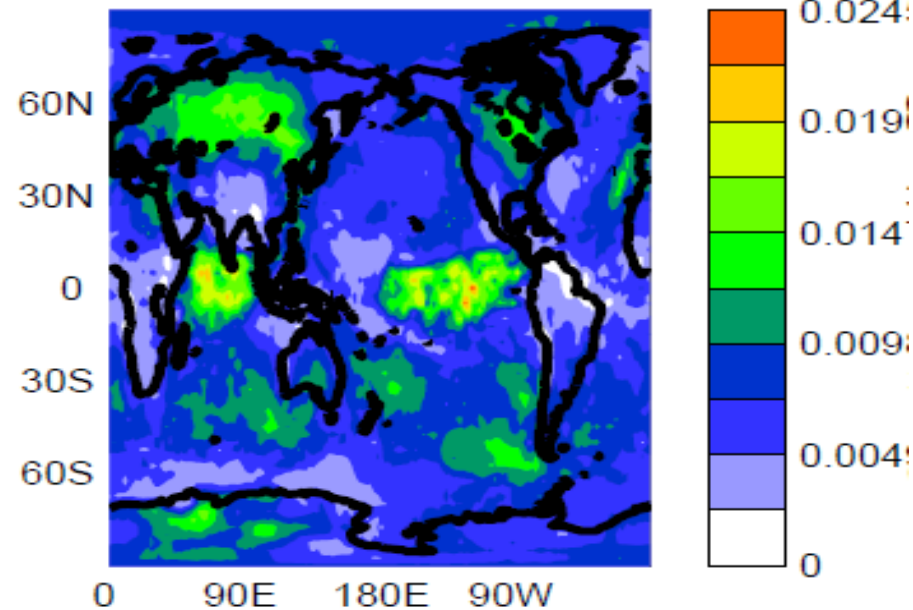
5 consecutive years

$\tau = 0$ $\rho = 0.021$

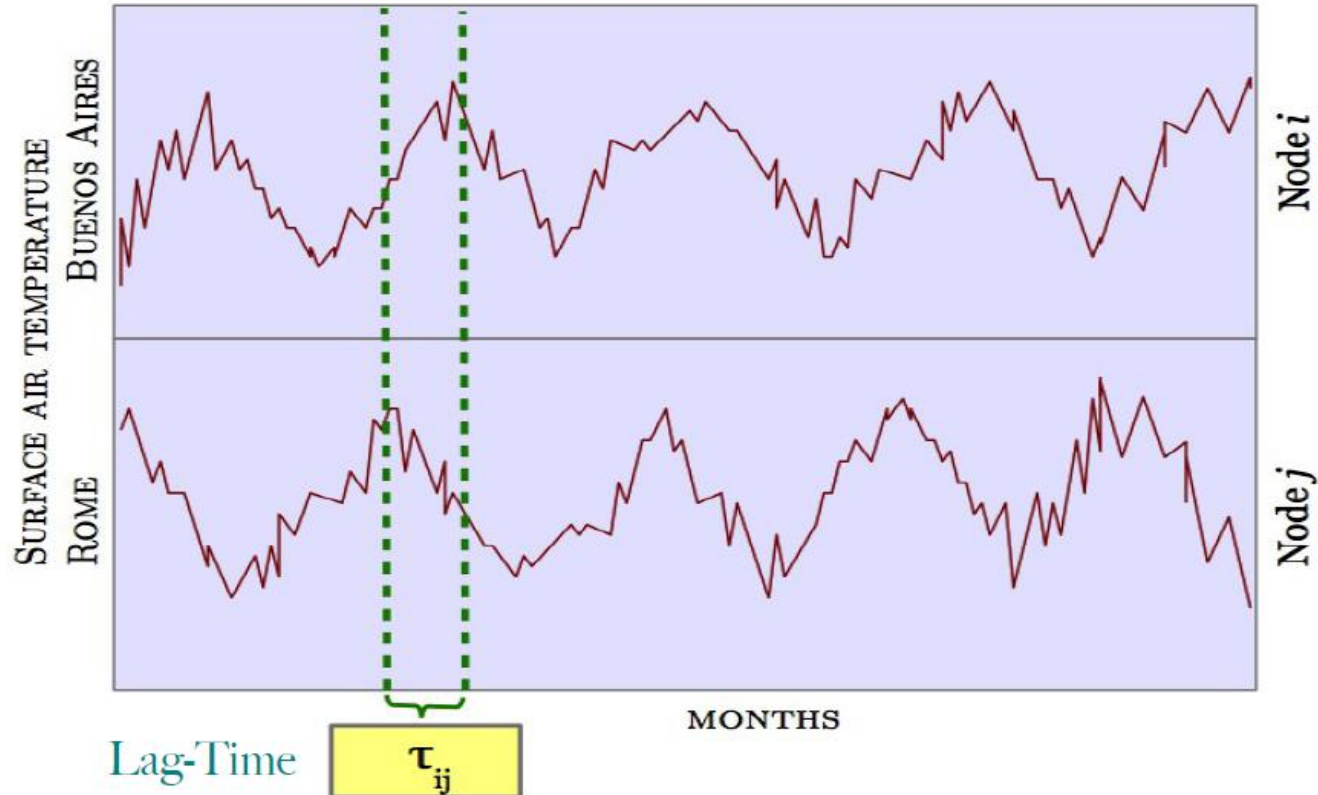


5 consecutive months

$\tau = 0$ $\rho = 0.012$



Question: can the connectivity increase if the annual cycles are synchronized?



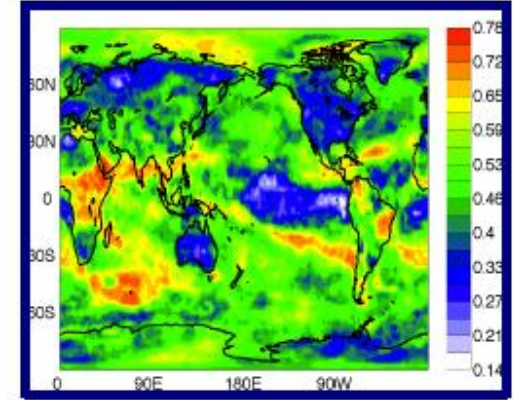
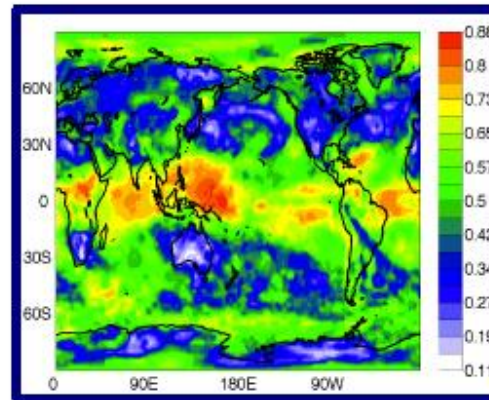
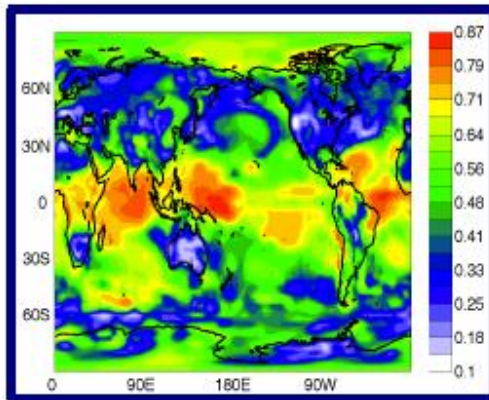
AWC with 50% strongest links

