

Extreme Pulses in Optically Injected Semiconductor Lasers: Precursors and on-demand Generation

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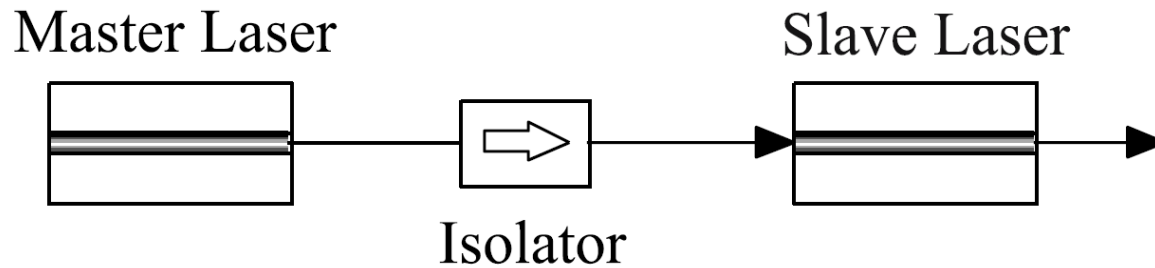
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Zurich, July 2018*



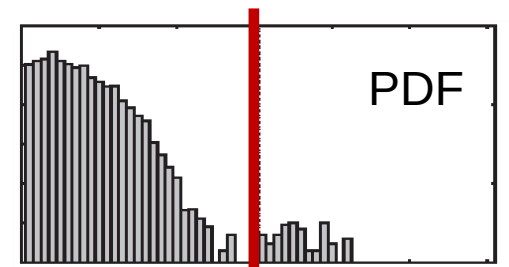
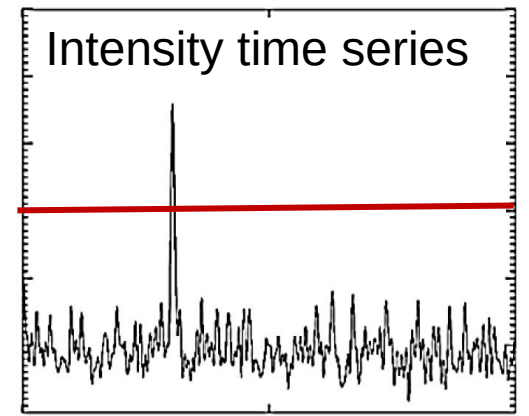
Deterministic Optical Rogue Waves

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José R. Rios Leite,^{2,3} and Jorge R. Tredicce^{2,3}



Parameters:

- Injection ratio
- Frequency detuning
(controlled via the pump current)



RW: pulse above

$$\langle A \rangle + \mathbf{6-8} \sigma$$

Questions

In our system:

- Which mechanism induces ultra-high pulses (rogue waves) ?
- Role of noise ?
- Can the RWs be suppress ?
- Can they be predicted ?
- Can they be generated “on demand” ?

Governing equations

Complex field, **E** –**Laser intensity** $\sim |E|^2$

Carrier density, **N**

$$\frac{dE}{dt} = \frac{1}{2\tau_p} (1 + i\alpha)(N - 1)E + \underbrace{i\Delta\omega + \sqrt{P_{\text{inj}}}}_{\text{optical injection}} + \underbrace{\sqrt{2\beta_{\text{sp}} / \tau_N} \xi(t)}_{\text{spontaneous emission noise}}$$

$$\underbrace{\frac{dN}{dt} = \frac{1}{\tau_N} (\mu - N - N|E|^2)}_{\text{Solitary laser parameters: } \alpha, \tau_p, \tau_N, \mu}$$

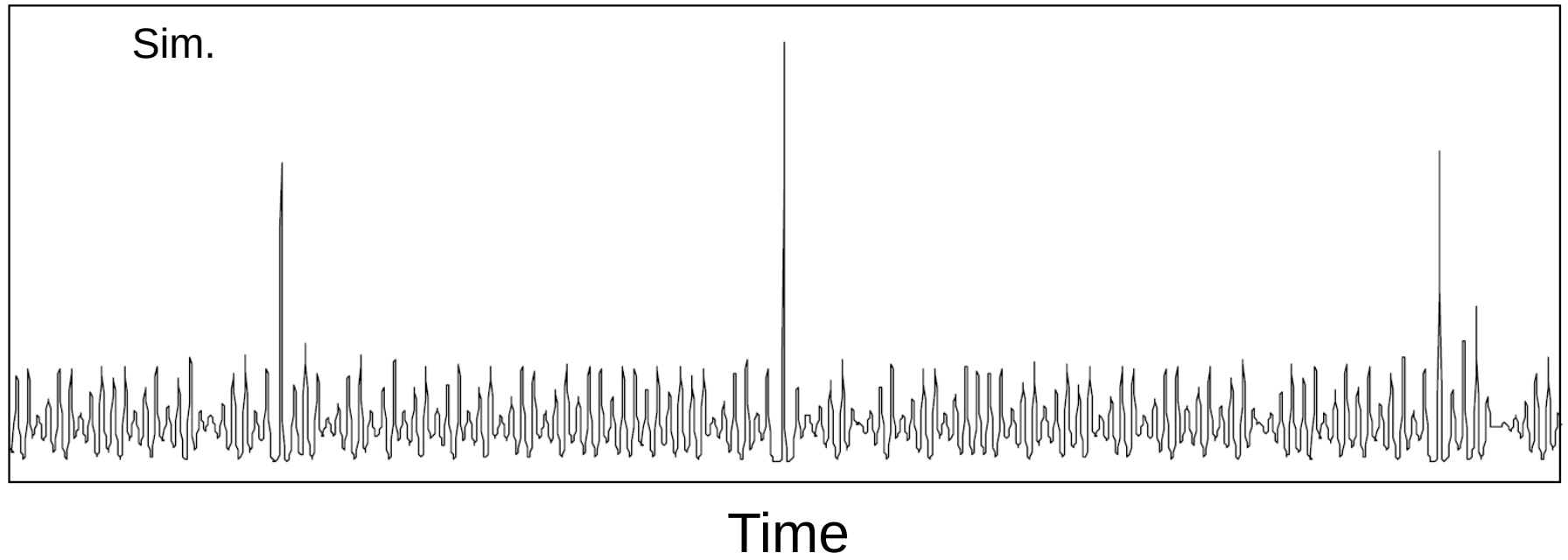
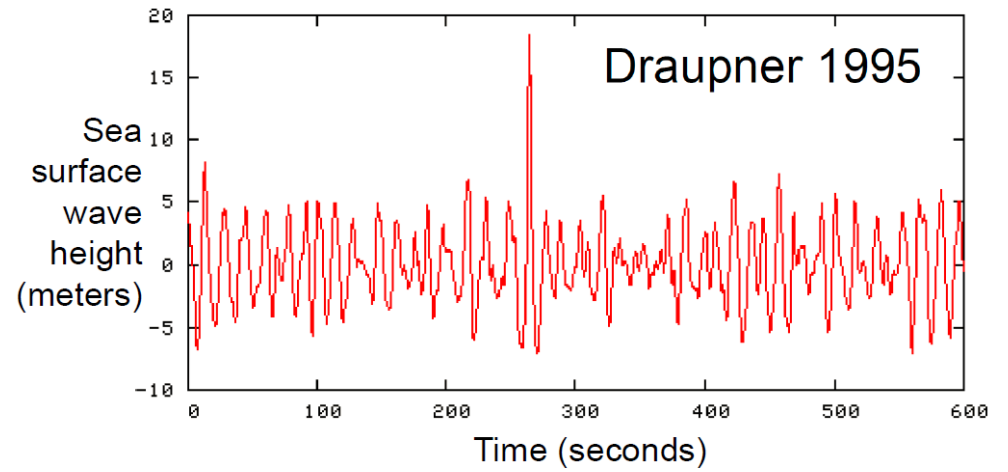
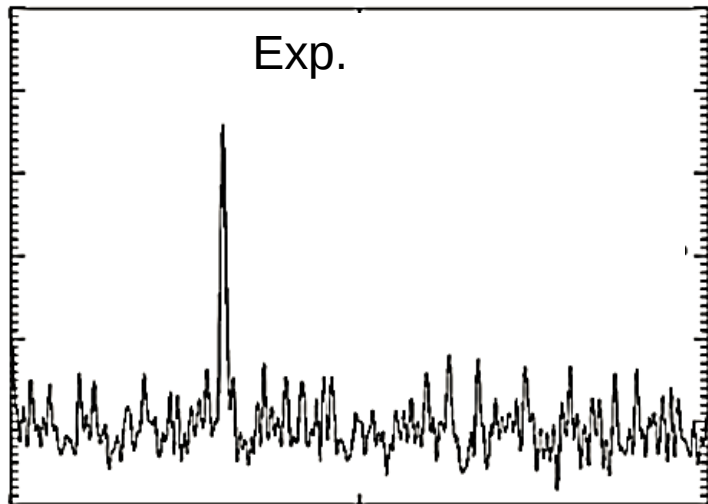
η : injection strength
 $\Delta\omega = \omega_s - \omega_m$: detuning

Typical parameter values:

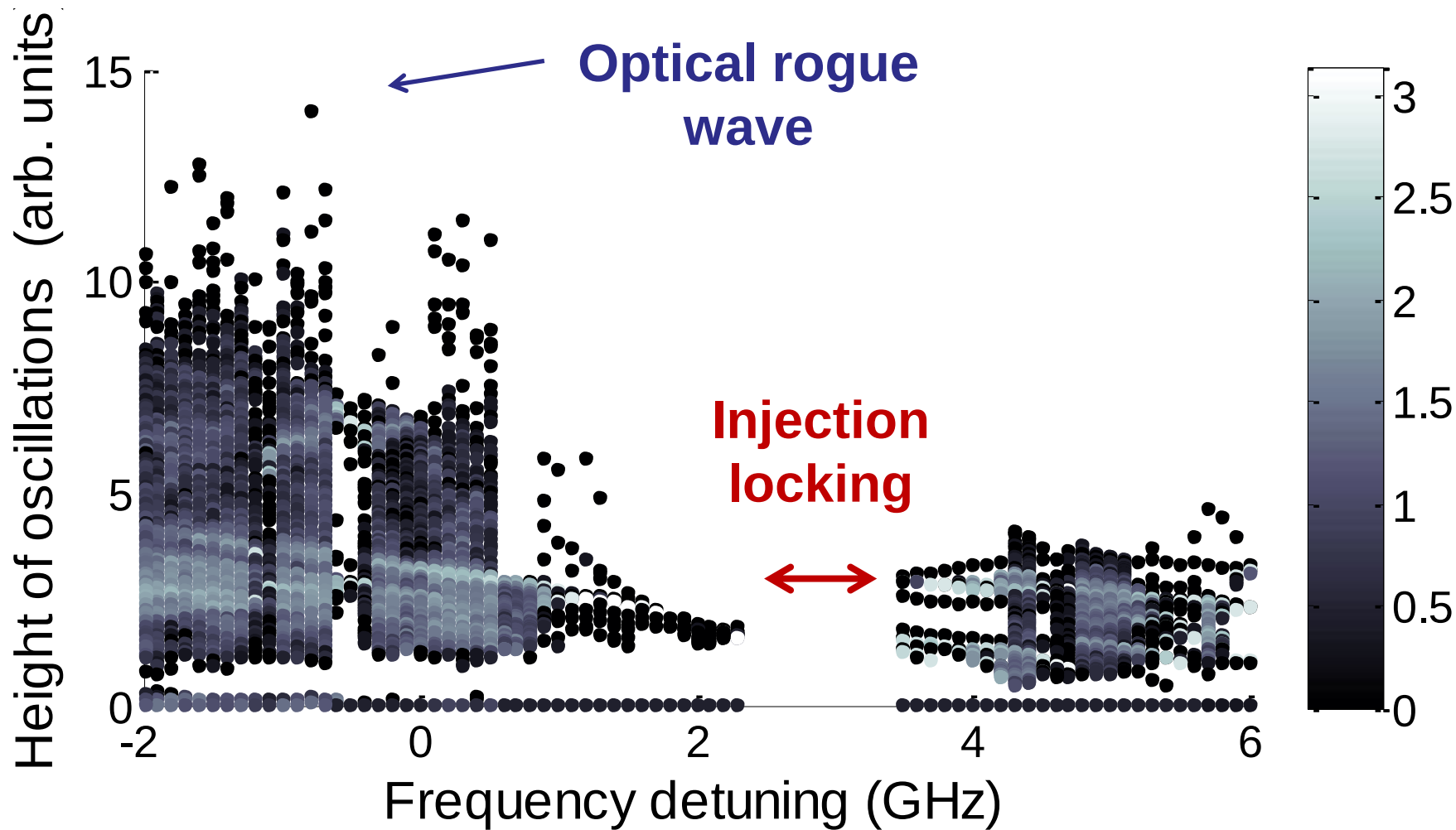
$\alpha = 3, \tau_p = 1 \text{ ps}, \tau_N = 1 \text{ ns}$

μ : normalized pump current parameter

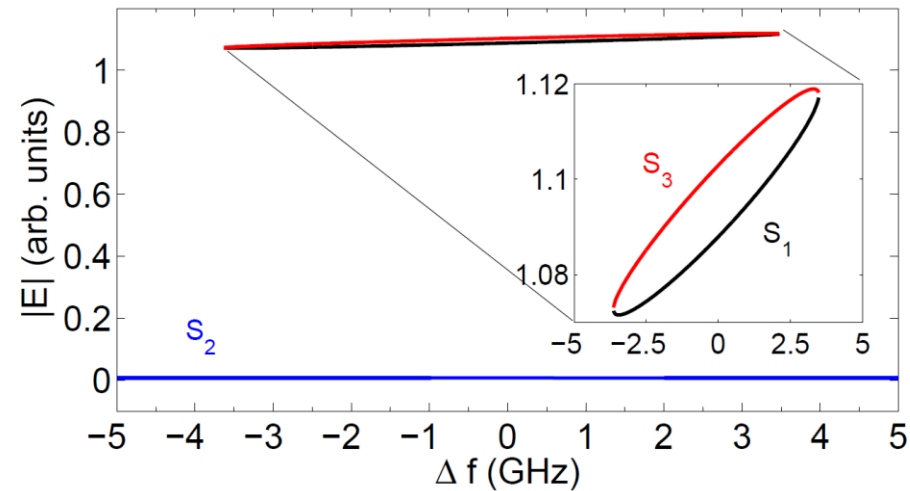
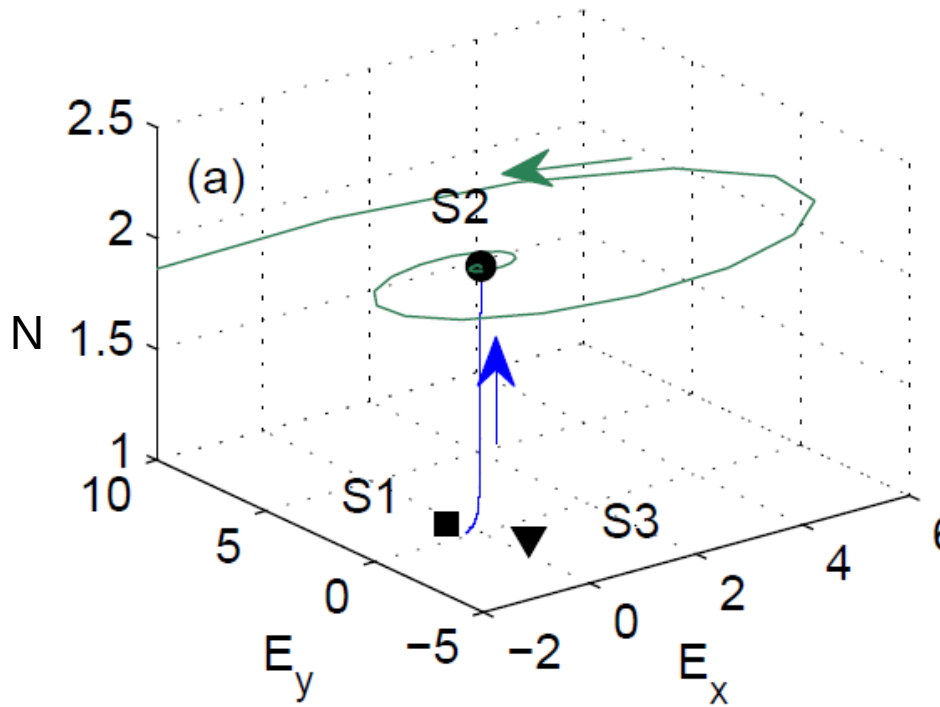
These 0D rate-equations provide good qualitative agreement with the experimentally observed intensity dynamics.