CC

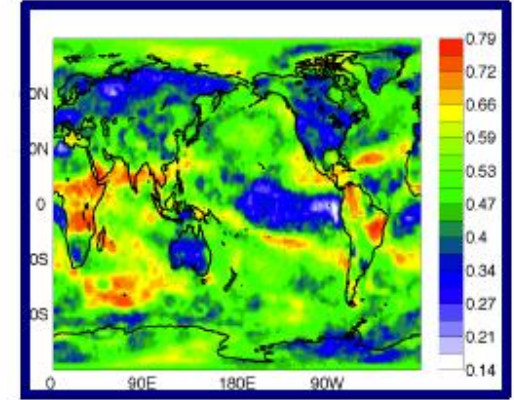
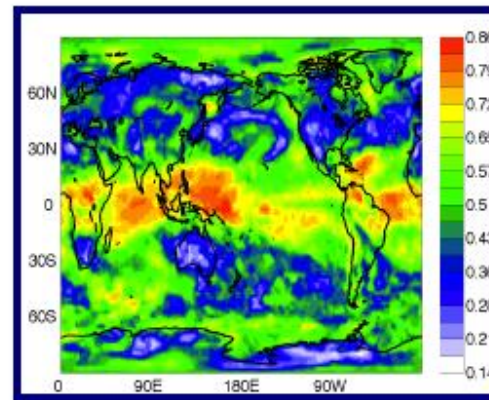
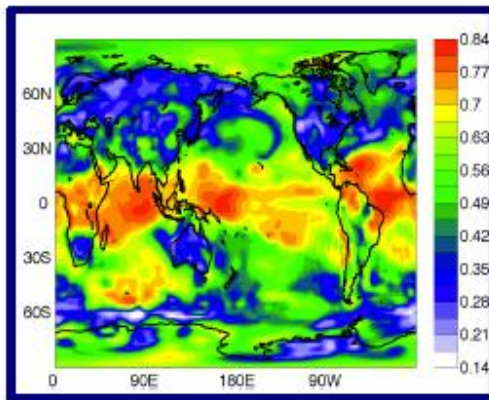
MI