Bifurcation diagram: in color code: $\log(\# \text{ of pulses})$

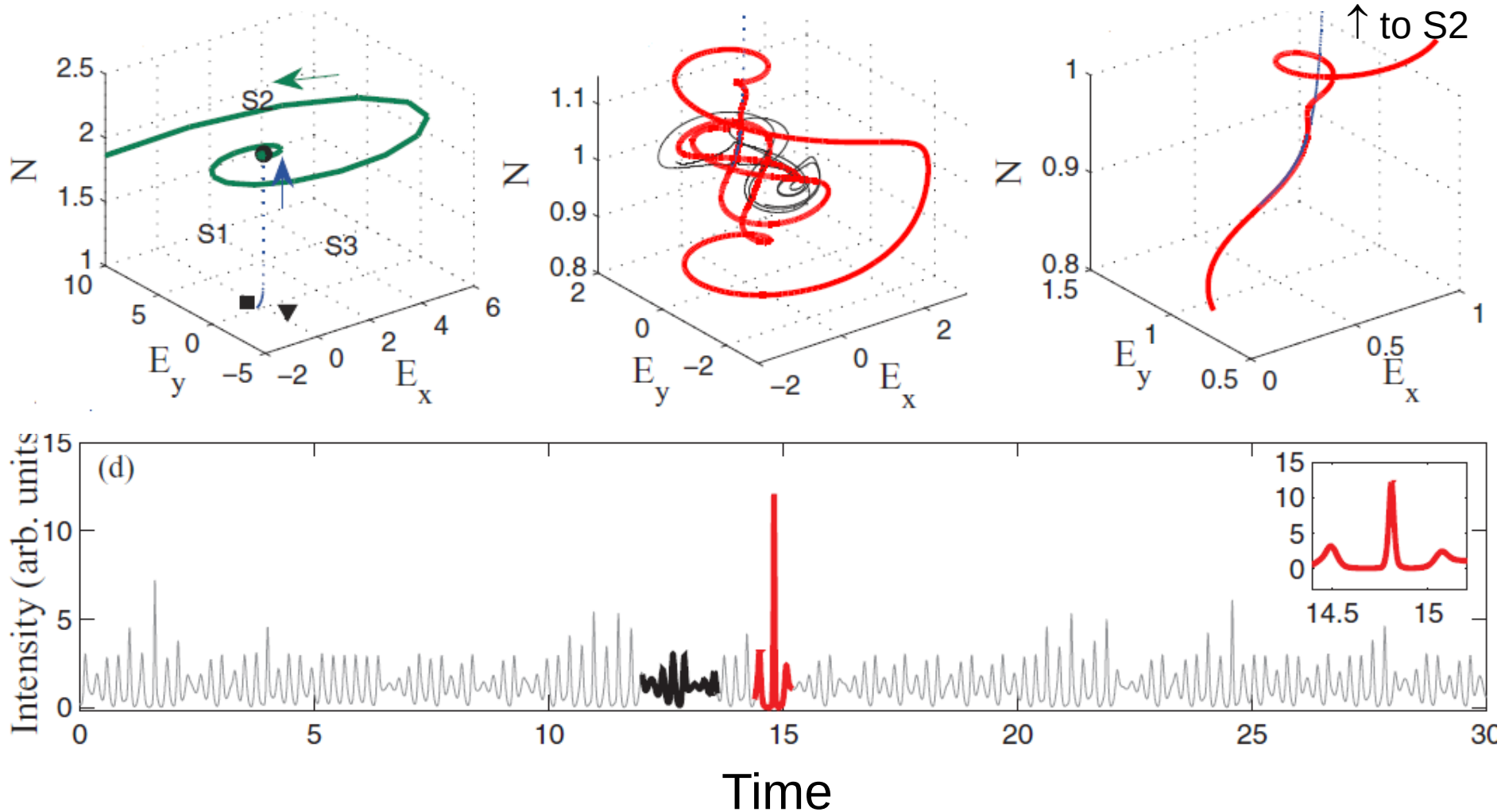


To understand the mechanism underlying the extreme pulses we need to examine the location the **three fixed points**.

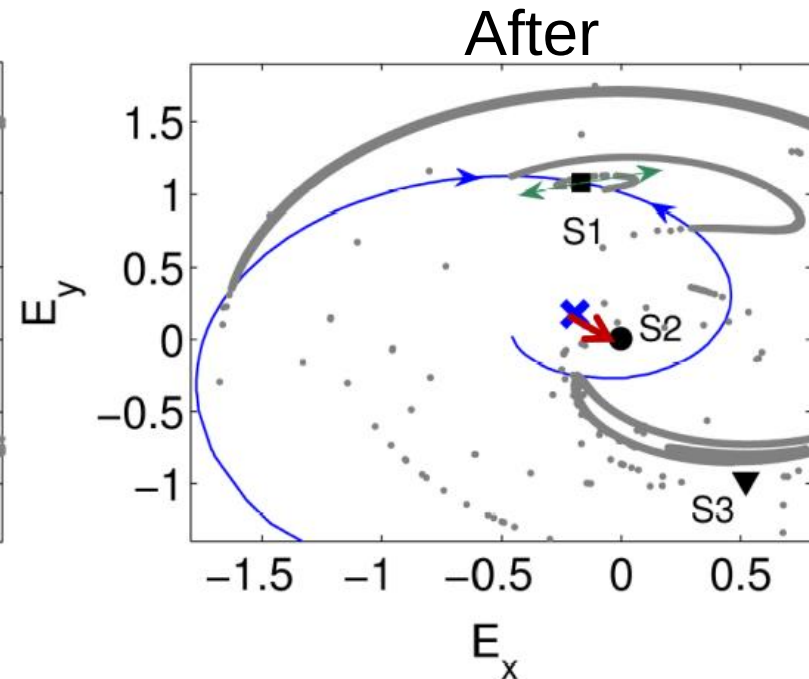
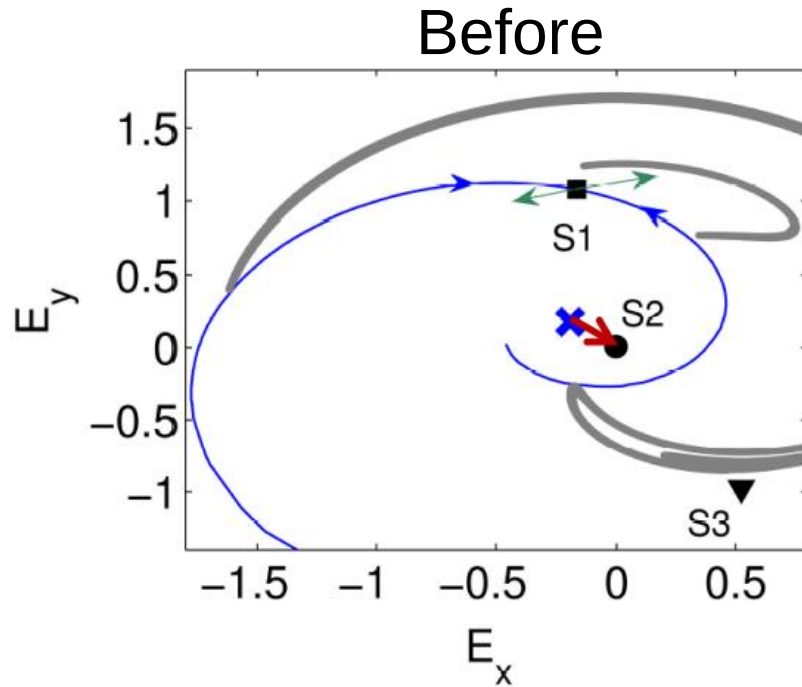
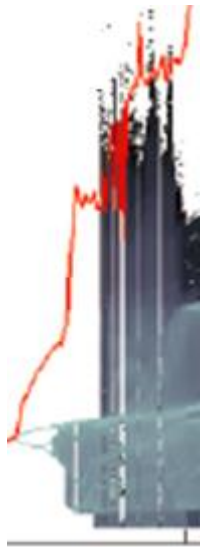


During an extreme pulse the trajectory moves towards S_1/S_3 ?

A **RW** is triggered whenever the trajectory closely approaches the stable manifold of **S2** (the “RW door”)



With the Poincare map ($N=1$) we see the expansion of the attractor when RWs appear.



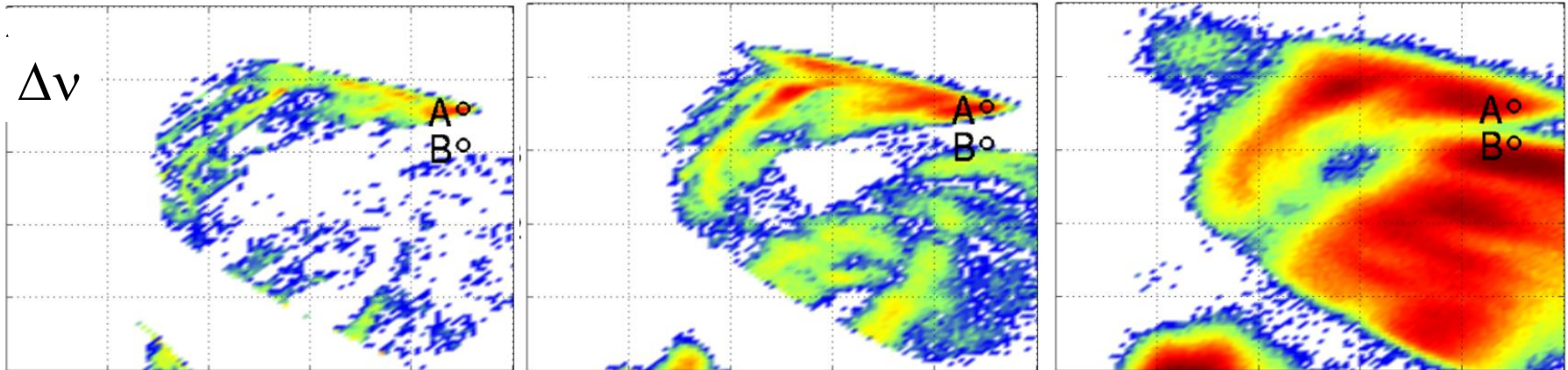
J. Zamora-Munt et al. PRA (2013).