MIOP

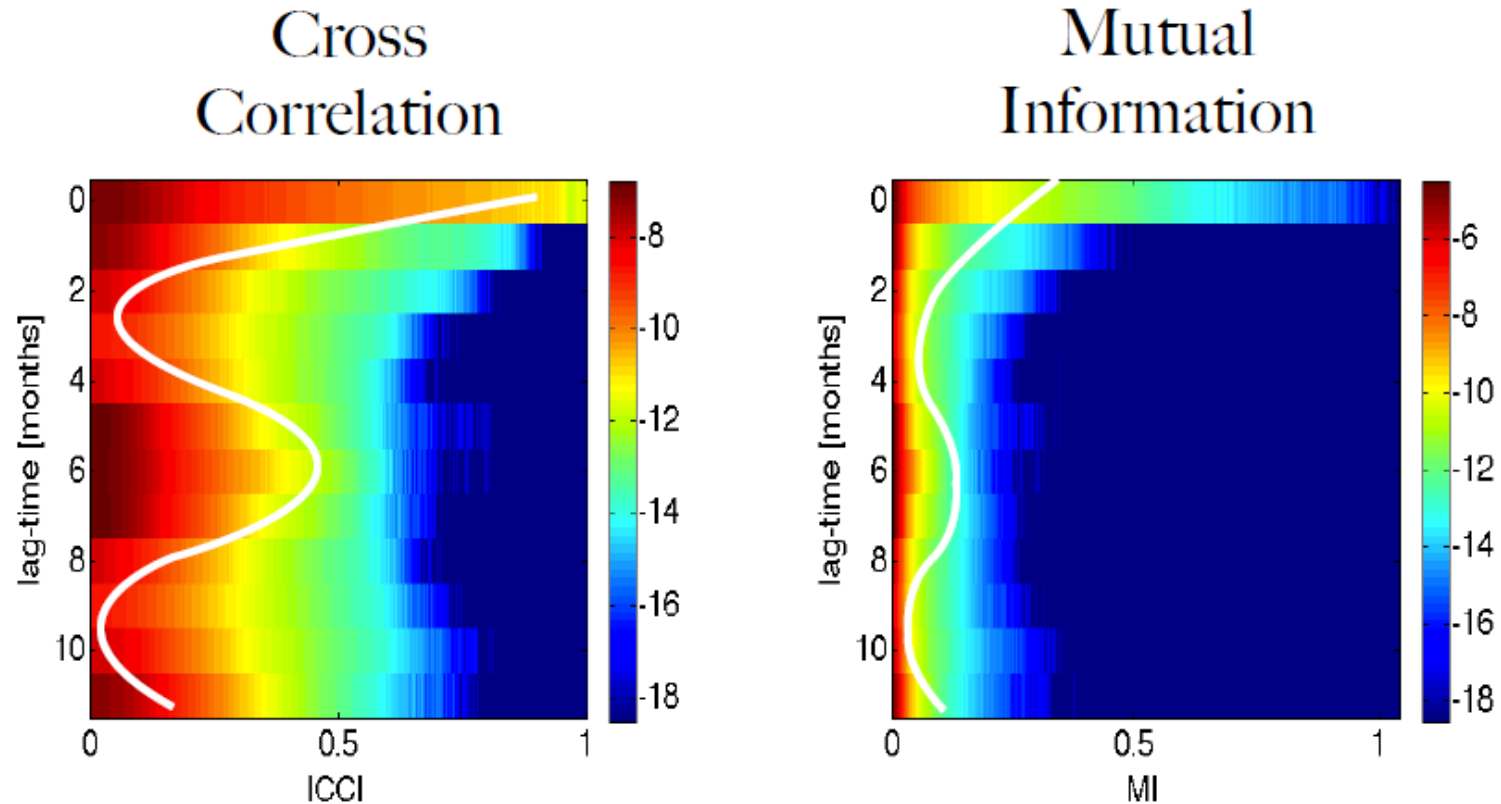
Lag



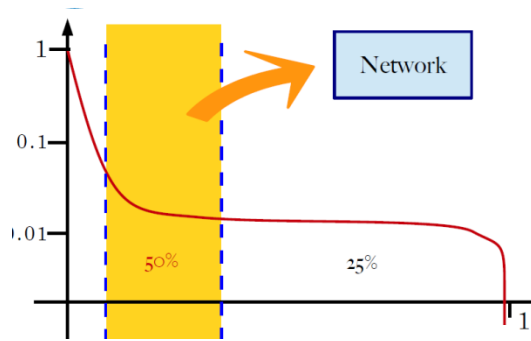
No
Lag



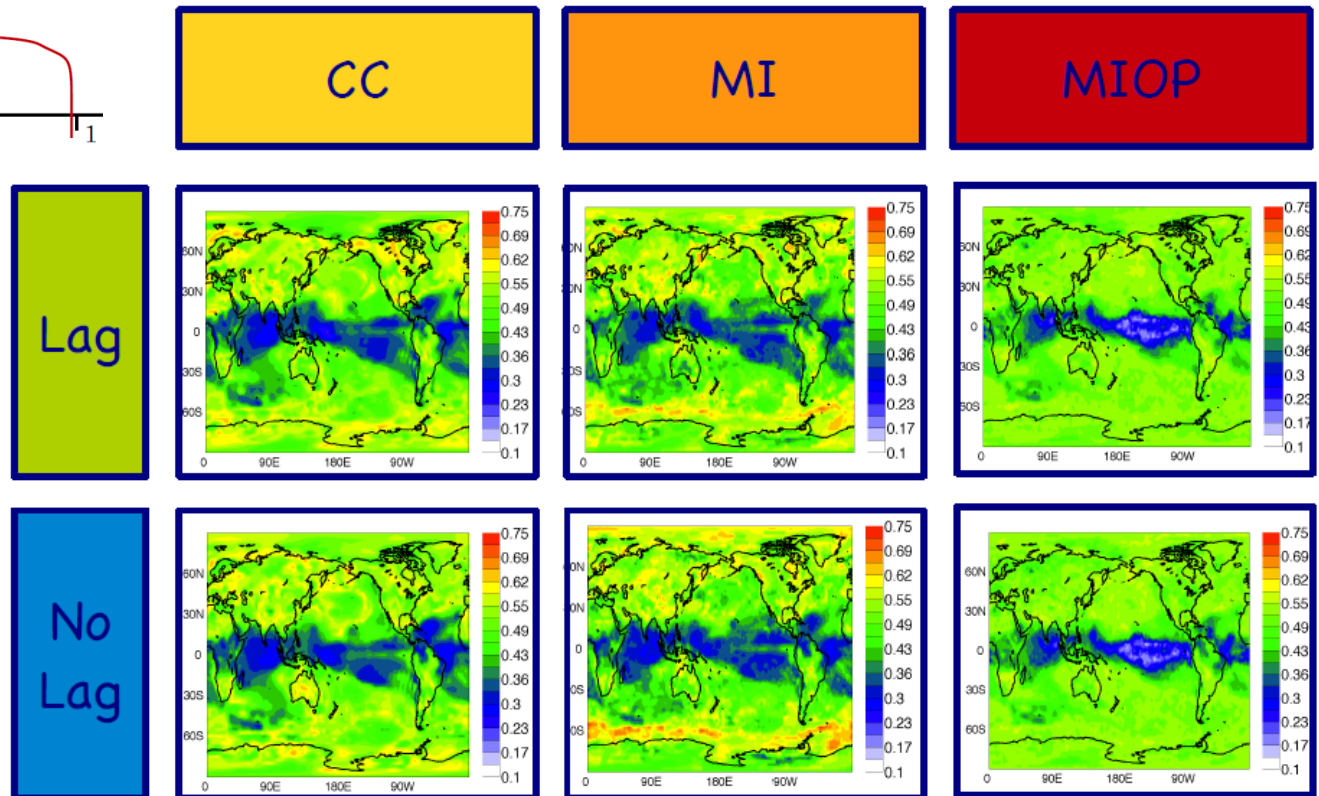
Links: distribution of strengths and lag-times



Strongest links have lag-time = 0;
most of the links with non-zero lags are weak

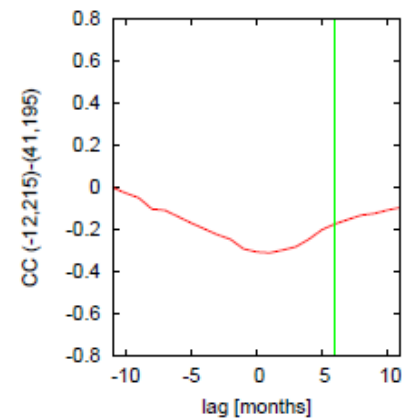
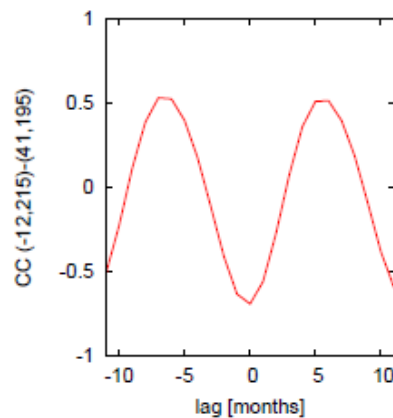
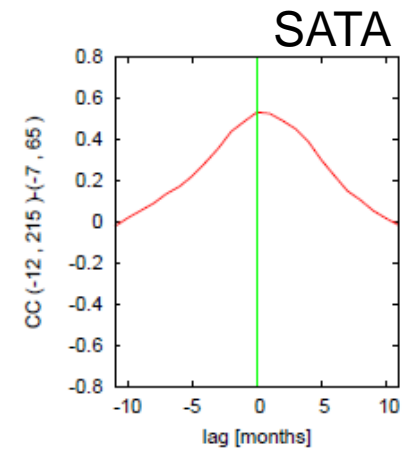
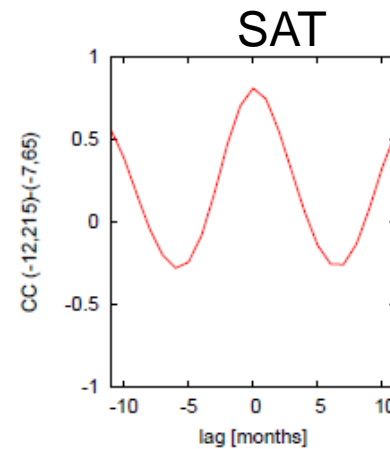
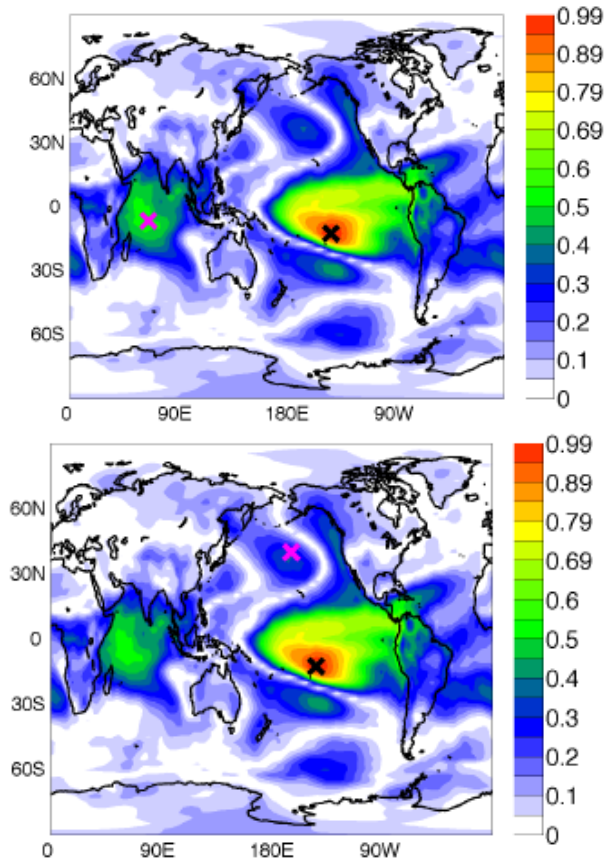


AWC density 50%, the strongest and the weakest links are removed



Why there is no effect?

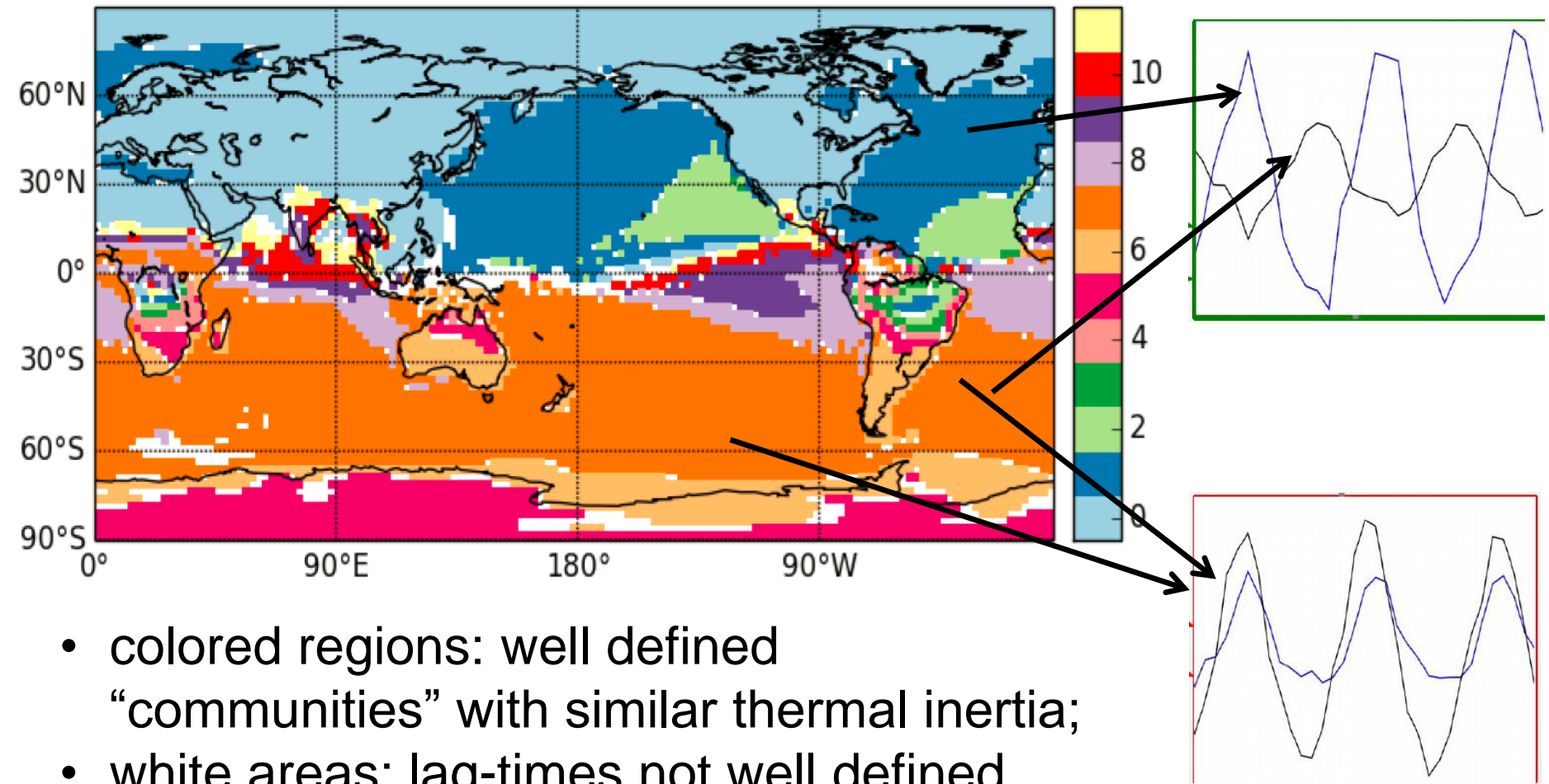
$$C_{ij}(\tau) = \sum_{t=1}^N x_i(t + \tau) x_j(t)$$



Links with non-zero lags: the time-shifting changes their weight.
But, these changes appear to be random \Rightarrow effects are washed out in the AWC.

Lag-times useful to identify regions with in-phase cycles

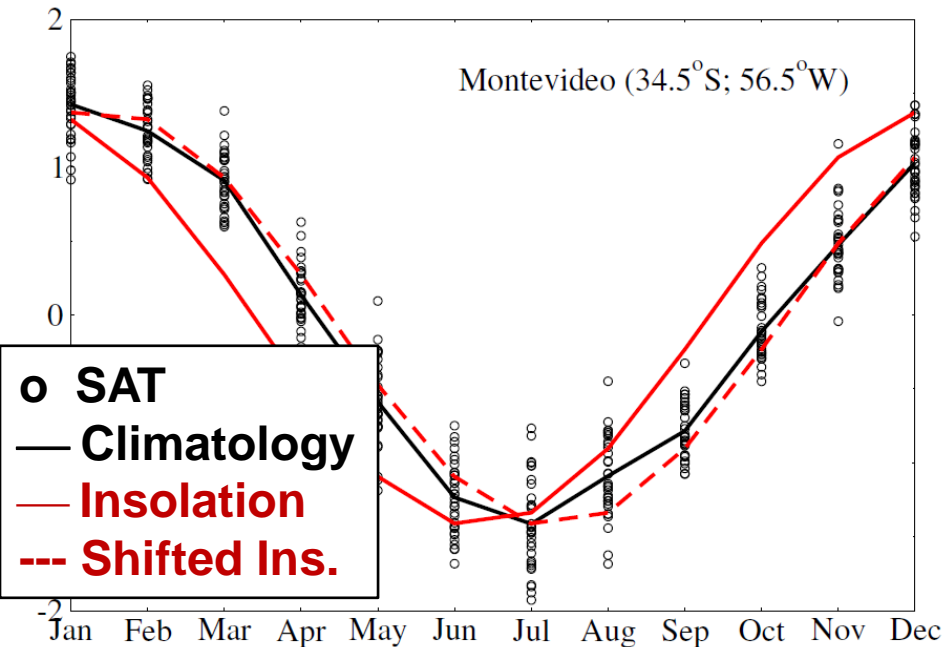
$$\ell_{ij} = (\ell_{ik} + \ell_{kj}) \bmod 12$$



To further understand the role of annual solar forcing

- where are the regions with strongest nonlinear climate?
- where are the regions where the climate is more stochastic?
- A first step: univariate analysis of monthly **SAT data** and **SAT anomalies** to quantify atmospheric nonlinearity and stochasticity.

Quantifying atmospheric nonlinearity and stochasticity

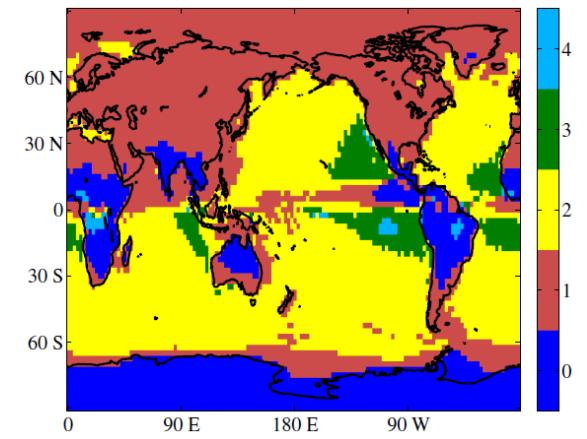
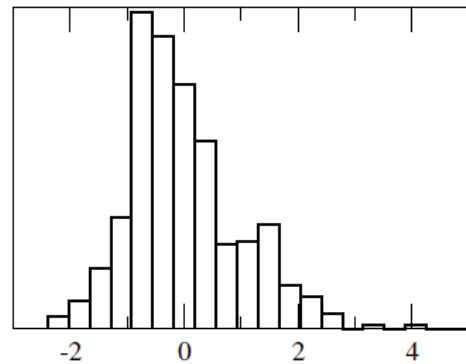


$$D_i(\varphi_i) = \frac{1}{T} \sum_{t=1}^T |x_i(t) - I_i(t + \varphi_i)|$$

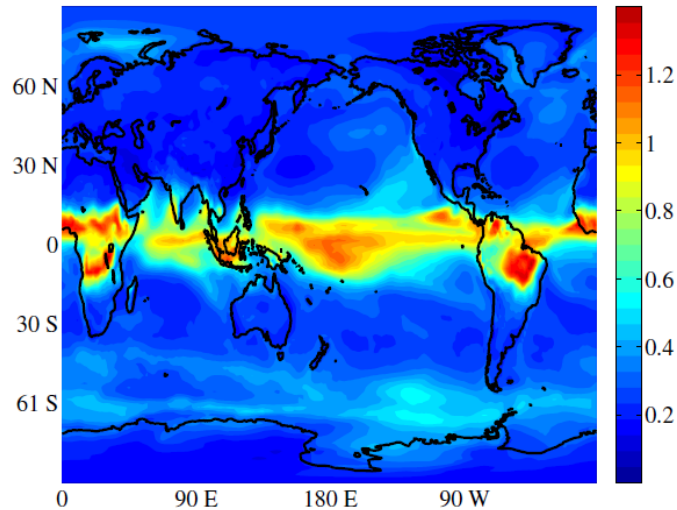
I_i = insolation at node i (top-of-atmosphere incoming solar radiation)
 x_i = climatology at node i
 x_i and I_i are both normalized to zero mean and $\sigma=1$.

φ_i = in [0-4 months] minimizes D_i .