Noise can induce RWs

Noise strength

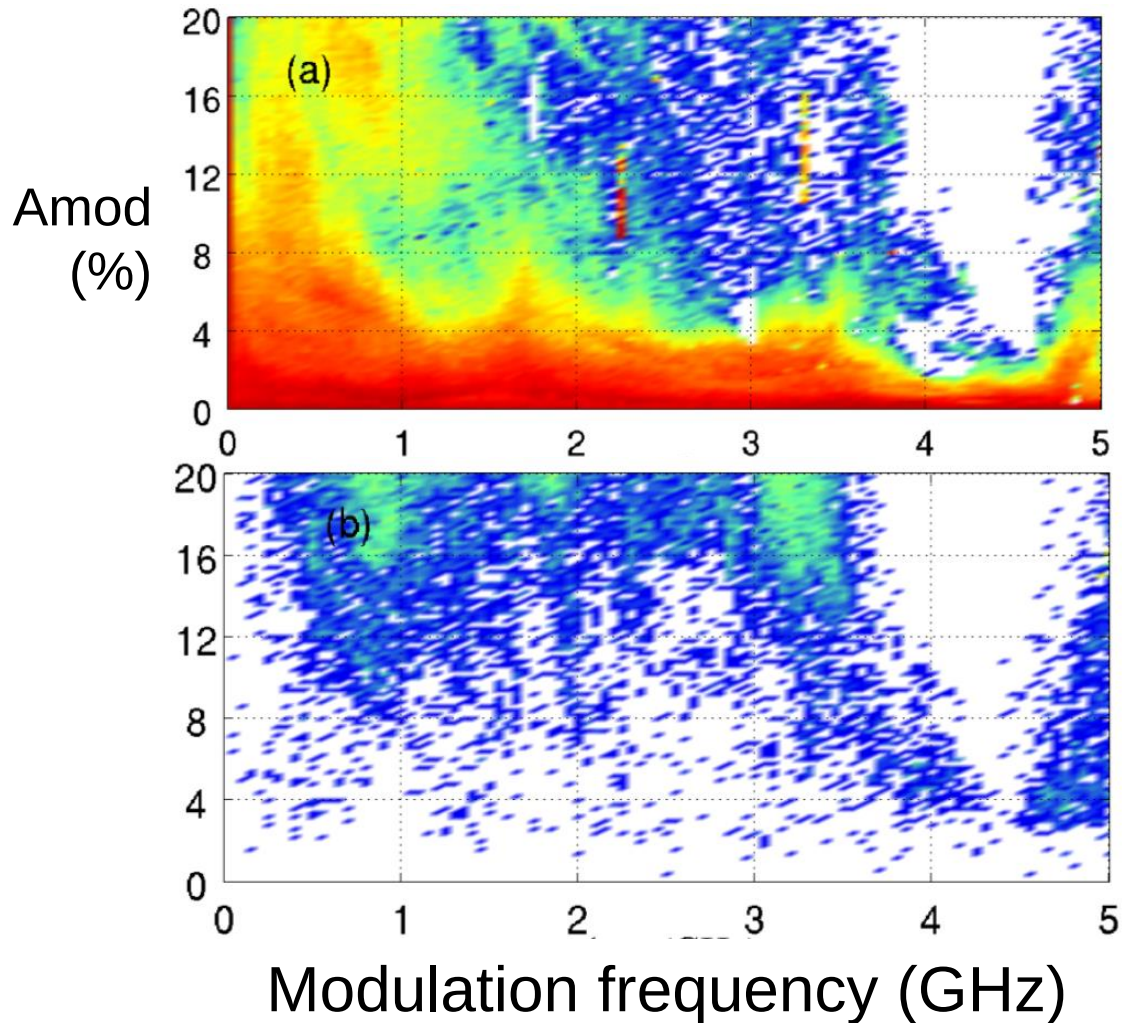


In color code the
number of RWs



Pump current parameter

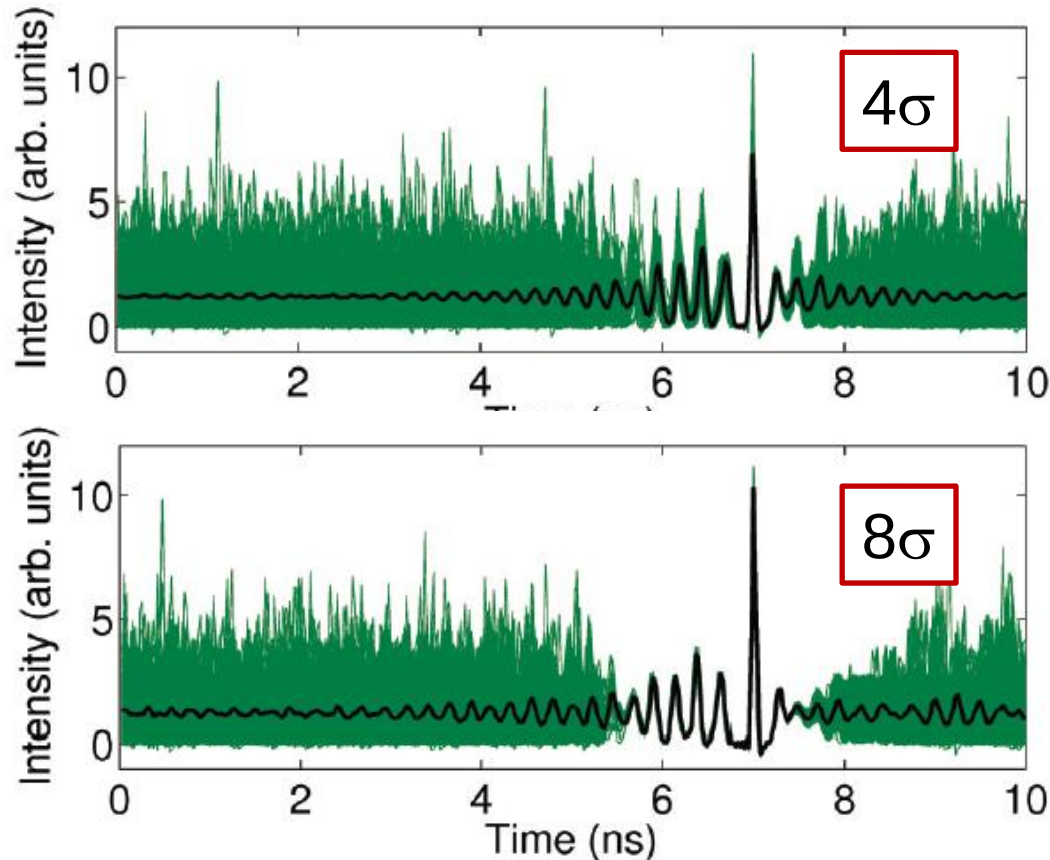
Current modulation can suppress RWs, but can also induce RWs



In color code the number of RWs

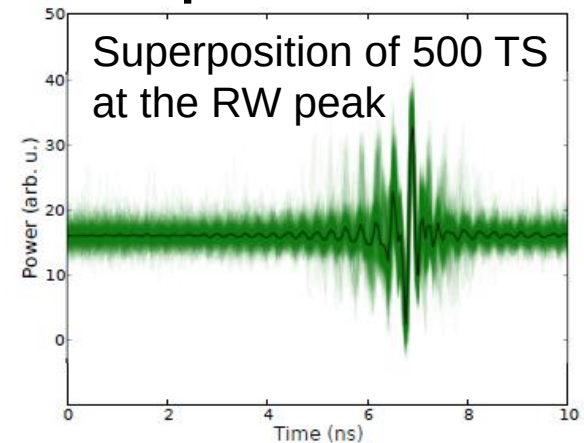
Predictability?

Deterministic simulations



Superposition of 50 time-series at the RW peak

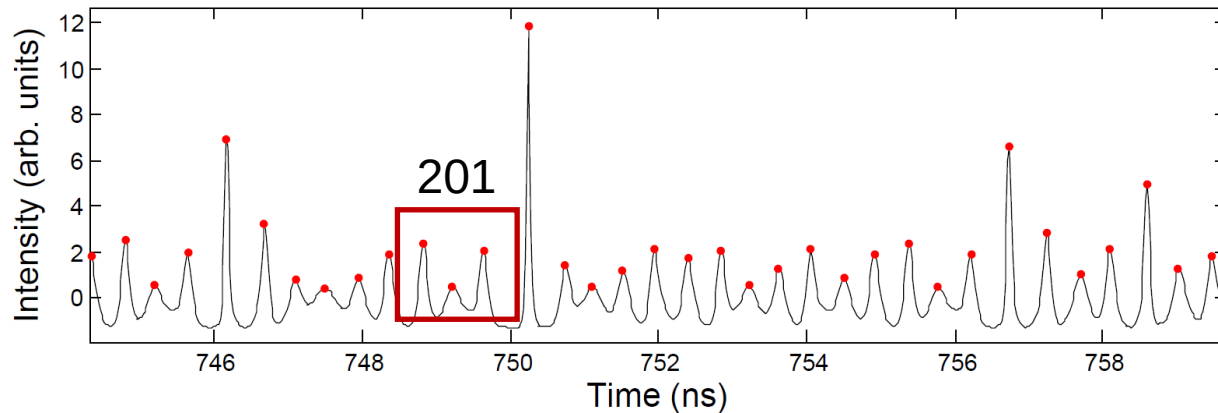
Experiments



⇒ Well-defined oscillation pattern anticipates extreme pulses.