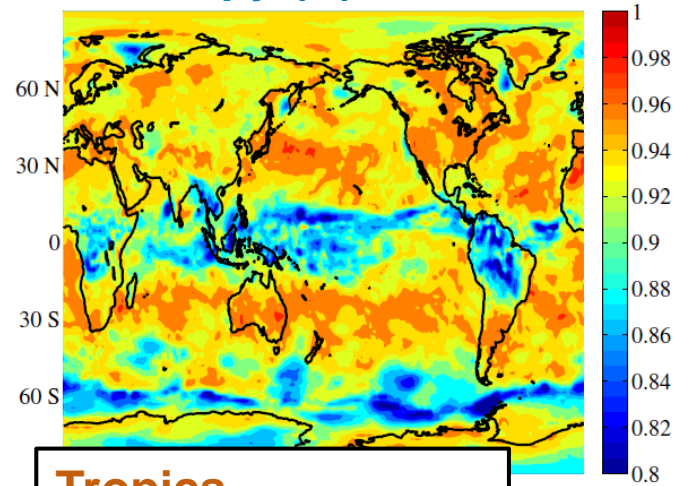
The entropy is computed from the PDF of SAT anomalies



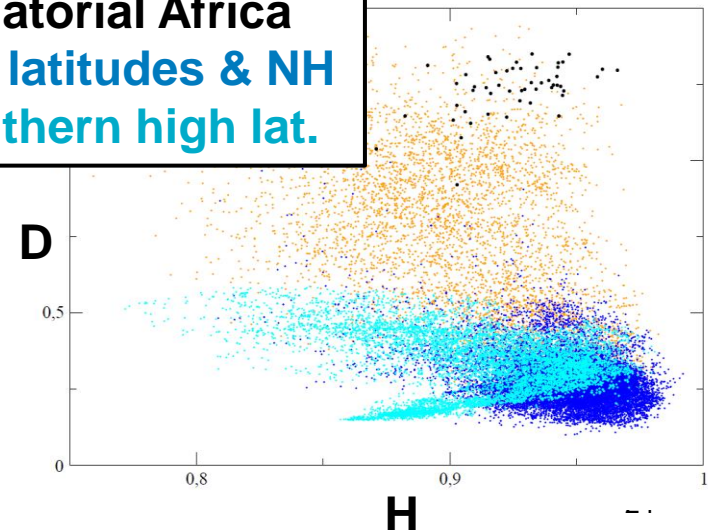
Nonlinear measure (D)



Entropy (H)



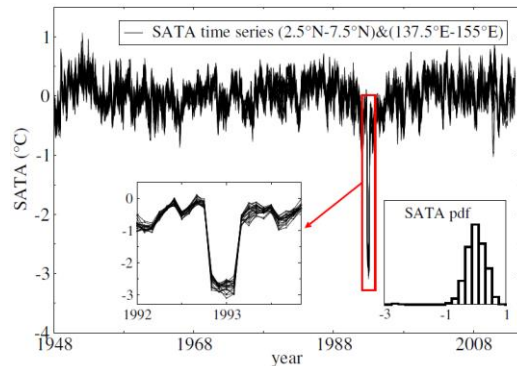
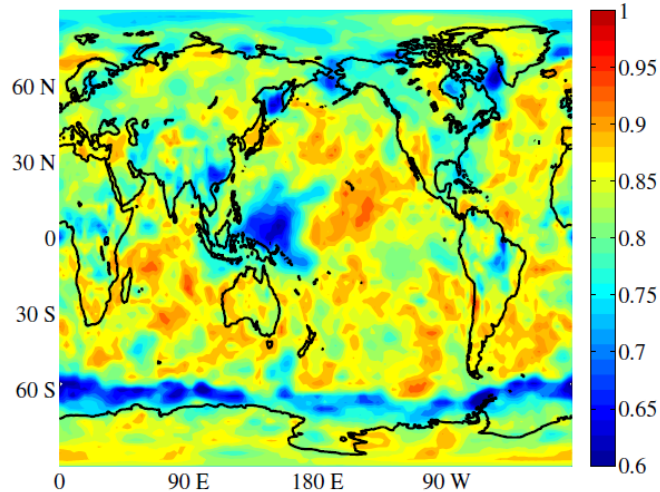
Tropics
Equatorial Africa
Mid latitudes & NH
Southern high lat.



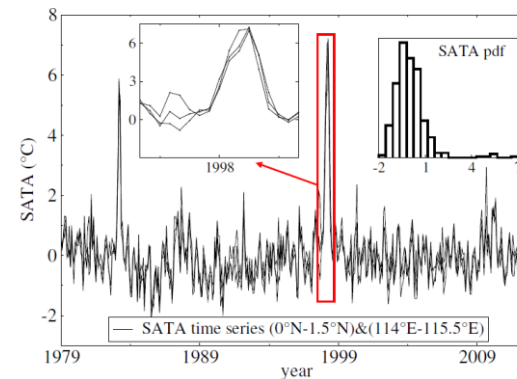
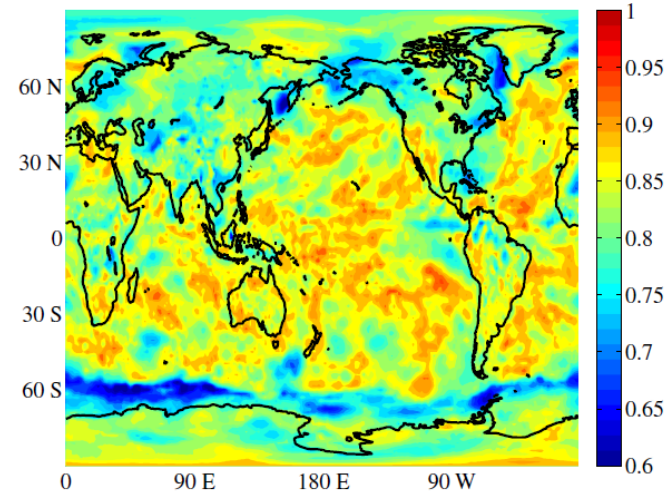
- Regions with high nonlinearity: tropics.
- Extratropics: high entropy & low nonlinearity

Dataset comparison

NCEP CDAS1



ERA Interim



In both cases, the extreme values do not appear in the other dataset

Identifying regions with similar climate

- Goal: to construct a network in which regions with similar climate (e.g., continental) are in the same “community”.
- “Usual” way not doable: NH and SH are indirectly connected.

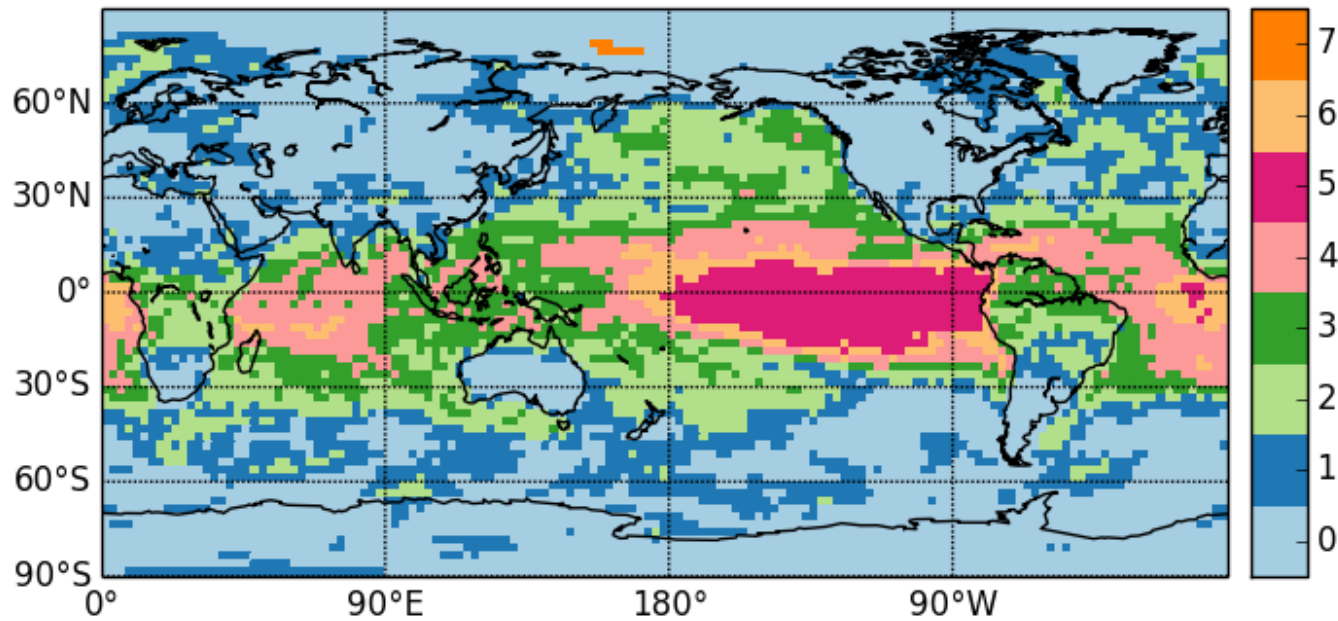
- Step 1: transform SAT anomalies in each node in a sequence of ordinal patterns

$$s_i = \{012, 102, 210, 012, \dots\} \quad s_j = \{201, 210, 210, 012, \dots\}$$

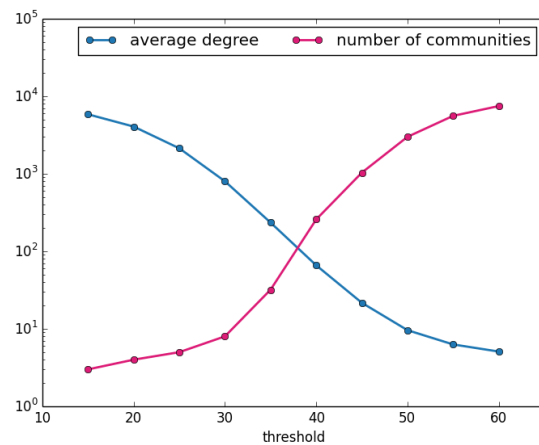
- Step 2: compute transition probabilities

$$TP_{\alpha\beta}^i = \#(\alpha \rightarrow \beta) / N$$

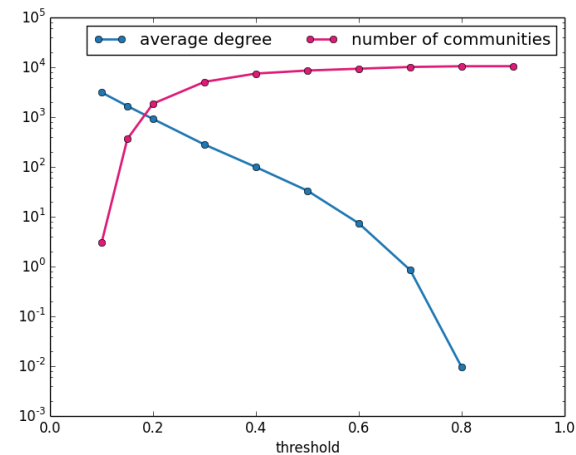
- Step 3: define the weights $w_{ij} = \frac{1}{\sum_{\alpha\beta} (TP_{\alpha\beta}^i - TP_{\alpha\beta}^j)^2}$
- Step 4: threshold w_{ij} to obtain the adjacency matrix.
- Step 5: run a community detection algorithm.



TP Network



CC Network

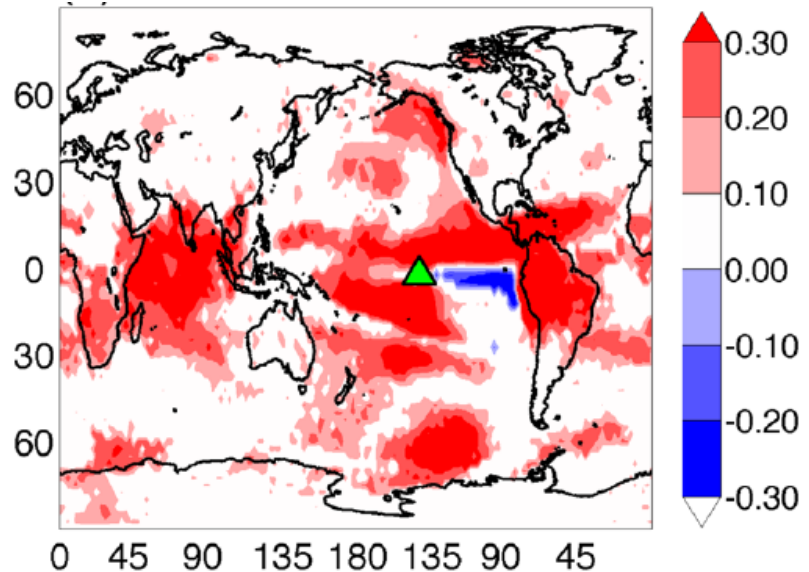
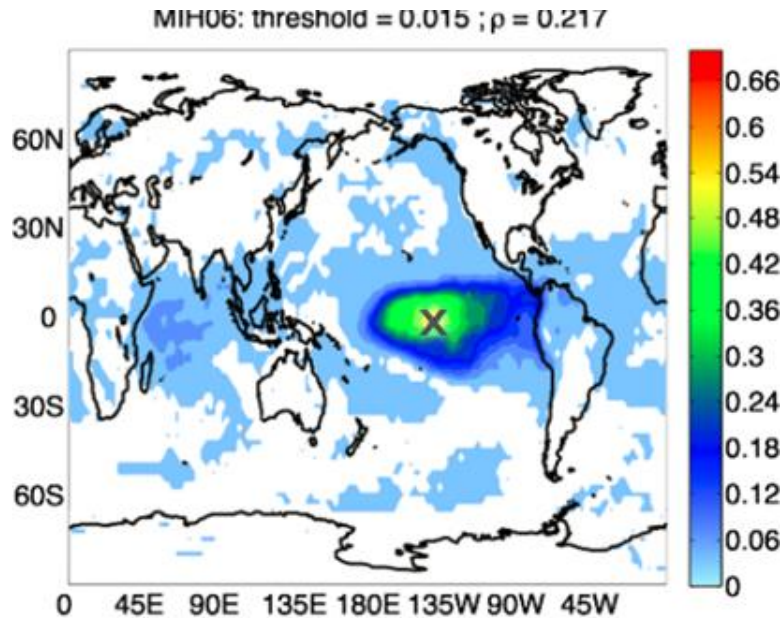


Link directionality

$$D_{XY}(\tau) = \frac{I_{XY}(\tau) - I_{YX}(\tau)}{I_{XY}(\tau) + I_{YX}(\tau)}$$