How can this effect be quantified?

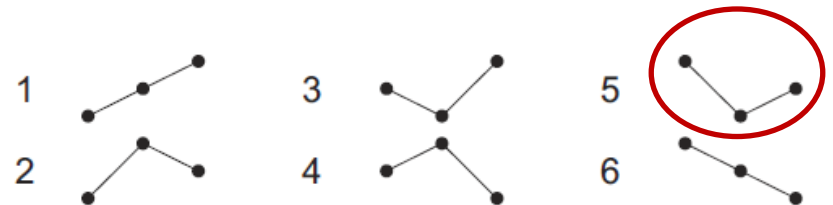
Identifying the pattern that tends to occur before the pulse



- Consider the sequence of intensity peak heights (red dots):

$$\{\dots, I_i, I_{i+1}, I_{i+2}, \dots\}$$

- Possible order relations of three consecutive values:

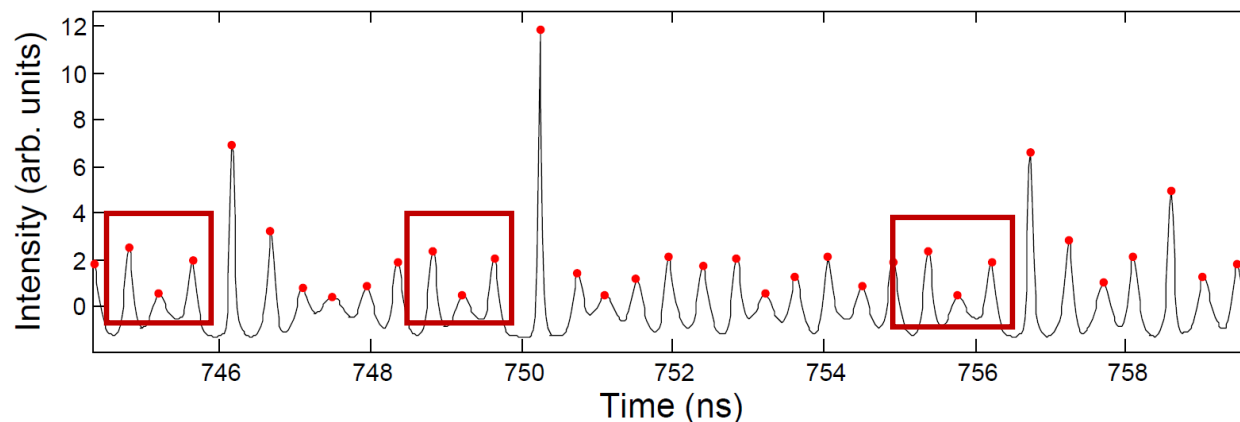
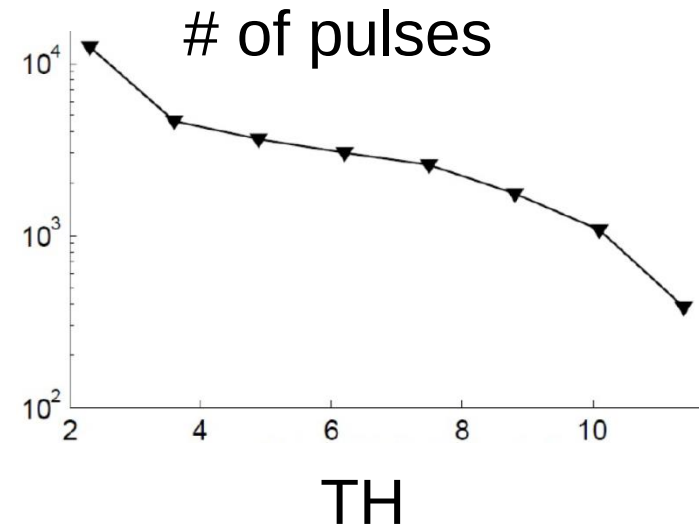
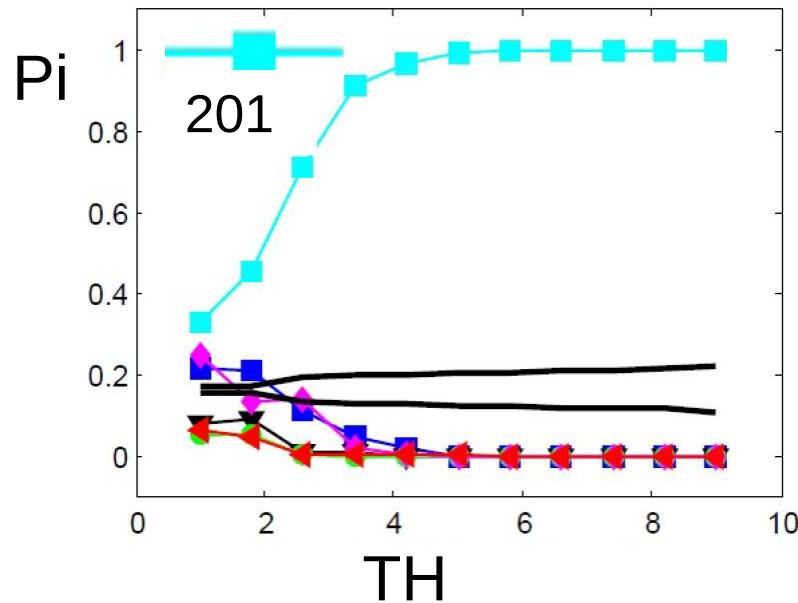


We calculate the probability of the pattern that occurs before each high pulse:

If $I_i > \text{TH}$, we analyze the pattern defined by $(I_{i-3}, I_{i-2}, I_{i-1})$

“Good” results in deterministic simulations: $P(201)=1$ if $TH > 6$

Black lines:
 3σ
 confidence
 probabilities
 consistent
 with $p_i=1/6$
 $\forall i$

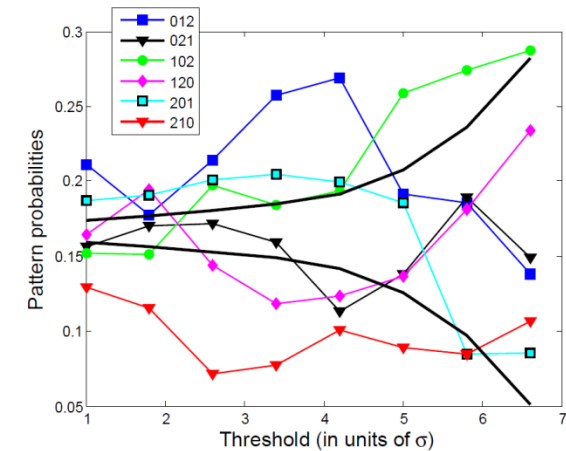
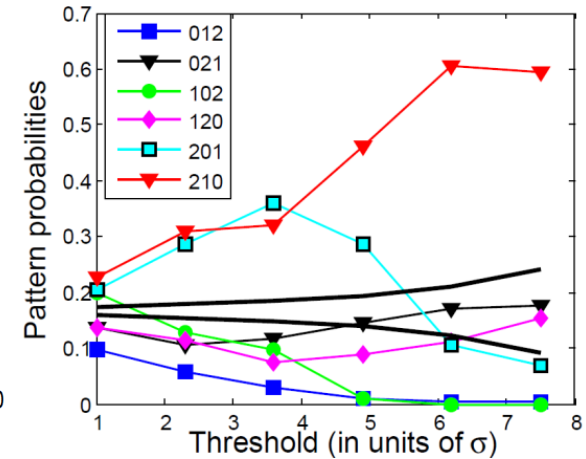
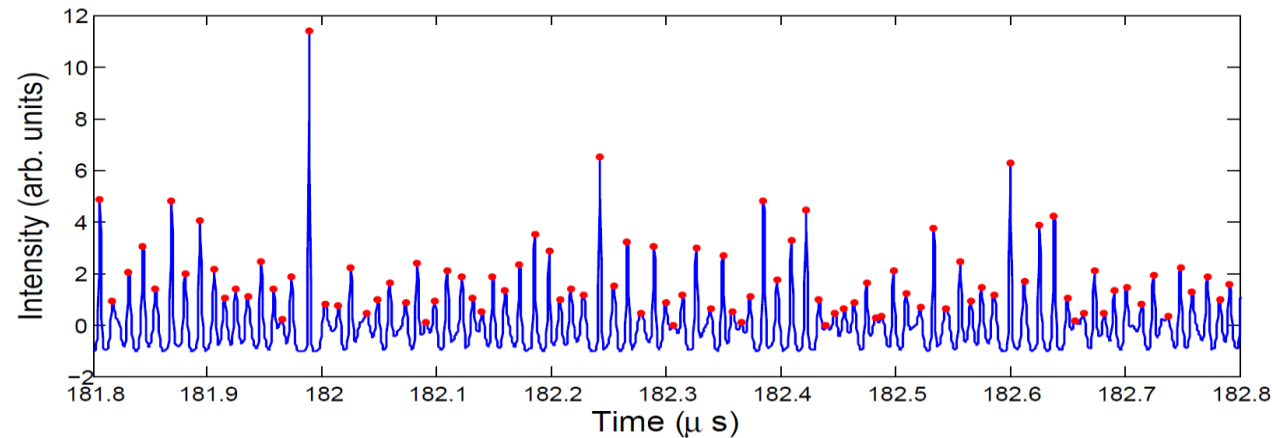
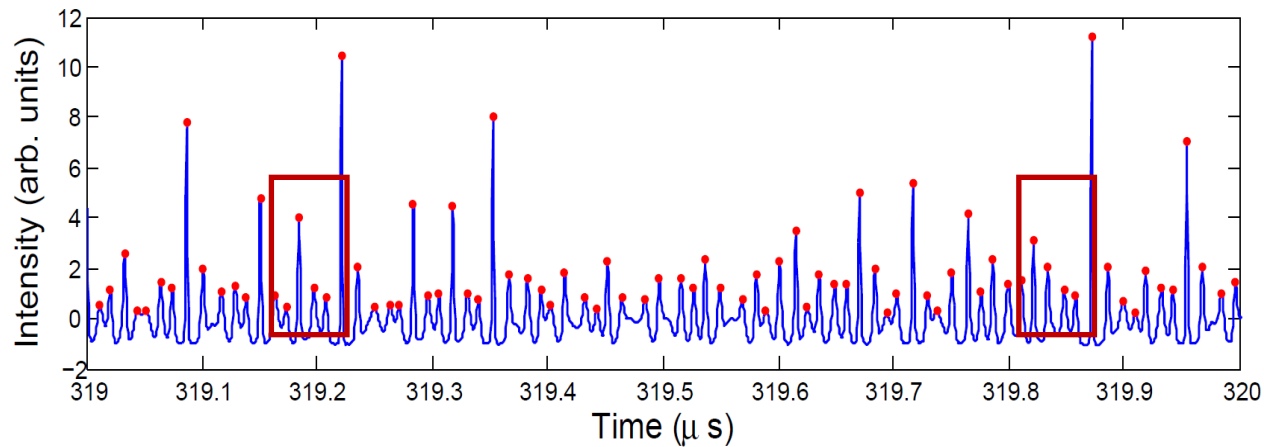