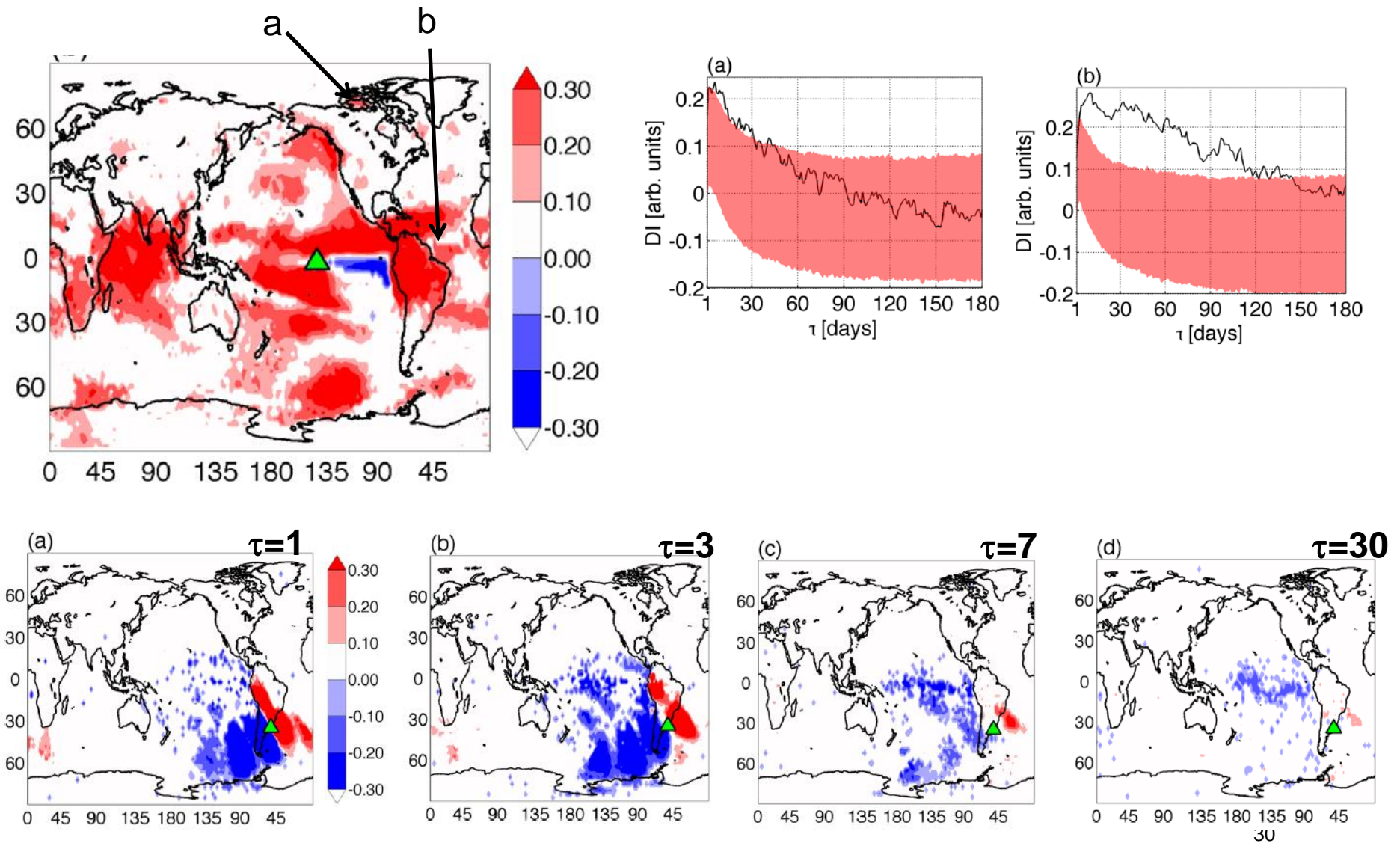
(Prof. Palus' talk)

- $I_{xy}(\tau)$: *conditional* mutual information
- τ : *time-scale* of information transfer
- D : *net direction* of information transfer



Computed from daily SAT anomalies, PDFs estimated from histograms of values. MI and DI are both significant ($>3\sigma$, bootstrap surrogates), $\tau=30$ days.

Time-scale of interactions



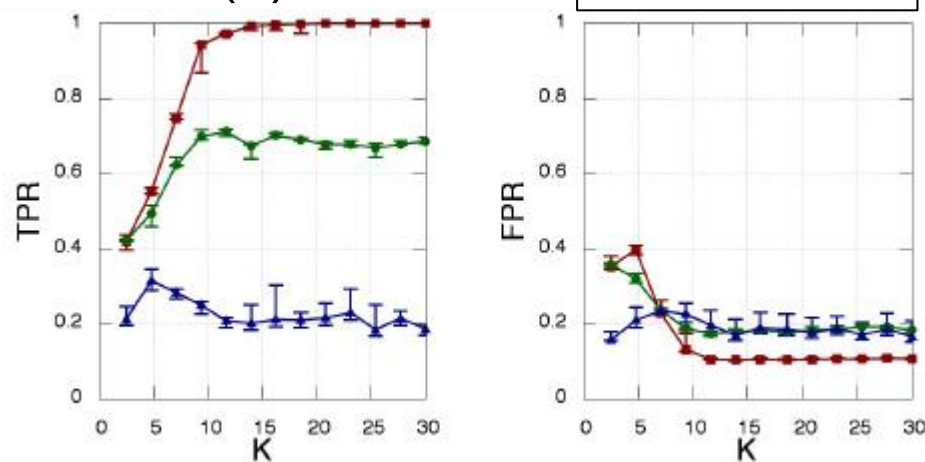
Contrasting structural and functional connectivity

Goal: to test the method of network inference on Kuramoto oscillators with known coupling topology (A_{ij})

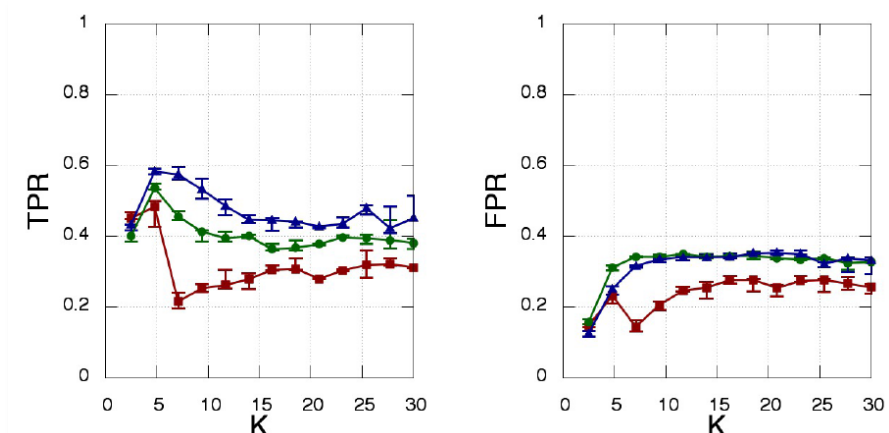
$$d\theta_i = \omega_i dt + \frac{K}{N} \sum_{j=1}^N A_{ij} \sin(\theta_j - \theta_i) dt + D dW_t^i$$

N=12 time-series with 10^4 data points

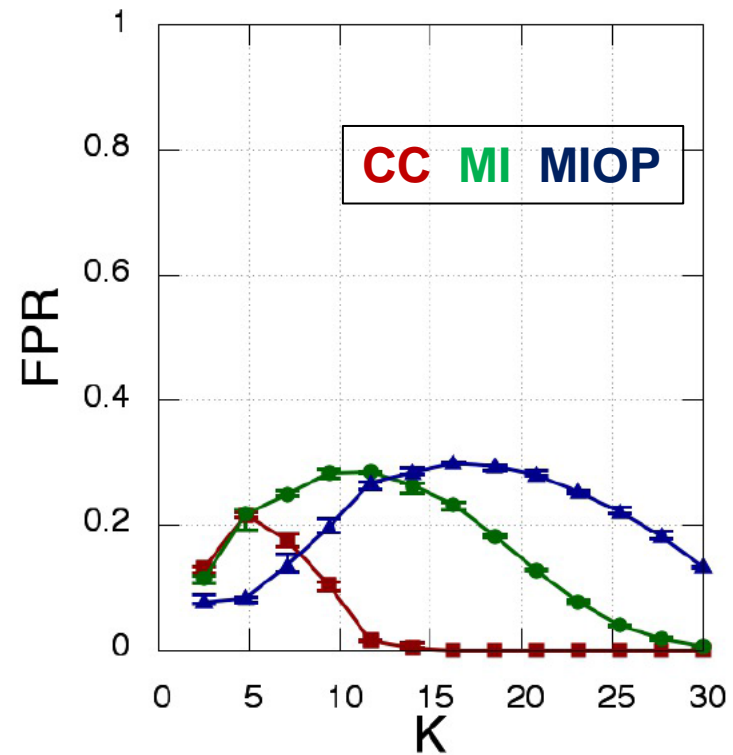
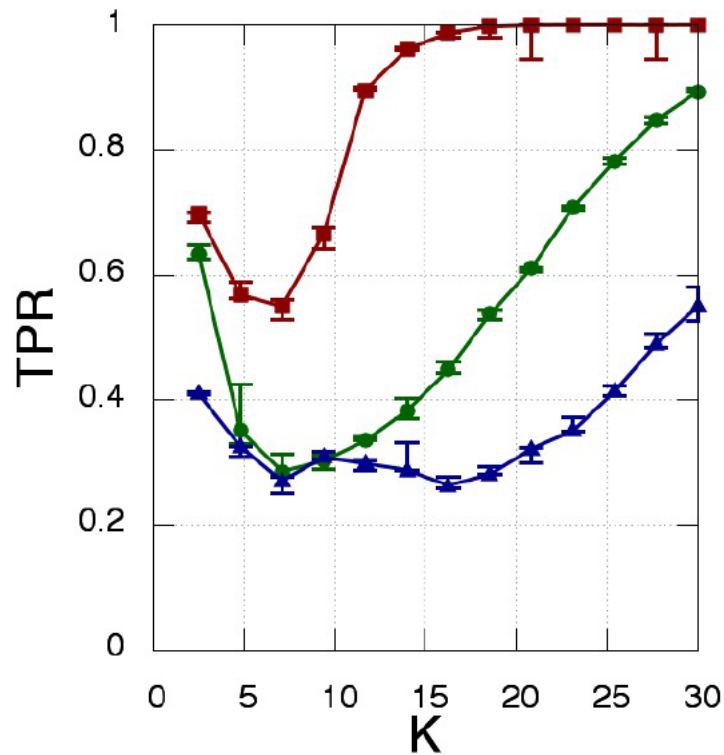
Phases (θ)