Problem:

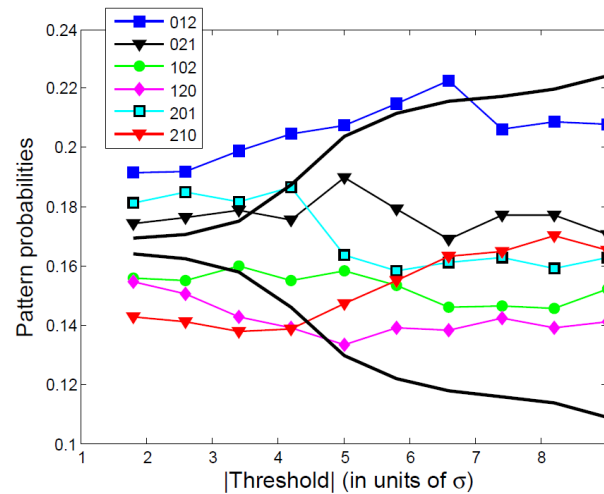
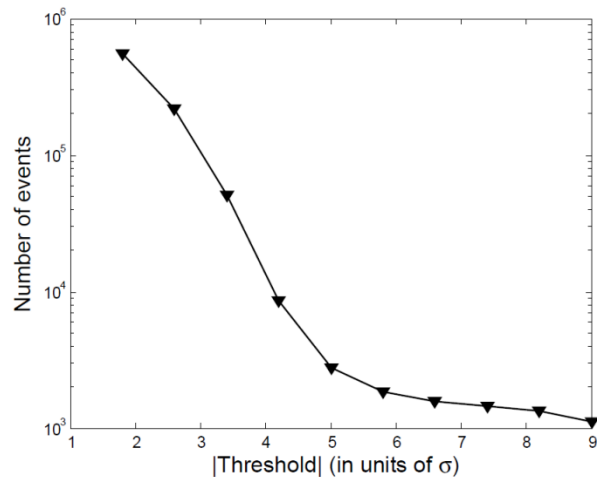
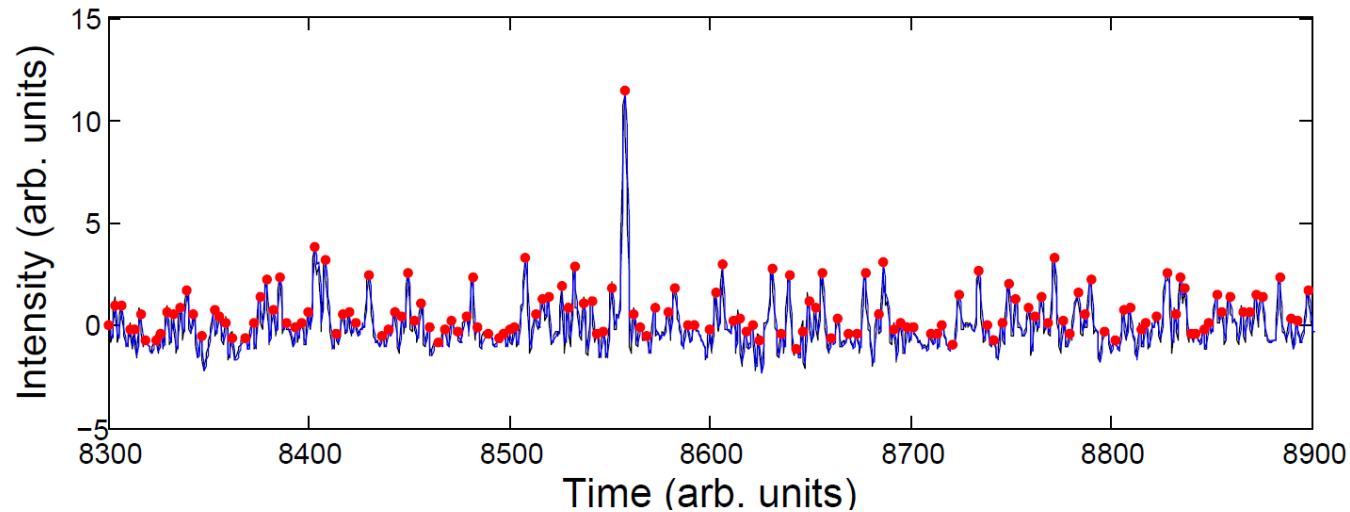
$P(201) \neq 0$ if $TH < 6$
 (pattern 201 also anticipates some small pulses) $\Rightarrow$
 false alarms (false positives)

The “early warning pattern” varies with the parameters and might not exist.

Including noise, two modulation frequencies



Analysis of experimental data



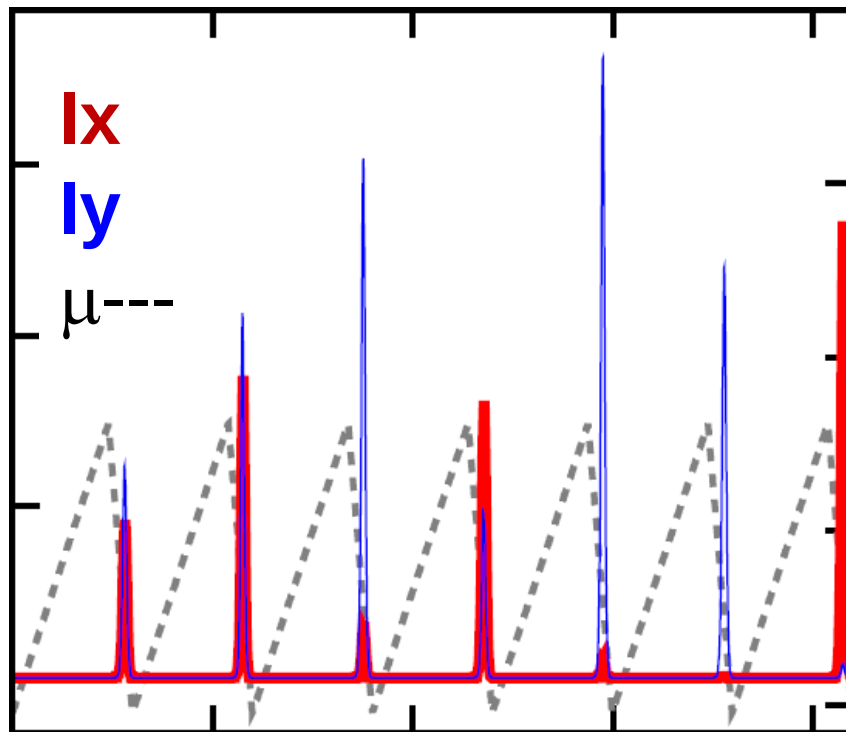
Way to improve the “early warning”:

- Filter noise
- Longer patterns

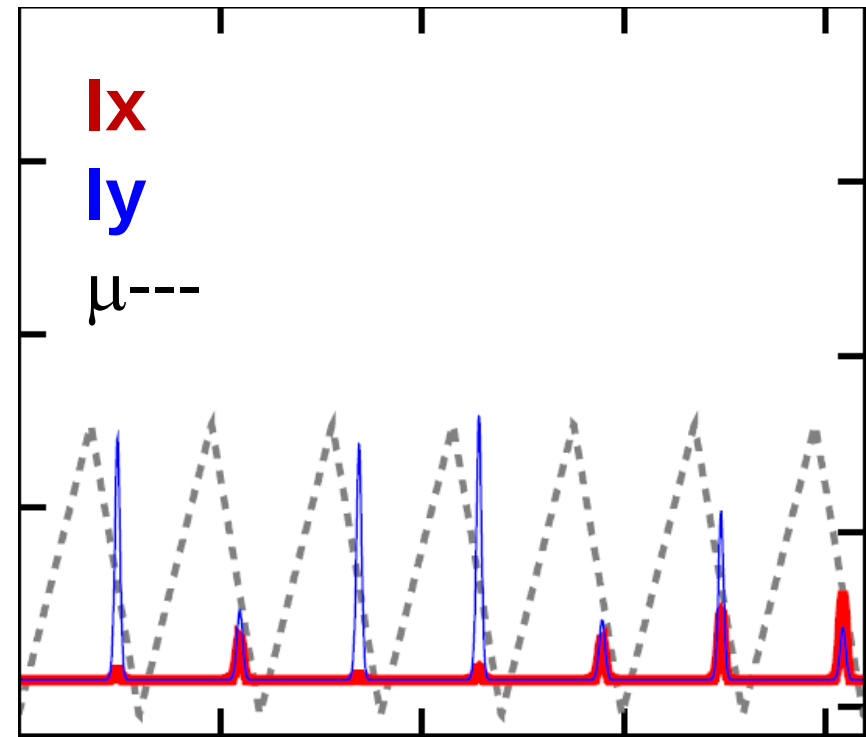
$\{\dots l_i, l_{i+1}, l_{i+2}, l_{i+3}, \dots\}$

Data from S. Barland, M. Giudici (Nice)

On demand generation? Simulations of VCSEL model



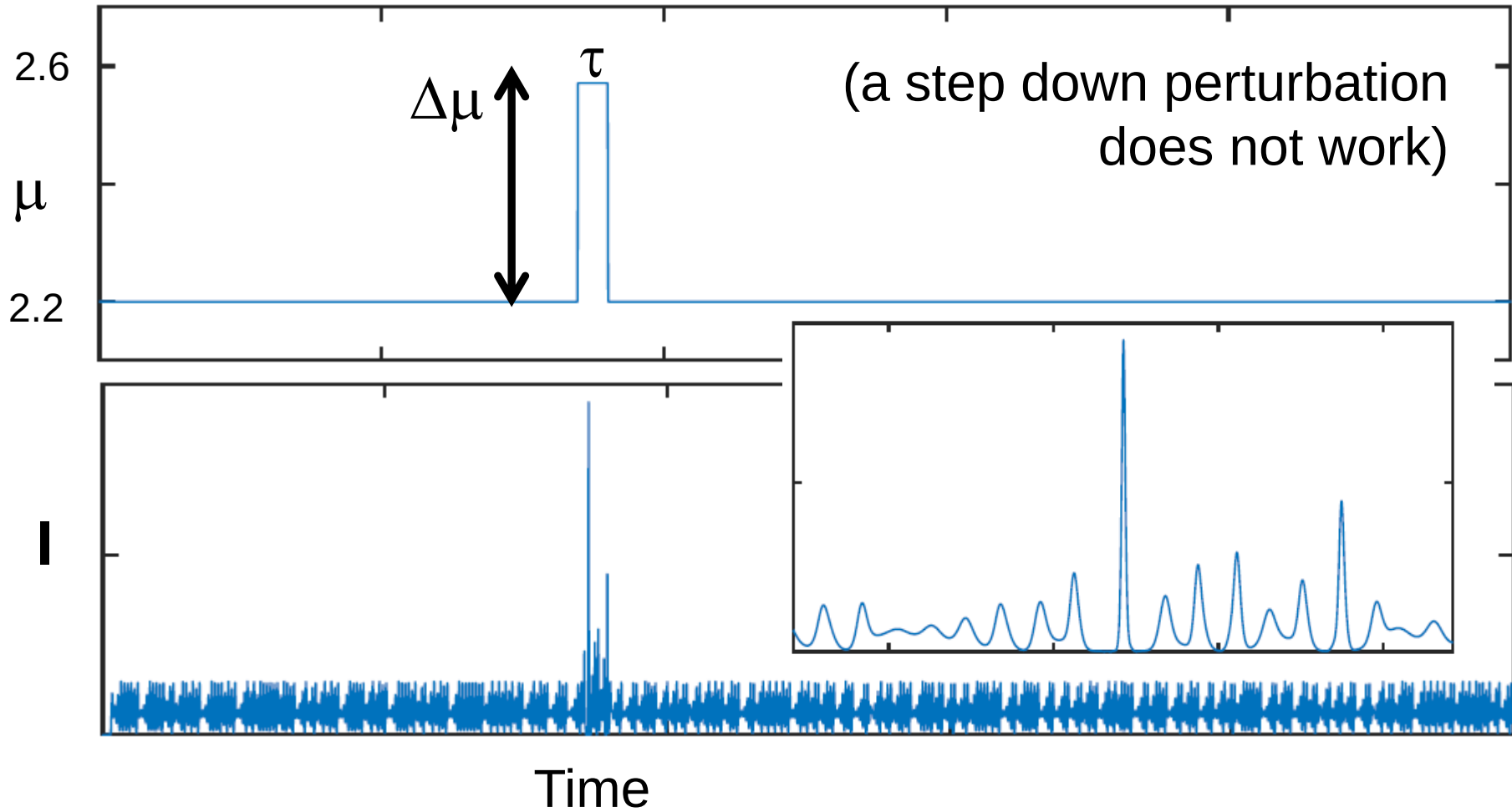
Time



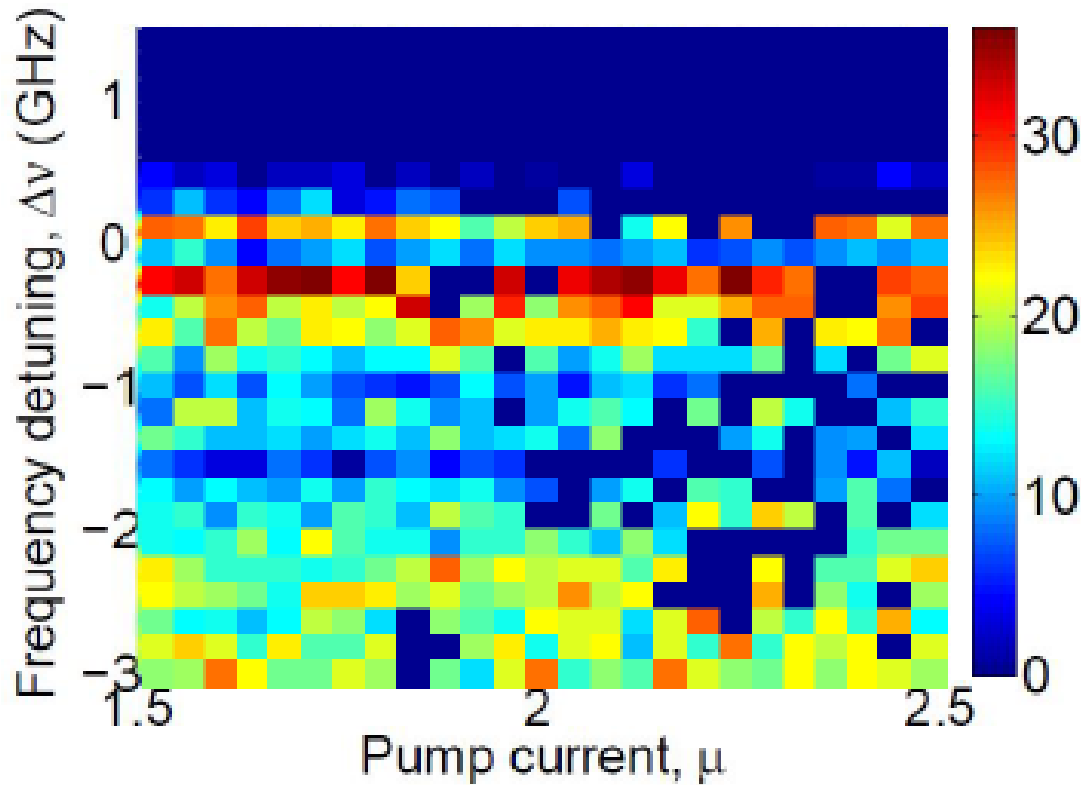
Time

Zamora and Masoller, Opt. Express (2008).

On demand generation?