“Observables” $Y = \sin(\theta)$



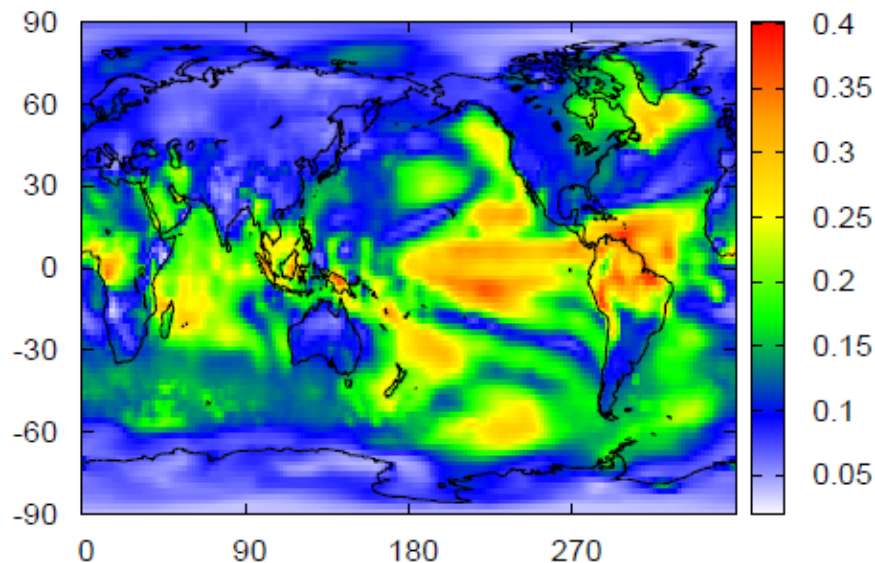
Instantaneous frequencies ($d\theta/dt$)



Also analyzed empirical data from coupled electronic chaotic circuits: results in good agreement with synthetic Kuramoto data.

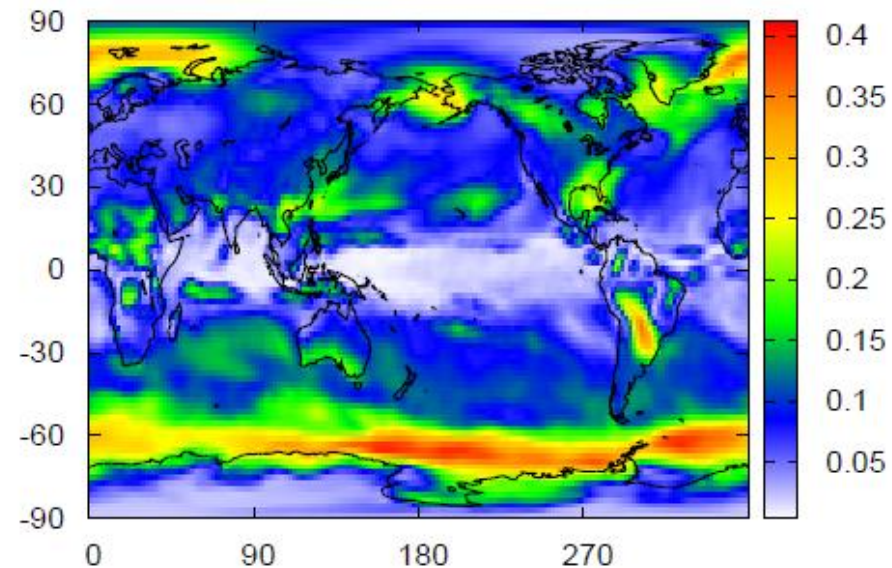
Tirabassi et al, Sci. Rep. **5** 10829 (2015)

Climate network constructed from CC analysis of SAT data



(a) Data anomaly. $p = 10^{-4}$; $d = 0.13$

CC analysis of Hilbert frequencies computed from SAT data



(b) Frequency. $p = 10^{-3}$; $d = 0.13$

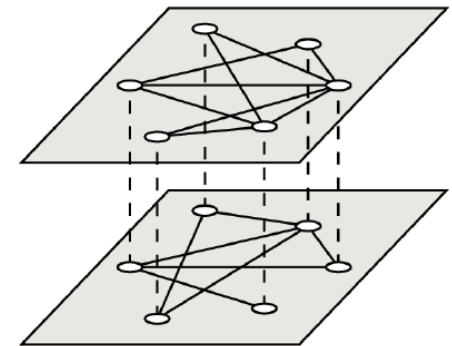
Details in Dario Zappala's poster

Summary: what did we learn?

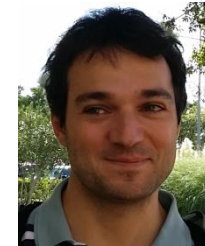
- Take home message: nonlinear time-series analysis unveils relevant information about our climate dynamics, consistent with well-known climate phenomena.

- A few conclusions:
 - No increase of connectivity obtained when taking into account lag-times between annual solar cycles.
 - Atmospheric stochasticity & nonlinearity: nonlinearity mainly in the tropics; possible application: model inter-comparisons.
 - Climate communities: regions with similar thermal inertia or dynamics.
 - DI identifies the net direction & time-scale of information transfer.
 - In a small synthetic network, CC analysis of the instantaneous frequencies allowed perfect network inference.

- Favored / infrequent patterns in climate dynamics?
- Quantifying time-evolving networks via a novel network dissimilarity measure (poster by Laura Carpi).
- Ordinal analysis & multiplex networks:
 - in different seasons (winter, summer) or years (El Niño / La Niña)
 - from different fields (pressure, wind velocity, etc.)
- Networks in shorter time-scales (sub-seasonal).



- Ignacio Deza (UPC)
- Giulio Tirabassi (UPC)
- Dario Zappala (UPC)
- Laura Carpi (UPC)
- Fernando Arismendi
Universidad de la República, Uruguay
- Marcelo Barreiro
Universidad de la República, Uruguay





THANK YOU FOR YOUR ATTENTION !

<crisrina.masoller@upc.edu>

[Climatelinc.eu](http://www.fisica.edu.uy/~cris/)

<http://www.fisica.edu.uy/~cris/>

M. Barreiro et al, Chaos 21, 013101 (2011).

J. I. Deza et al, Eur. Phys. J. Special Topics 222, 511 (2013).

G. Tirabassi and C. Masoller, EPL 102, 59003 (2013).

J. I. Deza et al, Chaos 25, 033105 (2015).

G. Tirabassi et al, Sci. Rep. 5, 10829 (2015).