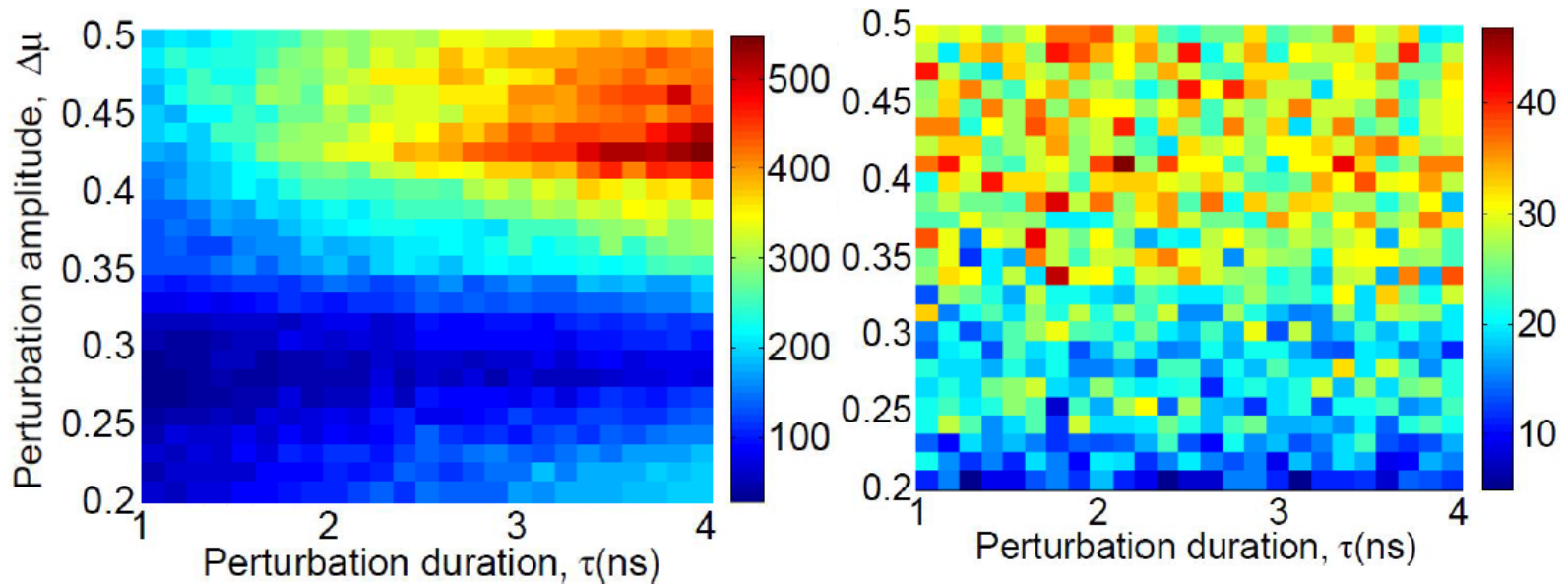


Where in the parameter space is easier to generate pulses?



100 perturbations.
In regions where
there are “natural”
extreme pulses,
no perturbation is
applied.

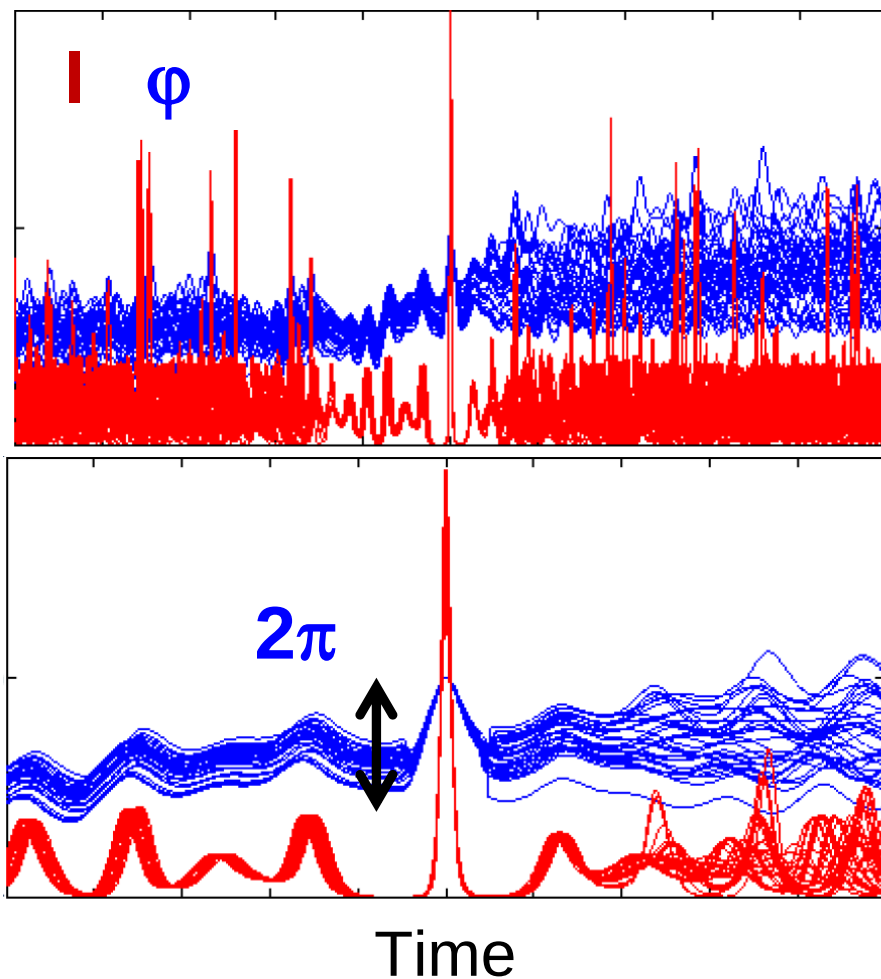
**The number of RWs generated after 1000 perturbations as a function of the perturbation parameters:
can be as large as 50% or as small as 5%**



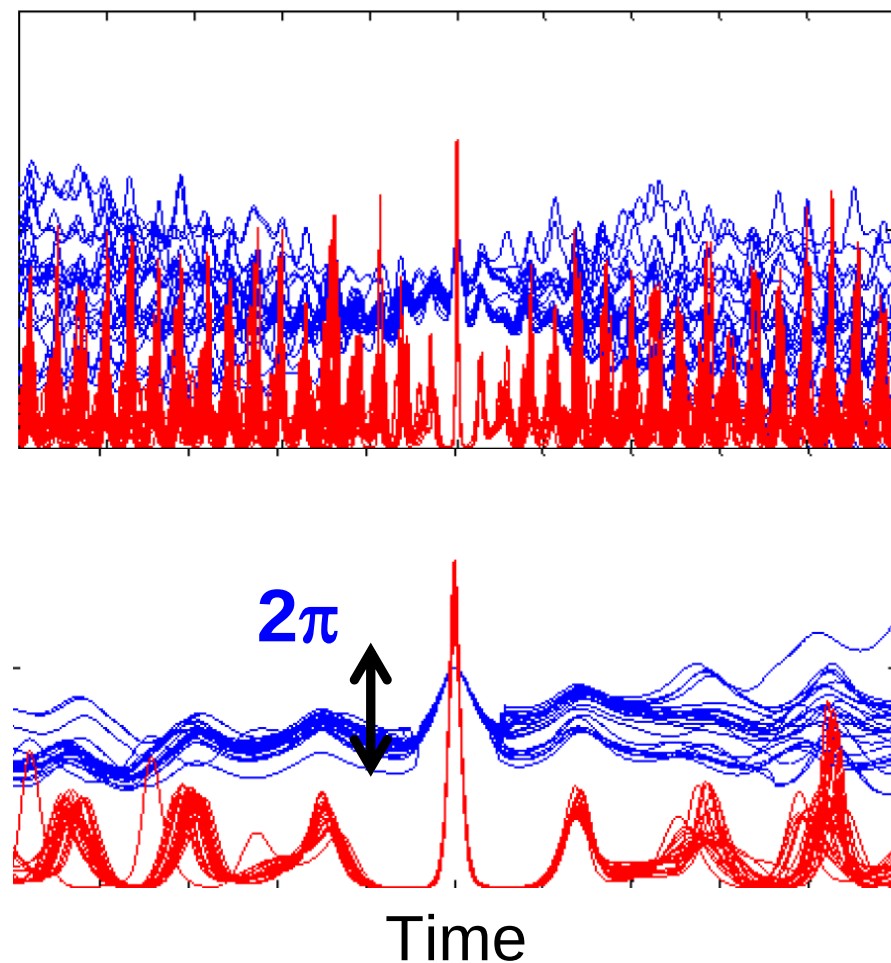
The “success rate” depends on the laser parameters and on the perturbation parameters.

Are the generated pulses similar to the “natural” ones?

“Natural”



“On demand”



Summary

- Extreme optical pulses can be deterministic or triggered by noise, and can be suppressed by current modulation.
- Certain patterns of oscillations can be more (or less) likely to occur before the extreme intensity pulses.
- Extreme pulses can be generated “on demand” by appropriated perturbation of the pump current parameter.
- Ongoing work: potential for sensing applications?
- To do in the future: the symbolic approach to predict extreme events in empirical data needs to be explored.



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Tian Jin, Chen Siyu, and C. Masoller, “*Generation of extreme pulses on demand in semiconductor lasers with optical injection*”, Opt. Express **25**, 031326 (2017).

